Study of Qualitative and Quantitative Metric for Pixel Factor Mapping and Extended Pixel Mapping Method

Indradip Banerjee, Souvik Bhattacharyya, Gautam Sanyal

Abstract—In this paper, an approach is presented to investigate the performance of Pixel Factor Mapping (PFM) and Extended PMM (Pixel Mapping Method) through the qualitative and quantitative approach. These methods are tested against a number of well-known image similarity metrics and statistical distribution techniques. The PFM has been performed in spatial domain as well as frequency domain and the Extended PMM has also been performed in spatial domain through large set of images available in the internet.

Keywords—Qualitative, quantitative, PFM, EXTENDED PMM.

I. INTRODUCTION

CECURITY of information is one of the aspect of Dinformation technology and communication system. Computer, Laptop, etc. are the most important communication media that can join different parts of the world through internet. In contradiction, safety and security communication systems are the challenging issue in day to day life. Consequently, the concept of "Information Hiding" [1] has been introduced by the researchers. After that, the theory of cryptography [2] and the concept of watermarking [3] have been established. But nowadays, by rising computational supremacy, regular cryptographic and watermarking algorithms have been established to be evidence for weak point against mathematical and statistical methods. The research on reverse engineering techniques has increased the processing power. So, the most important race between researches in cryptanalysis [4] and watermarking detection [5] has been developed. To solve the problems, the concept of steganography [6] has been established by the researchers. Steganography diverges from cryptography. Cryptography is a secure communication which changes the information into a specific form and so an eavesdropper cannot recognize it. Steganography techniques attempt to hide the existence of the message itself, so that an observer does not know that the data are even there or not.

Steganography gives the certification over the data using some tag or labelling on some objects like text, audio, video, image. Fig. 1 illustrates the types of steganography used in modern days.

Hiding the existence of the message and creating the covert

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channel is the objective of the Steganography. The message is hidden in another object. Consequently, the transmitted item will be identical, considering to every individual's eye. Steganalysis is the art of detecting any hidden data on the communication channel. Steganography is rumpled when the presence of the hidden message is uncovered. Fig. 2 shows the framework of the steganography.

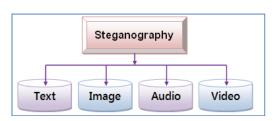


Fig. 1 Types of Steganography

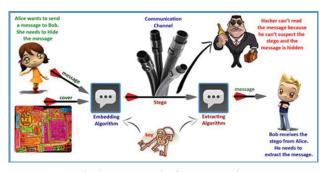


Fig. 2. Frame Work of Steganography

PFM [7], [8] is based on both spatial and frequency domains with the help of Gray scale images (512x512). More than 1000 images have been used, which have been collected from image databases that are used by most researchers. In this system, the input message (MSG_{BIT}) can be adopted as digital character format and cope with bit stream. Image converts from spatial domain $(f_{m,n})$ to frequency domain $(f_{x,y})$, in case of frequency domain method. Four-bit pair $\in (x, y)$ has been used for embedding in a separate DCT coefficient of frequency domain method or pixel intensity of spatial domain method. The selection of $\mathcal{L}(x, y)$ depends on one of the author's mathematical function. The selection technique is based on $\mathcal{E}(x, y)$ and its position on the image. Mapping of four bit from the secret message is used for embedding in a pixel's \in (x, y) position, which is based on the maximum prime factor value (PFV) of image $\in (x, y)$ value. PFM Table (Table

I) shows the PFV value of the corresponding 4-bit embedding character. After embedding in $\mathfrak{E}(x, y)$, it is generating the stego $\mathfrak{E}(x_l, y_l)$ and reconstruct the image value $f'_{x,y}$ converting the image $(f'_{x,y})$ from frequency to spatial domain image $(f'_{m,n})$ as stego in frequency domain method. Most of the existing methods can embed one bit per coefficient or pixel intensity, whereas this method can embed four bit per coefficient. Embedding four bit per coefficient can extend the embedding capacity four times than previous methods in spatial or frequency domain. At the receiver side, reverse operation has been carried out to get back the original information.

TABLE I

Prime Factor Value (PFV)	Embed 4 Bit	Prime Factor Value (PFV)	Embed 4 Bit
2	0000	23	1000
3	0001	29	1001
5	0010	31	1010
7	0011	37	1011
11	0100	41	1100
13	0101	43	1101
17	0110	47	1110
19	0111	53	1111

Extended PMM: This method is an extension of PMM method [9] which is based on special domain with the help of gray scale images (512x512). The input message can be adopted as digital character format. Two bit pair has been used for embedding in a separate pixel and the selection of embedding pixel also depends on mathematical function. The selection technique is based on pixel intensity value and pixel position on image. Mapping of two bit from the secret message is used for embedding in a pixel which is based on the intensity value, previous pixel value and number of the ones (in binary) present in that pixel. The existing PMM twobit tables have been used here for mapping and the previous embedded pixel intensity value used for mapping. The concept of previous pixel intensity value is added in this work along with the embedding pixel selection method. Extraction process starts again by selecting the same reverse process required during embedding. At the receiver side, the reverse operation has been carried out to get back the original information.

II. APPLIED SIMILARITY METRICS

We explain the experimental results as well as the hiding performance of presented methods based on some similarity metrics, which are discussed below. Capacity of hiding data and imperceptibility of the stego image are tested here using various performance metrics. Imperceptibility of the image is called the quality of the image.

Oualitative Metrics

There is an inclusive range of approaches to qualitative metrics. A qualitative attitude is a general way of thinking about directing qualitative research. It defines, either explicitly or implicitly, the role of the researchers, stages of research and the method of data analysis are the purpose of the qualitative

metrics. Qualitative research is designed to expose a target audience's range of behaviour and the observations that drive it with reference to specific matters or issues. It uses comprehensive studies of small groups of data to monitor and sustenance the construction of theories. The results of qualitative research are descriptive, predictive, collection of word data and question answers.

The quality of the stego image produced by the proposed methods and the stego image has been tested thorough statistical parameters like Mean, Standard Error Mean, Trimmed Mean, Standard Deviation, Variance, Coefficient of Variation, Sum, First quartile (Q_1) , Median (Q_2) , Third quartile (Q_3) , Range, Interquartile (IQR), Mode, N for Mode, Kurtosis, MSSD and Covariance etc. The hypothesis tests i.e. the goodness of fit tests have also been used for better distribution with the help of Kolmogorov Smirnov Test. The rank and statistic value can measure the goodness of fit [10] and it also declares the best fitted distribution technique for the image. The details of the tests are discussed below:

Mean: The mean [11] is used to denote one measure of the central tendency either of a probability distribution or random variable which is characterized by distribution technique in statistics or probability. The mathematical expectation, arithmetic mean and average are used to refer a central value of a discrete data set. The sum of the values divided by the number of values is the mean. In case of finite population and by considering every member of that population, the population mean of a property is equal to the arithmetic mean of the given property. For example, the population mean weight is equal to the sum of the weights of every individual divided by the total number of individuals. For the small sample data set, the sample mean may diverge from the population mean.

Standard Error Mean: The standard error (SE) [12] of the mean is the standard deviation of a sampling distribution of a statistic, most commonly it also called the standard deviation of the mean. The term may also be used to refer to an estimate of that standard deviation, consequent from a particular sample used to compute the estimate.

Trimmed Mean: A truncated mean or trimmed mean [13] is a statistical degree of central tendency and this is like mean and median. It involves the calculation of the mean after disposal of given parts of a probability distribution or sample at the high and low end. This number of points to be cast-off is usually given as a percentage of the total number of points, but may also be given as a fixed number of points.

Standard Deviation: In the statistics, the standard deviation [14] is a measure that is used to quantify the amount of variation or diffusion of a data set. The standard deviation is represented by the Greek letter sigma (σ). A standard deviation close to 0 indicates that the data points incline to be very close to the mean, which is also called the expected value of the set. When it is indicating a high standard deviation then the data points are spread out over a wider range of values.

Variance: In probability theory and statistics, the variance [15] measures how extreme a set of numbers is spread out. When a variance is 0, then it indicates that all the values are

identical. Variance is always positive values. A small variance indicates that the data points tend to be very close to the mean i.e. the expected value and hence it is adjacent to each other. While the variance is high then it indicates that the data points are very spread out around the mean and expansive from each other.

Coefficient of Variation: In probability theory and statistics, the coefficient of variation (CV) [16] is a standardized measure of spreading of a probability distribution. It is defined as the ratio of the mean and standard deviation. It is also known as the variation coefficient. The absolute value of the CV is sometimes known as relative standard deviation (RSD), which is expressed as a percentage. The coefficient of variation (CV) is defined as the ratio of the standard deviation to the mean.

Quartile: In descriptive statistics, the quartiles [17] of a ranked set of data values are the three points that divide the data set into four equal groups, each group comprising a quarter of the data. A quartile is a type of quantile. The first quartile (Q_1) is defined as the middle number between the smallest number and the median of the data set. The second quartile (Q_2) is the median of the data. The third quartile (Q_3) is the middle value between the median and the highest value of the data set.

In applications of statistics, the quartiles of a ranked set of data values are the four subsets whose boundaries are the three quartile points. Thus, an individual item might be described as being "in the upper quartile".

- **First quartile** (Labelled as Q₁) also called the lower quartile or the 25th percentile. It splits off the lowest 25% of data from the highest 75%.
- Second quartile (Labelled as Q₂) also called the median or the 50th percentile. This is the cuts of the data set in half.
- **Third quartile** (Labelled as Q₃) also called the upper quartile or the 75th percentile. This is splits off the highest 25% of data from the lowest 75%.
- Interquartile range (Labelled as IQR) is the difference between the upper and lower quartiles. So, the IQR = Q₃ -Q₁.

Range: In arithmetic, the range [18] of a set of data is the difference between the largest and smallest values. However, in imaginative statistics, this concept of range has a more difficult meaning. The range is the size of the smallest interval which contains all the data and provides an indication of statistical distribution. It is measured in the same units as the data. Since it only depends on two of the observations, it is most useful in representing the dispersion of small data sets.

Mode: The mode [19] is the value that appears most often in a set of data. The mode of a discrete probability distribution is the value *x* at which its probability mass function takes its maximum value. In other words, it is the value that is most likely to be sampled. The mode of a continuous probability distribution is the value *x* at which its probability density function has its maximum value. So, informally speaking, the mode is at the peak.

Kurtosis: In probability theory and statistics, kurtosis [20] comes from the Greek word i.e. $\kappa\nu\rho\tau\delta\varsigma$, kyrtos or kurtos, meaning "curved, arching". It is calculating any measure of the "peakedness" of the probability distribution of a real-valued random variable. In a similar way to the concept of skewness, kurtosisis is a descriptor of the shape of a probability distribution. For the skewness, there are different ways of quantifying it for a theoretical distribution and corresponding ways of estimating it from a sample from a population.

MSSD: The mean of the squared successive differences (MSSD) [21] is used as an approximation of variance. It is calculated by taking the sum of the differences between consecutive observations aligned, then taking the mean of that sum and dividing by two.

Covariance: In probability theory and statistics, how much two random variables change together is measured by covariance [22]. If the greater values of one variable mainly correspond with the greater values of the other variable, the same holds for the smaller values, i.e., the variables tend to show similar behaviour, the covariance is positive. In the opposite case, when the greater values of one variable mainly correspond to the smaller values of the other, i.e., the variables tend to show opposite behaviour, the covariance is negative. The sign of the covariance therefore shows the tendency in the linear relationship between the variables. The magnitude of the covariance is not easy to interpret. The normalized version of the covariance, the correlation coefficient, however, it is shown by the magnitude and strength of the linear relation.

Kolmogorov Smirnov Test: The Kolmogorov–Smirnov test [23] or KS test is a non-parametric test of the equality of continuous, one-dimensional probability distributions. KS test can be used to compare one or two sample with a reference probability distribution. The Kolmogorov–Smirnov statistic measures a distance between the cumulative distribution function of the reference distribution and the empirical distribution function of any sample. The KS test can also quantify a distance between the empirical distribution functions of two samples. The null distribution of this statistic is calculated under the null hypothesis that the sample is drawn from the reference distribution or that the samples are drawn from the same distribution.

The empirical distribution function F_n for independent and identically distributed random variables observations X_i is defined in (1):

$$F_n(x) = \frac{1}{n} \sum_{i=1}^n I_{[-\infty, x]}(X_i)$$
 (1)

where $I_{[-\infty,x]}(X_i)$ is the indicator function, equal to 1 if $X_i \le x$ and equal to 0 otherwise.

The Kolmogorov–Smirnov statistic for a given cumulative distribution function F(x) is (2)

$$D_n = \sup_{x} |F_n(x) - F(x)| \tag{2}$$

where sup_x is the supremum of the set of distances. By the Glivenko-Cantelli theorem, if the sample comes from

distribution F(x), then D_n converges to 0 almost surely in the limit when n goes to infinity. Kolmogorov strengthened this result, by effectively providing the rate of this.

Quantitative Metrics

The science and technology investigate the quantitative research by observing the systematic experiential analysis of observable indications via statistical, mathematical and computational techniques [24]. The objective of quantitative metrics is to develop the mathematical models and theories related to exact value of the information. In this observation, the measurement is very accurate because the relationship between data and mathematical expression is quantitative. Quantitative information is any data which can be represented as the numerical form such as the value of the similarity matrices, embedding percentages, etc. We analyse the data with the help of some similarity metrics like MSE, PSNR, Correlations, RMSE, SSIM, KL divergence, Entropy.

Mean Square Error (MSE): It is computed by averaging the squared intensity of the cover and stego image pixels [25]. Equation (3) shows the MSE:

$$MSE = \frac{1}{NM} \sum_{m=0}^{M-1} \sum_{n=0}^{N-1} e(m,n)^{2}$$
 (3)

where NM is the image size $(N \times M)$ and e(m,n) is the reconstructed image.

Peak Signal-to-Noise Ratio (PSNR): A mathematical measure of image quality is signal-to-noise ratio (SNR) [25], which is based on the pixel difference between two images [26]. The SNR measure the estimate of Stego image and cover image. PSNR is shown in (4):

$$PSNR = 10\log_{10} \frac{S^2}{MSE}$$
 (4)

where, S stands for maximum possible pixel value of the image. If the PSNR is greater than 36 DB then the visibility looks same in between cover and stego image, so HVS not identified the changes.

Correlations: Pearson's correlation coefficient is widely used in statistical analysis as well as image processing [27]. Here this can be used to Cover and Stego images to find the difference between these two images. The correlation is shown in (5):

$$r = \frac{\sum_{i=1}^{n} (x_i - \overline{x}) \cdot (y_i - \overline{y})}{\sqrt{\sum_{i=1}^{n} (x_i - \overline{x})^2 \cdot \sum_{i=1}^{n} (y_i - \overline{y})^2}}$$
(5)

The X_i and Y_i are the cover image and bar of X and Y are stego image positions.

Root Mean Square Error (RMSE): RMSE [28] is a frequently used measure of the difference between Cover and Stego Image values. These individual differences are called

residuals and the RMSE aggregates them into a single measure of predictive power. The RMSE is shown in (6):

$$RMSE = \sqrt{\frac{\sum_{i=1}^{n} (X_{obs,i} - X_{model,i})^{2}}{n}}$$
(6)

 X_{obsi} and X_{modeli} are two image vectors i.e. cover and stego.

Structural Similarity Index (SSIM): Wang et. al [29] proposed Structural Similarity Index concept between original and distorted image [10]. The Stego and Cover images are divided into blocks of 8 x 8 and converted into vectors. Then two means, two standard derivations and one covariance value are computed. After that, the luminance, contrast and structure comparisons based on statistical values are computed. Then the SSIM is computed between Cover and Stego images. SSIM is shown in (7):

$$SSIM = \frac{\left(2\mu_x \mu_y + C_1\right) \left(2\sigma_{xy} + C_2\right)}{\left(\mu_x^2 + \mu_y^2 + C_1\right) \left(\mu_x^2 + \mu_y^2 + C_2\right)}$$
(7)

KL divergence: With the help of probability density function (PDF) for each Image (cover and stego) we estimate the Kullback-Leibler Divergence [30]. KL divergence is shown in (8):

$$D(p \parallel q) = \sum_{x} p(x) \log \frac{p(x)}{q(x)}$$
(8)

Entropy: Entropy is a measure of the uncertainty associated with a random variable [16]. Here, a 'message' means a specific realization of the random variable. It is shown in (9):

$$\Delta S = \int \frac{dQ_{rev}}{T} \tag{9}$$

where, S is the entropy and T is the uniform thermodynamic temperature of a closed system divided into an incremental reversible transfer of heat into that system (dQ).

Cross Entropy: The cross entropy [31] between two probability distributions over the image intensity measures the average number of element needed to identify an event drawn from the image matrix. The cross entropy for the distributions p and q over a given image is defined as:

$$H(p,q) = E_p[-\log q] = H(p) + D_{KL}(p||q)$$
 (10)

where H(p) is the entropy of p, and $D_{KL}(p||q)$ is the Kullback-Leibler divergence of q from p.

III. EXPERIMENTAL RESULTS

In this section, we deliberate the experimental results of the PFM method in spatial and frequency domain with the help of gray scale images, extended PMM method in spatial domain using also gray scale images. First thing is the capacity of

hiding data and another is the imperceptibility of the stego image, also called the quality of stego image. This capacity and the quality of image are discussed here with the help of quantitative as well as qualitative nature of similarity metrics. A comparative study with some existing methods like LSB, PVD and the methods proposed by the author are also discussed in this section. Experimental results of stego images are computed based on the images taken form the freely available image database in the internet and used by most of the researchers.

Qualitative Metrics

The qualitative approach has been discussed by means of the relative error of statistical parameters with respect to the covering values. Relative errors are plotted in a graph and the qualitative phases i.e. Best, Good, Moderate, etc. are categorized. The transition occurring in the graph helps in dividing to the phase. The quality of the steganography approach is depending upon the corresponding relative error phase. The relative error is in between 0 and 1. When, the relative error is near to 0, the performance is better. It has been observed that the Extended PMM and PFM methods are robust and secure, which have been tested by various statistical parameters. So, Extended PMM and PFM methods both of them work altogether than LSB, PVD mechanisms.

Mathematical Schemes:

. Estimate the relative error

$$e_{i,j} = \frac{|cover_i - X_{i,j}|}{cover_i} \tag{11}$$

where, i = 1,2,3,..., 17; j = 1,2,3. All these $e_{i,j} \in [0,1]$. Here i denotes the statistical parameters and j denotes the steganography methods. X is denoting the statistical parameter values of steganography methods.

- 2. Demolish the matrix to form a sequence $\{e_l\}_{l=1}^{51}$, where l=3(i-1)=j
- 3. Next sort these e_l in increasing order.
- 4. Plot the graph with the help of e_l and identify the phases ε_{Best} , ε_{Good} , $\varepsilon_{Moderate}$, $\varepsilon_{Not\ Acceptable}$. The phases are established in the graph by assuming the transition occurrence.

PFM Method: PFM method has been implemented in image spatial and frequency domain. The qualitative approach is described with the help of spatial domain technique.

Table II illustrates the relative error, where i is the statistical parameters and j is the steganography methods. In (11), the X is denoting the statistical parameter values of LSB, PVD and PFM. Fig. 3 shows the graph by assuming the transition occurrence.

The phases are identified by the help of mathematical function (11). If the relative error $e_{i,j}$ is less than or equal to ε_{Best} then it is considered as 'Best'. While if $e_{i,j}$ is greater than or equal to ε_{Good} and less than ε_{Best} , it is considered as 'Good'. If $e_{i,j}$ is greater than or equal to $\varepsilon_{Moderate}$ and less than ε_{Good} then it is considered as 'Moderate'. When $e_{i,j}$ is greater than or equal to $\varepsilon_{Not\ Acceptable}$ then it is considered as

'Not acceptable'. Table III describes the relative values of statistical parameters for PFM, LSB & PVD.

 $\label{eq:table ii} \textbf{TABLE II}$ Relative Error $e_{i,j}$ of statistical parameters for LSB, PVD & PFM

	STATISTICAL PARAMETERS	LSB	PVD	PFM
	Mean	0.5943	0.5943	0.0001
	Standard Error Mean	0.2826	0.2826	0.0014
	Trimmed Mean	0.5950	0.5950	0.0001
	Standard Deviation	0.2816	0.2816	0.0012
	Variance	0.6424	0.6422	0.0023
<i>j</i> ↓	Coefficient of Variation	0.1963	0.1963	0.0000
$i \rightarrow$	Sum	0.5943	0.5943	0.0001
• /	First quartile (Q1)	0.7451	0.7451	0.0000
where	Median (Q2)	0.5926	0.5926	0.0000
i =	Third quartile (Q ₃)	0.5096	0.5096	0.0000
$1, 2, \dots, 17$ i = 1, 2, 3	Range	0.3631	0.3095	0.0238
J = 1, 2, 3	Interquartile (IQR)	0.2830	0.2830	0.0000
	Mode	0.5347	0.5347	0.0099
	N for Mode	0.2111	0.2090	0.0852
	Kurtosis	0.0000	0.0000	0.0119
	MSSD	0.6413	0.6385	0.0623
	Covariance	0.2814	0.2814	0.0002

Relative Error

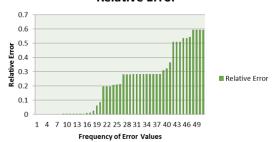


Fig. 3 Relative error graph for LSB, PVD & PFM

TABLE III
RELATIVE VALUES OF STATISTICAL PARAMETERS FOR PFM, LSB & PVD

STATISTICAL PARAMETERS	PFM	LSB	PVD
Mean	Best	Moderate	Moderate
Standard Error Mean	Best	Good	Good
Trimmed Mean	Best	Moderate	Moderate
Standard Deviation	Best	Good	Good
Variance	Best	Moderate	Moderate
Coefficient of Variation	Best	Best	Best
Sum	Best	Moderate	Moderate
First quartile (Q_1)	Best	Moderate	Moderate
$Median(Q_2)$	Best	Moderate	Moderate
Third quartile (Q_3)	Best	Moderate	Moderate
Range	Best	Moderate	Moderate
Interquartile (IQR)	Best	Good	Good
Mode	Best	Moderate	Moderate
N for Mode	Best	Good	Good
Kurtosis	Best	Best	Best
MSSD	Best	Moderate	Moderate
Covariance	Best	Good	Good

<u>Kolmogorov Smirnov Test:</u> By this hypothesis test, it can be observed that the performance of both PFM and the LSB are

better by the help of the relative error of their Rank and Test parameter value for Burr, Log-Gamma, Lognormal, Beta, Gamma, Cauchy and Normal distribution. Also, it has been noted that performance of both PVD and PFM are same for Burr, Gamma, Cauchy and Normal distribution. The table of relative test results is furnished in Table IV. Hence, it can be proven that the PFM is robust and secure like LSB, PVD and the PFM is also acceptable for the hiding concept.

 $\label{total} TABLE~IV\\ Relative~Values~of~Hypothesis~Test~Result~for~PFM,~LSB~\&~PVD$

Kolmogorov Smirnov Test:							
Distribution	PFM	LSB	PVD				
Burr	Good	Good	Good				
Log-Gamma	Moderate	Moderate	Best				
Lognormal	Moderate	Moderate	Best				
Beta	Moderate	Moderate	Best				
Gamma	Good	Good	Good				
Cauchy	Good	Good	Good				
Normal	Good	Good	Good				

 $\label{eq:table_v} \textbf{TABLE V}$ Relative Error $e_{i,j}$ of Statistical Parameters for LSB, PVD & PFM

RELATIVE ERROR $e_{i,j}$ OF STATISTICAL PARAMETERS FOR LSD, F V D & FFIVE							
	STATISTICAL PARAMETERS	LSB	PVD	Ex PMM			
	Mean	0.5943	0.5943	0.5928			
	Standard Error Mean	0.2826	0.2826	0.2826			
	Trimmed Mean	0.5950	0.5950	0.5936			
	Standard Deviation	0.2816	0.2816	0.2816			
j↓	Variance	0.6424	0.6422	0.6422			
$i \rightarrow$	Coefficient of Variation	0.1963	0.1963	0.1956			
•	Sum	0.5943	0.5943	0.5929			
where Firs	First quartile (Q1)	0.7451	0.7451	0.7451			
i =	Median (Q2)	0.5926	0.5926	0.5926			
1, 2, . , 17	Third quartile (Q ₃)	0.5096	0.5096	0.5096			
j = 1, 2	Range	0.3631	0.3095	0.3214			
, 3	Interquartile (IQR)	0.2830	0.2830	0.2830			
	Mode	0.5347	0.5347	0.5446			
	N for Mode	0.2111	0.2090	0.2062			
	Kurtosis	0.0000	0.0000	0.0000			
	MSSD	0.6413	0.6385	0.6533			
	Covariance	0.2814	0.2814	0.2810			

Relative Error

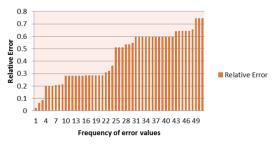


Fig. 4 Relative error graph for LSB, PVD & Extended PMM

Extended PMM Method: This method has been implemented in image spatial domain. The qualitative approach is described with the help of relative error.

Table V illustrates the relative error, where i denotes the statistical parameters and j denotes the steganography methods. In (11), X denote the statistical parameter values of LSB, PVD and Extended PMM. Fig. 4 shows the graph by assuming the occurrence of qualitative transitions.

The phases are identified by the help of mathematical function in (11). If $e_{i,j}$ is less than or equal to ε_{Best} then it is considered as 'Best'. If $e_{i,j}$ is greater than or equal to ε_{Good} and less than ε_{Best} , it is considered as 'Good'. If the $e_{i,j}$ is greater than or equal to $\varepsilon_{Moderate}$ and less than ε_{Good} then it is considered as 'Moderate'. When $e_{i,j}$ is greater than or equal to $\varepsilon_{Not\ Acceptable}$ then it considered as 'Not acceptable'. Table VI describes the relative values of statistical parameters for Extended PMM, LSB & PVD.

TABLE VI
RELATIVE VALUES OF STATISTICAL PARAMETERS FOR LSB, PVD & EX PMM

STATISTICAL PARAMETERS	LSB	PVD	Ex PMM
Mean	Good	Good	Good
Standard Error Mean	Good	Good	Good
Trimmed Mean	Good	Good	Good
Standard Deviation	Good	Good	Good
Variance	Moderate	Moderate	Moderate
Coefficient of Variation	Best	Best	Best
Sum	Good	Good	Good
First quartile (Q_1)	Moderate	Moderate	Moderate
$Median(Q_2)$	Good	Good	Good
Third quartile (Q_3)	Good	Good	Good
Range	Good	Good	Good
Interquartile (IQR)	Good	Good	Good
Mode	Good	Good	Good
N for Mode	Good	Good	Good
Kurtosis	Best	Best	Best
MSSD	Moderate	Moderate	Moderate
Covariance	Good	Good	Good

TABLE VII RELATIVE VALUES OF HYPOTHESIS TEST RESULT FOR EX PMM, LSB & PVD

Kolmogorov Smirnov Test:							
Distribution	LSB	PVD	Ex PMM				
Burr	Good	Good	Best				
Log-Gamma	Moderate	Best	Best				
Lognormal	Moderate	Best	Best				
Beta	Moderate	Best	Best				
Gamma	Good	Good	Best				
Cauchy	Good	Good	Best				
Normal	Good	Good	Best				

<u>Kolmogorov Smirnov Test:</u> In this hypothesis test, it has been observed that the Extended PMM performs better than the LSB and PVD by means of relative error of their Rank and Test parameter value for Burr, Log-Gamma, Lognormal, Beta, Gamma, Cauchy and Normal distribution. The tabular form of relative test results is furnished in Table VII. Hence, from that point of view, it can be proved that the Extended PMM is robust and secure than LSB, PVD and the PFM is also acceptable for the hiding concept.

Quantitative Metrics

In qualitative approach, the methods have been tested through some techniques and the assessment is marked. But in the quantitative approach, the metrics are proving the robustness of methods with the help of quantitative values. The comparison with other methods through quantitative metrics are also substantiate that the developed techniques are superior to others methods.

Experimental Results of PFM Method: This section describes the results and analysis of PFM method through the quantitative nature. This method has been developed in spatial as well as frequency domain. Both are described below separately.

Spatial Domain: The similarity metrics of spatial domain technique with gray scale images are described in Tables VIII-XI

Frequency Domain: The similarity metrics of frequency domain technique with gray scale images are described in Tables XII-XV.

TABLE VIII

MSE AND PSNR OF PEM I SR & PVD

MSE AND PSNR OF PFM, LSB & PVD								
		MSE			PSNR			
Message Length	PFM	LSB	PVD	PFM	LSB	PVD		
500	0.0285	0.018	0.0138	58.588	65.584	66.717		
1000	0.0559	0.0375	0.0277	56.66	62.392	63.712		
2000	0.1098	0.0707	0.0551	54.724	59.636	60.722		
5000	0.2714	0.1737	0.1391	53.794	55.732	56.699		
10000	0.4379	0.3401	0.2917	52.012	52.815	53.482		
15000	0.6206	0.514	0.474	50.989	51.021	51.373		
20000	0.8101	0.6844	0.6633	49.712	49.778	49.914		
30000	1.0962	1.0388	1.1542	46.048	47.965	47.508		

TABLE XI

CORRELATION AND RIVISE OF PFINI, LSB & PVD								
	Correlations							
Message Length	PFM	LSB	PVD	PFM	LSB	PVD		
500	1	1	0.999997	0.033	0.097	0.096		
1000	0.99999	0.99999	0.999994	0.046	0.13	0.135		
2000	0.99998	0.99998	0.999988	0.125	0.188	0.19		
5000	0.99997	0.99996	0.99997	0.297	0.29	0.298		
10000	0.99991	0.99993	0.999937	0.526	0.392	0.433		
15000	0.99987	0.99989	0.999897	0.727	0.487	0.546		
20000	0.99977	0.99985	0.999856	0.871	0.564	0.644		
30000	0.99964	0.99977	0.999751	0.967	0.691	0.838		

TABLE X

SSIM AND CROSS ENTROPY OF PFM, LSB & PVD								
		SSIM		Cross Entropy				
Message Length	PFM	LSB	PVD	PFM	LSB	PVD		
500	1	1	1	4.35E+01	17.52882	13.55991		
1000	1	1	1	85.01501	43.0382	27.3302		
2000	1	1	1	166.9952	126.4012	55.85684		
5000	1	1	0.999	425.8677	281.8571	147.6679		
10000	0.999	1	0.999	884.1487	582.9952	331.6544		
15000	0.997	1	0.998	1403.106	855.6058	554.9409		
20000	0.997	1	0.998	2572.633	1111.579	753.9296		
30000	0.996	0.999	0.997	3630.424	1594.039	1453.505		

TABLE XI
ENTROPY AND KL DIVERGENCE OF PFM, LSB & PVD

,								
	Entropy			KL Divergence				
Message Length	PFM	LSB	PVD	PFM	LSB	PVD		
500	7.4405	7.4451	7.445	7.18E-07	5.41E-07	4.17E-07		
1000	7.4409	7.4452	7.4451	1.40E-06	1.32E-06	8.41E-07		
2000	7.4415	7.4455	7.4452	2.75E-06	3.95E-06	1.72E-06		
5000	7.4419	7.4458	7.4453	6.98E-06	8.76E-06	4.53E-06		
10000	7.4424	7.4461	7.4457	1.44E-05	1.81E-05	1.02E-05		
15000	7.4438	7.4465	7.4458	2.26E-05	2.65E-05	1.70E-05		
20000	7.4457	7.4467	7.4462	3.17E-05	3.44E-05	2.30E-05		
30000	7.4469	7.4474	7.447	4.83E-05	4.92E-05	4.44E-05		

TABLE XII
MSE AND PSNR OF PFM, LSB & PVD

Message		MSE			PSNR	
Length	PFM	LSB	PVD	PFM	LSB	PVD
100	0.188564	0.017975	0.013847	55.37621	65.58415	66.71714
200	0.370255	0.037483	0.027664	52.4458	62.39244	63.71162
500	0.993813	0.070717	0.055069	48.15776	59.63557	60.72173
1000	2.106766	0.173714	0.139065	44.89464	55.73246	56.69863
2000	4.327614	0.340054	0.291687	41.76832	52.81533	53.48163
3000	6.621696	0.514008	0.47398	39.92111	51.02111	51.3732
4000	8.925777	0.684372	0.663311	38.62434	49.77788	49.91363
5000	11.20823	1.038841	1.154232	37.63543	47.96531	47.50787

TABLE XIII
CORRELATION AND RMSE OF PFM, LSB & PVD

Message	(Correlations	S		RMSE	
Length	PFM	LSB	PVD	PFM	LSB	PVD
100	0.999954	0.999996	0.999997	0.246063	0.097284	0.096339
200	0.999909	0.999992	0.999994	0.341054	0.129864	0.135359
500	0.999756	0.999985	0.999988	0.540367	0.188201	0.189765
1000	0.999483	0.999962	0.99997	0.76879	0.289952	0.297812
2000	0.998939	0.999926	0.999937	1.094649	0.391805	0.432775
3000	0.998379	0.999888	0.999897	1.346844	0.486556	0.546174
4000	0.997817	0.999851	0.999856	1.55667	0.563909	0.643951
5000	0.997262	0.999773	0.999751	1.743785	0.691398	0.838396

TABLE XIV SSIM AND CROSS ENTROPY OF PFM, LSB & PVD

	SSIIVI A	SSIM AND CROSS ENTROPY OF PFM, LSB & PVD						
Message		SSIM		Cross Entropy				
Length	PFM	LSB	PVD	PFM	LSB	PVD		
100	1	1	0.999999	3.00E-06	17.52882	13.55991		
200	1	1	0.999985	5.96E-06	43.0382	27.3302		
500	1	1	0.999858	1.65E-05	126.4012	55.85684		
1000	1	0.999999	0.999453	3.53E-05	281.8571	147.6679		
2000	0.999998	0.999988	0.998927	7.35E-05	582.9952	331.6544		
3000	0.999992	0.999928	0.998459	0.000112	855.6058	554.9409		
4000	0.999985	0.999778	0.998056	0.000151	1111.579	753.9296		
5000	0.999976	0.999086	0.997261	0.000188	1594.039	1453.505		

Experimental Results of PMM Method: This section describes the results and analysis of Extended PMM through the quantitative nature. This is a spatial domain technique using gray scale images. Tables XVI-XIX show the quantitative metrics value.

TABLE XV
ENTROPY AND KL DIVERGENCE OF PFM, LSB & PVD

Message	Entropy			KL Divergence		
Length	PFM	LSB	PVD	PFM	LSB	PVD
100	6.677885	7.44512	7.445017	32096	5.41E-07	4.17E-07
200	6.677695	7.445197	7.445057	32096	1.32E-06	8.41E-07
500	6.678876	7.445477	7.445153	3.21E+04	3.95E-06	1.72E-06
1000	6.681039	7.445803	7.445341	3.21E+04	8.76E-06	4.53E-06
2000	6.68535	7.446146	7.445717	3.21E+04	1.81E-05	1.02E-05
3000	6.689584	7.446484	7.445837	32096	2.65E-05	1.70E-05
4000	6.693826	7.446715	7.44616	32096	3.44E-05	2.30E-05
5000	6.699424	7.447361	7.44702	3.21E+04	4.92E-05	4.44E-05

TABLE XVI MSE AND PSNR OF EXTENDED PMM, LSB & PVD

Message		MSE			PSNR	
Length	Extended	LSB	PVD	Extended	LSB	PVD
	PMM			PMM		
500	0.019165	0.017975	0.013847	65.30571	65.58415	66.71714
1000	0.038563	0.037483	0.027664	62.26912	62.39244	63.71162
2000	0.076477	0.070717	0.055069	59.29549	59.63557	60.72173
5000	0.188751	0.173714	0.139065	55.37191	55.73246	56.69863
10000	0.381187	0.340054	0.291687	52.31942	52.81533	53.48163
15000	0.568932	0.514008	0.47398	50.5802	51.02111	51.3732
20000	0.684212	0.684372	0.663311	49.7789	49.77788	49.91363

TABLE XVII
CORRELATION AND RMSE OF EXTENDED PMM, LSB & PVD

	Correlations				RMSE		
Message Length	Extended PMM	LSB	PVD	Extended PMM	LSB	PVD	
500	0.999993	0.999996	0.999997	0.10298	0.097284	0.096339	
1000	0.999986	0.999992	0.999994	0.145491	0.129864	0.135359	
2000	0.999973	0.999985	0.999988	0.206792	0.188201	0.189765	
5000	0.999932	0.999962	0.99997	0.323471	0.289952	0.297812	
10000	0.999863	0.999926	0.999937	0.45846	0.391805	0.432775	
15000	0.999796	0.999888	0.999897	0.560833	0.486556	0.546174	
20000	0.999755	0.999851	0.999856	0.61435	0.563909	0.643951	

TABLE XVIII SSIM AND CROSS ENTROPY OF EXTENDED PMM, LSB & PVD

	SSIM			Cross Entropy		
Message	Extended	LSB	PVD	Extended	LSB	PVD
Length	PMM			PMM		
500	0.999989	1	0.999999	64.49798	17.52882	13.55991
1000	0.999953	1	0.999985	111.3092	43.0382	27.3302
2000	0.999874	1	0.999858	171.3853	126.4012	55.85684
5000	0.999619	0.999999	0.999453	415.9149	281.8571	147.6679
10000	0.999318	0.999988	0.998927	2762.02	582.9952	331.6544
15000	0.998958	0.999928	0.998459	4956.63	855.6058	554.9409
20000	0.998702	0.999778	0.998056	5243.456	1111.579	753.9296

$\label{thm:table XIX} \textbf{Entropy and KL Divergence of Extended PMM, LSB \& PVD}$

Entropy			KL Divergence			
Message Length	Extended PMM	LSB	PVD	Extended PMM	LSB	PVD
500	7.088114	7.44512	7.445017	3.19E-06	5.41E-07	4.17E-07
1000	7.088101	7.445197	7.445057	5.49E-06	1.32E-06	8.41E-07
2000	7.08801	7.445477	7.445153	8.43E-06	3.95E-06	1.72E-06
5000	7.087567	7.445803	7.445341	2.04E-05	8.76E-06	4.53E-06
10000	7.087073	7.446146	7.445717	NA	1.81E-05	1.02E-05
15000	7.086213	7.446484	7.445837	NA	2.65E-05	1.70E-05
20000	7.085546	7.446715	7.44616	NA	3.44E-05	2.30E-05

IV. CONCLUSION

In this article, we investigated the performance of the PFM and Extended PMM method in various domains using various image similarity measure metrics. The approach of quantitative and qualitative similarity metrics is furnished in this method. A comparative study also has been shown with some other existing methods like LSB & PVD. From the experimental results, it can be seen that the embedding capacity of the presented methods are much better compared to existing methods. With the computation of various images, quantitative and qualitative similarity metrics have been shown through some figures for measuring the similarity between the cover image as well as stego image and these methods give a good result.

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