

# Semi-Automatic Artifact Rejection Procedure based on Kurtosis, Renyi's Entropy and Independent Component Scalp Maps

Antonino Greco, Nadia Mammone, Francesco Carlo Morabito, and Mario Versaci

**Abstract**—Artifact rejection plays a key role in many signal processing applications. The artifacts are disturbance that can occur during the signal acquisition and that can alter the analysis of the signals themselves. Our aim is to automatically remove the artifacts, in particular from the Electroencephalographic (EEG) recordings. A technique for the automatic artifact rejection, based on the Independent Component Analysis (ICA) for the artifact extraction and on some high order statistics such as kurtosis and Shannon's entropy, was proposed some years ago in literature. In this paper we try to enhance this technique proposing a new method based on the Renyi's entropy. The performance of our method was tested and compared to the performance of the method in literature and the former proved to outperform the latter.

**Keywords**—Artifact, EEG, Renyi's entropy, kurtosis, Independent Component Analysis.

## I. INTRODUCTION

ARTIFACT rejection is a key topic in many signal processing applications, particularly in biomedical applications. When an artifact occurs during a signal recording, it generates some unwelcome signals that can be superimposed to the signals that we want to analyse, therefore it can undermine the results of the analysis. In this paper we focus on the artifact rejection from brain activity registrations, in particular we focus on the artifact rejection from Electroencephalography (EEG). EEG is a technique for monitoring the electrical activity of the brain: the brain cells communicate by producing tiny electrical impulses and, by means of some electrodes placed on the scalp over multiple areas of the brain, we can detect and record patterns of electrical activity. Some flat metal discs (electrodes) are applied in different positions on the scalp, these discs are held in places with a sticky paste, the electrodes are connected by wires to an amplifier and a recording machine.

EEG is used to help to diagnose the presence and type of seizure disorders, to look for causes of confusion, and to evaluate head injuries, tumors, infections, degenerative diseases and metabolic disturbances that affect the brain. The occurrence of the artifacts can alter the analysis or completely obscure the EEG waves. Artifacts are disturbances caused by eye movement, eye blink, electrode movement, muscle activity, movements of the head, sweating, breathing, earth

beat, electrical line noise.

For these reason, many efforts have been devoted to artifact cancellation, in general two approaches have been adopted so far: the cancellation of the entire data segment affected by artifacts (in the following named *artifact-laden trials*), which implies throwing away both useful and artifactual information or, when we cannot afford to lose any information from the recorded data, the second approach consists in isolating the artifactual signals and then in cancelling them. In this paper we focus on the second approach.

It is well accepted that an artifact is independent from the rest of the signals, this is clear when the artifact is "external" (electrical line noise), it is also well accepted if it is "internal" (muscle activity, eye blink, etc.) because even though the triggering event starts from a brain area (for example the motor cortex) the time course of the artifact carries no information about the triggering event signal. The spectrum of the signals related to muscle activity contains high frequencies (>50 Hz) and it can spread from low frequencies to high frequencies; therefore, it can be overlapped to the spectrum of the brain waves, which goes from 0.5 up to 35 Hz, sometimes up to 50 Hz, we can weaken the high frequencies by a lowpass filtering.

Since it is accepted that the artifactual signals are independent from the rest, it is also well accepted that the artifactual signals can be extracted by Independent Component Analysis (ICA). ICA has been widely exploited as a tool for artifactual signals extraction, since it was proposed by Cichocki et al. [1] and Jung et al. [2]. The artifactual signal is isolated by ICA as a component independent from the rest.

In order to make the artifacts rejection procedure to be automatic we need some markers capable to measure how much an independent component (IC) is likely to be an artifactual signal, Delorme et al. [3] proposed the joint use of kurtosis and entropy as markers, while Vorobyov et al. [4] proposed the Hurst exponent. Delorme et al. [3] proposed the joint use of kurtosis and entropy, in particular the Shannon's entropy, for the detection of the artifactual signals (once they have been isolated by means of ICA). This method had shown to be promising and, since we were interested in automatic artifact rejection, we decided to adopt and test it. The test showed some failures of the procedure in detecting some artifactual signals, thus we guessed whether another entropy definition could improve the performance of the method. This paper proposes a method based on the joint use of kurtosis and Renyi's entropy, instead of Shannon's entropy.

The paper is organized as follows: Section II describes the application of ICA to the EEG data and the Extended

Author are with DIMET – University Mediterranea of Reggio Calabria, Via Graziella Loc. Feo di Vito Reggio Calabria, Italy (e-mails: nadia.mammone@ing.unirc.it, ngreco@ing.unirc.it, versaci@ing.unirc.it, morabito@unirc.it).

INFOMAX algorithm, Section III introduces the parameters for automatic detection and Section IV presents the results.

## II. INDEPENDENT COMPONENT ANALYSIS

### A. ICA and EEG data

Independent component analysis was originally developed to deal with problems that are closely related to the cocktail-party problem. Since many real observations can be assumed to be a mixing of “sources”, ICA was exploited for a lot of applications, for example for EEG data. The EEG data are presumably generated by mixing some underlying brain activity related signals and artifacts. This situation is quite similar to the cocktail-party problem: we would like to find the original components of the brain activity, but we can only observe mixtures of the components.

It is worth to wonder whether there are independent sources in the EEG data or not, we told above that it is a shared opinion that at least the artifacts are accounted by components independent from the rest of the signals. The second assumption for standard ICA is that each channel collects a linear combination of the sources, this assumption is well accepted for the EEG sensors, because the different electrical sources (brain activations, muscle activations) are supposed to sum linearly at the scalp electrodes.

### B. The Extended-INFOMAX algorithm

Given an input data vector  $\mathbf{x}$ , we consider it generated as a mixture of  $n$  statistically independent sources  $(s_1, \dots, s_n)$ :

$$\mathbf{x} = \mathbf{f}(\mathbf{s}) \quad (1)$$

If  $\mathbf{f}$  is a linear function, we deal with the *linear* ICA problem:

$$\mathbf{x} = \mathbf{A}\mathbf{s} \quad (2)$$

ICA is a tool for multivariate data analysis which yields  $(y_1, \dots, y_n)$  components as independent as possible so that  $\mathbf{y} = \mathbf{W}\mathbf{x}$ , and  $\mathbf{W}$  is close to  $\mathbf{A}^{-1}$ .

Here we focus on the Bell-Sejnowski *INFOMAX* algorithm [5]. The input of the network is the observed data  $\mathbf{x}$ , the output is  $\mathbf{y}$ , whose elements are the estimated independent components  $(y_1, \dots, y_n)$ .

The *marginal entropy* of each estimated component is defined as follows:

$$H(y_i) = -E\{\log p(y_i)\} \quad (3)$$

The *joint entropy* has the following expression:

$$H(\mathbf{y}) = -E\{\log p(\mathbf{y})\} = -\int_{-\infty}^{\infty} \dots \int_{-\infty}^{\infty} p(\mathbf{y}) \log p(\mathbf{y}) d\mathbf{y} \quad (4)$$

The *mutual information* is defined as:

$$I(\mathbf{y}) = \int p(\mathbf{y}) \log \frac{p(\mathbf{y})}{\prod_{i=1}^N p_i(y_i)} d\mathbf{y} \quad (5)$$

The relationship between marginal entropy, joint entropy and mutual information is:

$$H(\mathbf{y}) = H(y_1) + \dots + H(y_N) - I(y_1, \dots, y_N) \quad (6)$$

Therefore the components of  $\mathbf{y}$  are as independent as possible when their mutual information is minimum. The marginal entropies are constant when  $(y_1, \dots, y_n)$  have uniform distribution and are amplitude bounded random variables, so while minimizing mutual information we maximize joint entropy. Maximizing joint entropy leads to the INFOMAX learning rule [5]:

$$\Delta \mathbf{W} \propto [\mathbf{I} - \phi(\mathbf{y})\mathbf{y}^T] \mathbf{W} \quad (7)$$

Where

$$\phi(\mathbf{y}) = -\frac{\frac{\partial p(\mathbf{y})}{\partial \mathbf{y}}}{p(\mathbf{y})} \quad (8)$$

is called *score function* and  $p$  is the joint probability density function of  $\mathbf{y}$ .

INFOMAX has the limitation to assume that the sources have super-gaussian distributions and at most one source is normally distributed, therefore, Extended-INFOMAX was introduced to separate sources with a variety of distributions. Since Renyi's entropy, as we will describe in Section III, depends on sources distribution, we needed to know whether a source was sub-gaussian or super-gaussian, therefore we used the extended version of INFOMAX. A way of generalizing the learning rule is to consider an approximation of the estimated pdf of the sub-gaussian and the super-gaussian sources, this leads to extended learning rule is [5]:

$$\Delta \mathbf{W} \propto [\mathbf{I} - \mathbf{K} \tanh(\mathbf{y})\mathbf{y}^T - \mathbf{y}\mathbf{y}^T] \mathbf{W} \quad (9)$$

There are two different learning rules for sub-gaussian and super-gaussian sources, the switching criterion between the two rules is given by  $\mathbf{K}$ : it is a N-dimensional diagonal matrix whose elements are:

$$k_{ii} = \begin{cases} 1 & \text{when } y_i \text{ is super-gaussian} \\ -1 & \text{when } y_i \text{ is sub-gaussian} \end{cases}$$

these elements are estimated as part of the algorithm. Extended-INFOMAX yields the independent components and the unmixing matrix  $\mathbf{W}$ , to reconstruct the observed signals we compute:

$$\tilde{\mathbf{x}} = \mathbf{W}^{-1}\mathbf{y} \quad (10)$$

in order to reconstruct the cleaned signals, we have to suppress the alleged artifactual components and to compute the (10).

### III. AUTOMATIC ARTIFACT DETECTION

Artifacts are outlier data, in other words transient and unexpected events, therefore we need some markers to measure this oddness to detect outlier trials or outlier independent components (ICs) once we have extracted them by ICA. The markers proposed by Delorme et al. [3] are kurtosis and entropy, which are both related to the distribution of the signals.

#### A. Kurtosis as a Marker for Artifacts

In some trials the distribution of the components is very peaky, for instance during a transient strong muscle activity, so the kurtosis can help us to detect these artifacts. Given a scalar random variable  $x$ , kurtosis has the following expression:

$$k = m_4 - 3m_2^2 \quad (11)$$

$$m_n = E\{(x - m_1)^n\} \quad (12)$$

where  $m_n$  is the  $n$ -order central moment of the variable and  $m_1$  is the mean. Kurtosis is positive for “peaked” activity distributions, typical of eye blink and cardiac artifacts; kurtosis is negative for “flat” activity distributions, typical of noise [3].

In order to detect artifactual components, kurtosis was computed for each trial and for all the ICs and it was normalized, to 0-mean and standard deviation 1, with respect to all the ICs, the threshold was set at  $\pm 1.64$  [6], if a component exceeded the threshold in more than 20% of the trials, the component was marked for rejection because it was very likely to be an artifact.

Kurtosis can also be exploited to detect the components which were very likely to account for gaussian noise: we estimated the kurtosis of the pdf of each component (global kurtosis), the IC with the minimum positive coefficient was marked as gaussian noise.

#### B. Entropy as a Marker for Artifacts

As a second marker we used the differential entropy:

$$H(x) = -\int p_x(\xi) \log(p_x(\xi)) d\xi \quad (13)$$

The entropy can be interpreted as a measure of randomness: if the random variable is concentrated on small temporal intervals, its differential entropy is small, indeed the variables whose probability densities take large values give a strong contribution to the integral in the (13), so their entropy is small. This feature of the entropy helps us to identify the signals which are concentrated in small temporal intervals with high probabilities and, therefore, which are very likely to be artifacts.

An approximation of the (13) was used:

$$H^i(j) = -\sum_{x \in j} f_j^i(x) \log(f_j^i(x)) \quad (14)$$

which is the entropy of the  $IC_i$  in the trial  $j$ , and  $f_j^i(x)$  is the pdf of the component  $IC_i$  during trial  $j$ .

In order to detect the artifactual components, entropy was computed for each trial and for all the ICs and it was normalized, to 0-mean and standard deviation 1, with respect to all the ICs, the threshold was set at  $\pm 1.64$  [6], if a component exceeded the threshold in more than 20% of the trials, the component was marked for rejection because it was very likely to be an artifact.

We want to compare the performances of the Shannon's entropy (14) and the Renyi's entropy. Renyi's entropy depends on a parameter  $\alpha$  and, for a random variable  $y$  with a pdf  $f_y(y)$ , it is defined as:

$$H_{R_\alpha}(y) = \frac{1}{1-\alpha} \log \int_{-\infty}^{+\infty} f_y(y) dy = \frac{1}{1-\alpha} \log E\{f^{\alpha-1}(y)\} \quad (15)$$

The Parzen window pdf estimate of a random variable  $y$  for which only the samples  $\{y_1, \dots, y_N\}$  are given, is defined by:

$$\hat{f}(y) = \frac{1}{N} \sum_{i=1}^N k_\sigma(y - y_i) \quad (16)$$

where  $i = 1 \dots N$  and  $k_\sigma$  is the gaussian kernel, whose size is specified by  $\sigma$  (we chose  $\sigma = 0.25$ ).

When we substitute the real pdf with the approximation (16) in the (15) we have:

$$H_{R_\alpha}(y) = \frac{1}{1-\alpha} \log \left[ \frac{1}{N^\alpha} \sum_j \left( \sum_i k_\sigma(y - y_i) \right)^{\alpha-1} \right] \quad (17)$$

The pdf's were estimated by the Parzen windowing method in both the Shannon's entropy and the Renyi's entropy computation.

All the properties stated in Section III.B are for both Shannon's entropy and Renyi's entropy and therefore they help us to identify the signals which are concentrated in small temporal intervals with high probabilities, for both artifact-laden trials and artifactual components. The automatic detection procedure, described in the Section III.B, was used for Renyi's entropy and each trial coincides with a Parzen window. We tested the automatic detection of the artifactual components for  $\alpha = 2$  in order to study the behaviour of the Renyi's entropy because we know that, for super-Gaussian sources, entropy orders  $\geq 2$  should be preferred, whereas for sub-Gaussian sources, entropy orders smaller than 2, perhaps closer to 1 or even smaller than 1, should be preferred [7].

Entropy orders larger than 2 emphasize samples in

## IV. RESULTS

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kurtosis and Renyi's entropy. The artifacts have been suppressed.

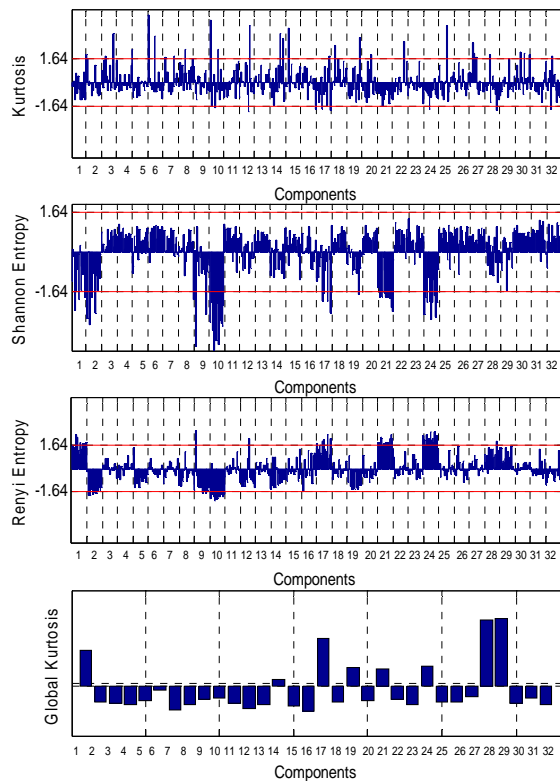


Fig. 4 The automatic artifact detection. Kurtosis detected IC10, which accounts for eye blink artifact. Shannon's entropy detected IC2, IC10, IC17, IC21, IC24. Renyi's entropy detected IC1, IC2, IC9, IC10, IC17, IC21, IC24. Global kurtosis detected IC14

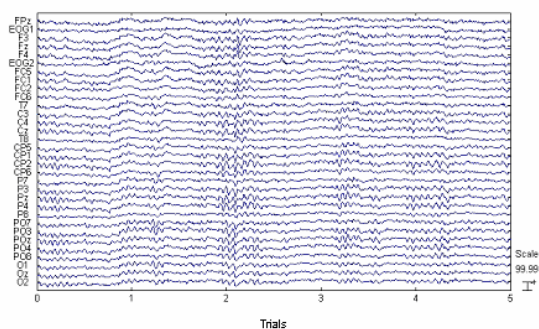


Fig. 5 The reconstructed EEG data. The ICs marked according to kurtosis and Renyi were suppressed and the data reconstructed by the Eq (10). Trial 3 appears free from the artifacts

## V. CONCLUSIONS

Artifact rejection is a key topic in biomedical signal processing and in literature, Independent Component Analysis (ICA) has shown to be a suitable tool for extracting the artifactual signals and some higher order statistics, kurtosis together with Shannon's entropy, have been used as markers for the automatic artifact detection. In this paper we have proposed the joint use of kurtosis and Renyi's entropy, instead of Shannon's entropy, and we have tested the reliability of the procedure comparing its results with the results of the visual inspection of the shape of the independent components and of the component scalp maps. The joint use of kurtosis and Renyi's entropy showed to outperform the joint use of kurtosis and Shannon's entropy. Future efforts will be devoted to enhance the reliability of the procedure focusing on artifactual signal extraction.

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