

Modeling and Validation of Microspheres Generation in the Modified T-Junction Device

Lei Lei, Hongbo Zhang, Donald J. Bergstrom, Bing Zhang, K. Y. Song, W. J. Zhang

Abstract—This paper presents a model for a modified T-junction device for microspheres generation. The numerical model is developed using a commercial software package: COMSOL Multiphysics. In order to test the accuracy of the numerical model, multiple variables, such as the flow rate of cross-flow, fluid properties, structure, and geometry of the microdevice are applied. The results from the model are compared with the experimental results in the diameter of the microsphere generated. The comparison shows a good agreement. Therefore the model is useful in further optimization of the device and feedback control of microsphere generation if any.

Keywords—CFD modeling, validation, microsphere generation, modified T-junction.

I. INTRODUCTION

MICROSPHERES have many important applications: drug delivery system (DDS), cosmetics, food, and other industrial uses. For the recent decades, microsphere produced with microfluidic technology has gathered a tremendous attention, such as T-junction [1]-[10], membrane emulsification [11]-[13], and flow focusing [14], [15]. In the original T-junction approach, the size of middle flow is determined by the size of the microchannel, and this means that the size of microspheres could only be adjusted in a very small range. To overcome this disadvantage, a modified T-junction device was developed by Song in 2011 in our group [16], as shown in Fig. 1. By introducing the sheath flow, the size of the middle flow is not only contributed by the size of microchannel but also the sheath flow rate. In this way, a tremendous economic value as well as the need of recycling the device has been achieved.

Although it has been proved that the controllability and uniformity of the microspheres generated using this device is acceptable [16], how the flow rate, channel size, and fluid property may influence the microspheres generation process has not been understood very well. Primary work has been done

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to study the effects from capillary number on the droplet formation in an analytical manner [17]. However, this model only considers part of the device structure.

The model in this paper considered the complete structure of the modified T-junction device. And this model could be further used for optimization and control the microsphere generation. Experiments were conducted to validate the model.

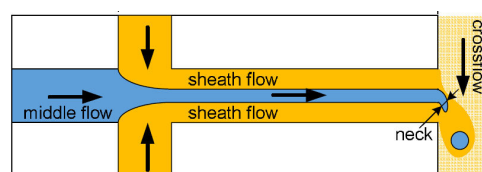


Fig. 1 Schematic diagram of a modified T-junction device: Three flows are involved: middle-flow, sheath-flow, and cross-flow. The fluid of sheath-flow and cross-flow are the same, which is immiscible with middle-flow [16]

II. MATERIALS AND PROPERTIES

In this work, Poly(lactic-co-glycolic acid) (PLGA) dissolved in dichloromethane (DCM) with concentration of 1%, 5%, and 15%, respectively, were used as dispersed phase. Polyvinyl alcohol (PVA) dissolved in distilled water with concentration of 1% was used as continuous phase. The physical properties are listed in Table I.

TABLE I
PHYSICAL PROPERTIES OF FLUIDS

	Concentration (%)	Density (g/cm ³)	Viscosity (Pa.s)
PLGA	1	1.329	0.12
	5	1.326	0.19
	15	1.315	0.33
PVA	1	1	1.702 [18]

PLGA (50/50, inherent viscosity 0.16-0.24 dl/g) was purchased from Jinan Daigang Biomaterial Co., Ltd (Jinan, Shandong, China), and Evonik Industries AG (Essen, Germany). PVA (Mw 85,000-124,000, 99+% hydrolyzed) was purchased from Shanghai Lingfeng Chemical Reagent Co., Ltd (Shanghai, China). DCM was purchased from Shanghai Chemical Reagent Co., Ltd (Shanghai, China). PDMS microchannel was fabricated in Shanghai Wenchang Chip Technology Co., Ltd (Shanghai, China).

III. STRUCTURE OF THE DEVICE

There were two structures of the modified T-Junction in this study: modified T-junction with straight channel, and modified T-junction with crooked channel, as shown in Fig 2 (a) and (b),

respectively. For both structures, all the channels were uniform in width and height. The details of the devices are listed in Table II.

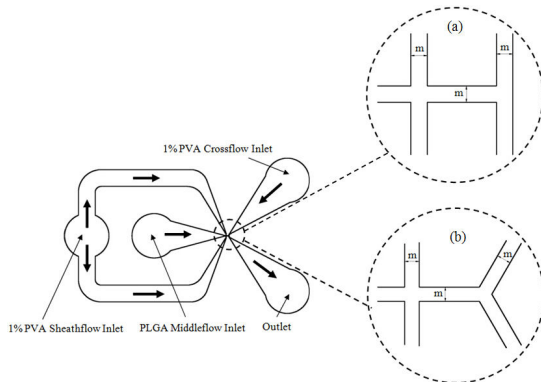


Fig 2 Schematic diagram of modified T-junction device: Channels are molded in PDMS. PLGA solutions with different concentrations are used: 1%, 5%, and 15%. *m*: channel width and height. (a) straight channel; (b) crooked channel

TABLE II
STRUCTURE AND DIMENSIONS OF MODIFIED DEVICE

Device	Structure	<i>m</i> (μm)
1	straight	50
2	straight	75
3	crooked	50
4	crooked	100

IV. THE MODEL OF THE DROPLET FORMATION PROCESS

A. Governing Equation

The Level Set (LS) method [19] was used in this study, which represents the front profile of the droplet. The LS equation could be expressed as

$$\frac{\partial \phi}{\partial t} + \mathbf{u} \cdot \nabla \phi = \gamma \nabla \cdot \left[\varepsilon \nabla \phi - \phi(1 - \phi) \frac{\nabla \phi}{|\nabla \phi|} \right] \quad (1)$$

where $\phi(x, t)$ is the level set function; x is the co-ordinate of system. If $\phi(x, t) > 0.5$, it refers to one phase; otherwise it refers to the other phase. Further, in the above equation, u is velocity (m/s); t is time (s); γ and ε are numerical stabilization parameters; ε is the thickness of the interface and has the same order of the mesh size; γ is the re-initialization parameter, and its value is the maximum value of u .

The Navier-Stokes (NS) equations and the continuity equation are the other two governing equations, and they are

$$\rho \left(\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} \right) = \nabla \cdot [-p\mathbf{I} + \eta(\nabla \mathbf{u} + (\nabla \mathbf{u})^T)] + \mathbf{F}_{st} \quad (2)$$

$$\nabla \cdot \mathbf{u} = 0 \quad (3)$$

where ρ denotes density (kg/m³); η is the dynamic viscosity (Pa·s); p is the pressure (Pa). $\mathbf{F}_{st} = \sigma \kappa \delta \mathbf{n}$ is the surface tension force (N/m³) acting on the interface between two phases, where σ is the surface tension coefficient; δ is the function concentrated at the interface between the two fluids; κ is the

curvature of the interface which can be defined as $\kappa = -\nabla \cdot \mathbf{n}$, where the normal vector \mathbf{n} can be written as $\mathbf{n} = \frac{\nabla \phi}{|\nabla \phi|}$.

The overall density ρ and viscosity η are calculated from:

$$\begin{aligned} \rho &= \rho_1 + (\rho_2 - \rho_1)\phi \\ \eta &= \eta_1 + (\eta_2 - \eta_1)\phi \end{aligned} \quad (4)$$

where ρ_1, ρ_2, η_1 and η_2 are the densities and viscosities of fluid 1 and fluid 2, respectively.

B. Boundary and Initial Conditions

All the flows (middle-flow, sheath-flow, and cross-flow) were assumed to be laminar flows, as this droplet formation process was in micron scale. The pressure in the outlet was 0 Pa without viscous stress. The boundaries were in no-slip conditions. $Q_s, Q_m,$ and Q_c are the flow rates of sheath-flow, middle-flow, and cross-flow, respectively. In this work, $Q_m = Q_s = 0.01$ ml/min were set to be constants. Fig. 3 illustrates the boundary and initial conditions. 9133 and 7815 triangular elements were applied for straight and crooked channel respectively considering accuracy and computational efficiency.

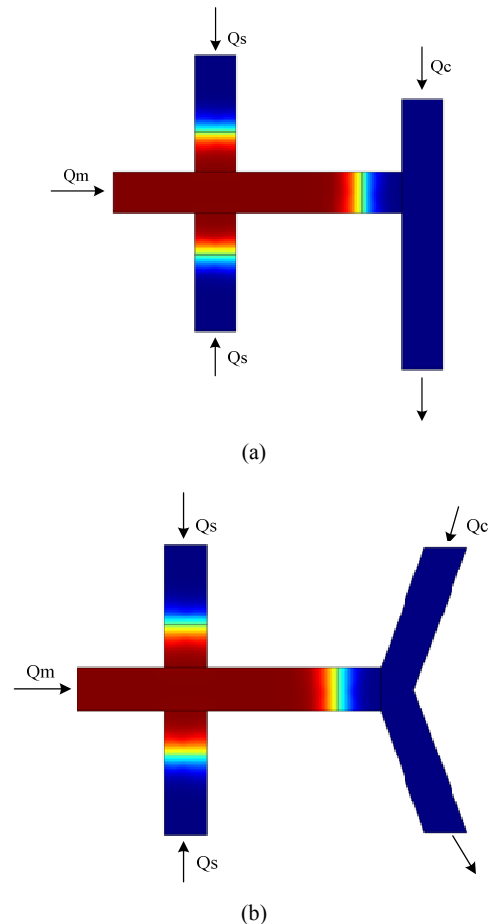


Fig. 3 Initial conditions for the simulation of the droplet formation process: (a) straight channel, (b) crooked channel

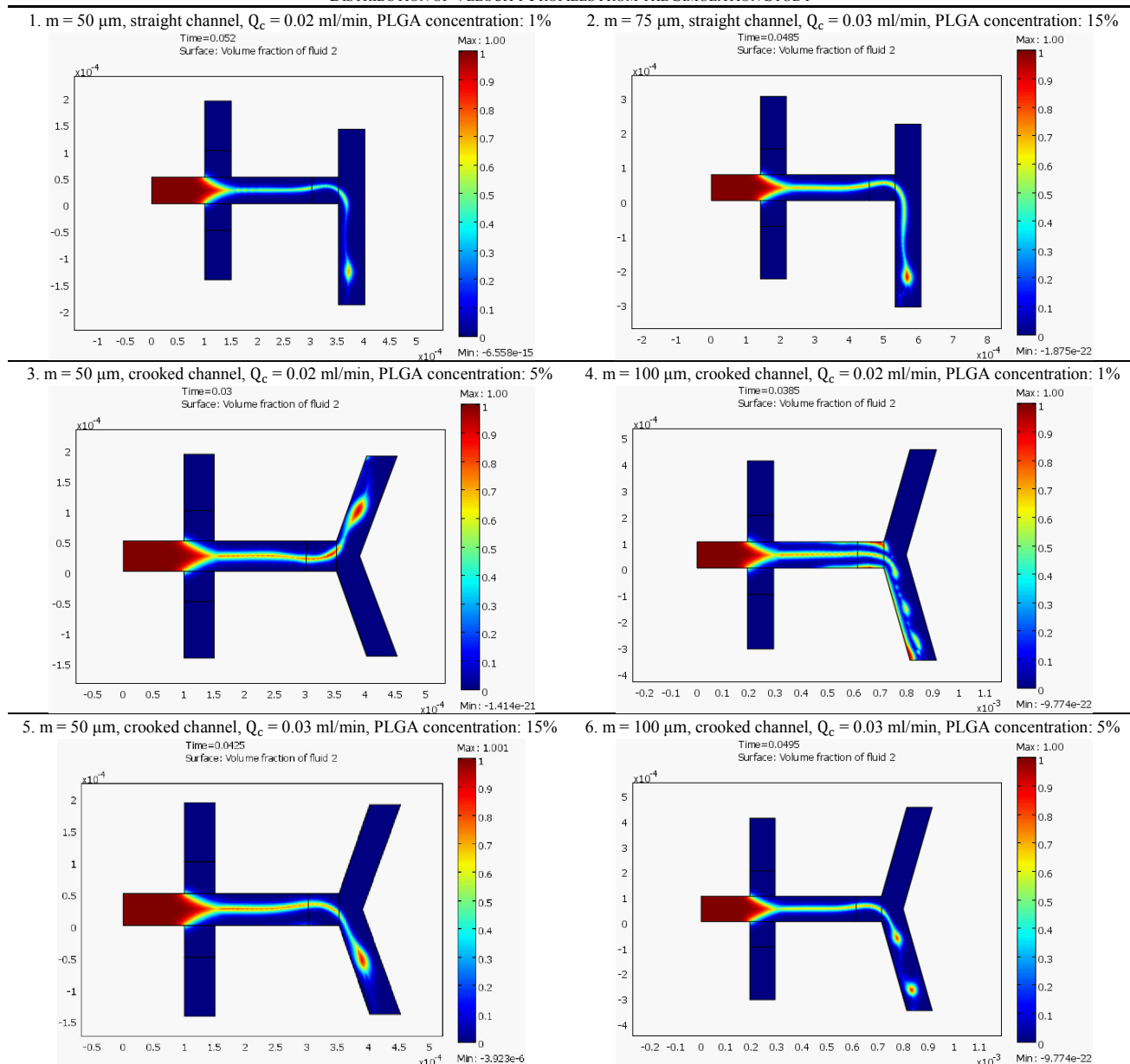
The numerical simulation was carried on using COMSOL Multi-physics 3.5 (COMSOL, Inc., Burlington, MA, USA) with the assumption of the two-dimensional and two-phase flow.

C. Experiments

Four devices were fabricated and tested in the experiment. Fig. 4 shows the experimental set-up. Three syringe pumps for sheath-flow, middle-flow and cross-flow were connected to the

microchannel device controlling the flow rate of the fluids, an optical microscope was used to observe microsphere generation, and the images of microspheres were taken by a computer system connected to the microscope. A commercial image processing software was applied to measure the size of microspheres using the images Fig. 4 shows the experimental set-up.

TABLE III
DISTRIBUTION OF VELOCITY PROFILES FROM THE SIMULATION STUDY



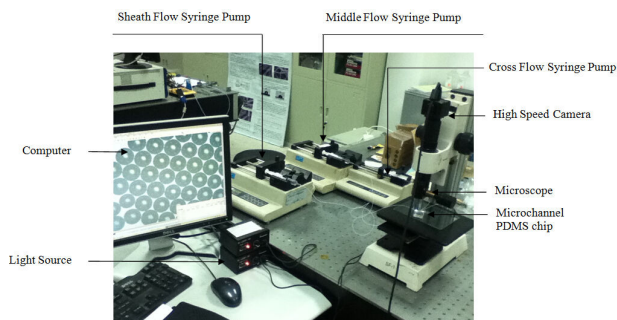


Fig. 4 Experimental set-up

V. RESULTS WITH DISCUSSION

Results of velocity distribution profiles are put in Table III.

Table IV and Fig. 5 conclude the numerical and experimental results of microsphere mean and standard (std) deviation of the sizes of microspheres. It is clear that the numerical and experimental results have a good agreement except for group 1, in which the calculated mean size of microsphere is twice the experimental one. This is probably caused by the unsteady environment during the experiments, or the channels in the devices might be clogged by PLGA after DCM has evaporated, leading to the dramatic decrease of the size of the microspheres. Second, the structure of the device, channel size, PLGA concentration, and the cross-flow rate all may affect the microsphere size.

TABLE IV
NUMERICAL AND EXPERIMENTAL RESULTS OF MICROSPHERE MEAN SIZE

Experiment	Diameter of microspheres (μm)	
	Numerical	Experimental
1	21.33	10.98 \pm 1.81
2	41.57	39.42 \pm 4.73
3	23.18	21.04 \pm 2.21
4	49.05	47.98 \pm 4.72
5	45.81	43.15 \pm 3.22
6	33.95	35.56 \pm 3.83

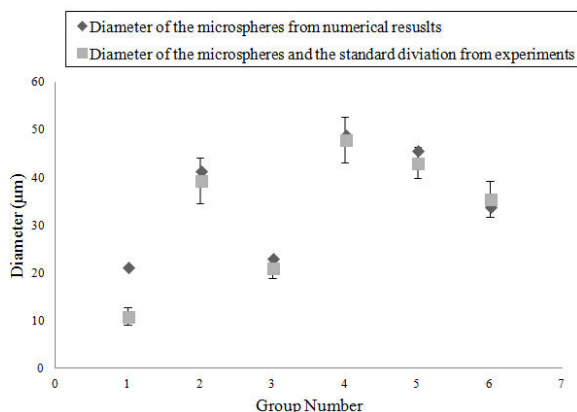
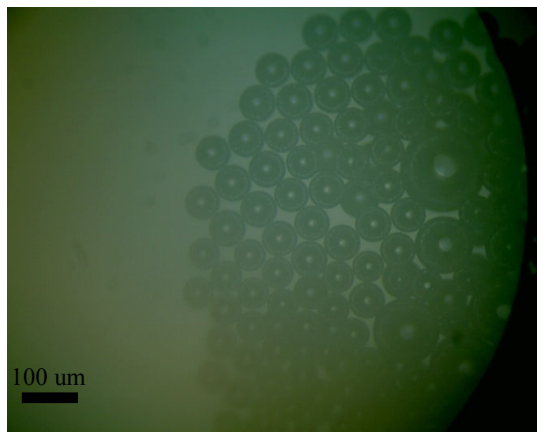


Fig. 5 Diameter of the microspheres from numerical and experimental results

Fig. 6 is an optical image of microspheres generated in the device with $m = 50 \mu\text{m}$, crooked channel, $Q_c = 0.03 \text{ ml/min}$.

Fig. 6 Optical image of microspheres generated. $m = 50 \mu\text{m}$, crooked channel, $Q_c = 0.03 \text{ ml/min}$

VI. CONCLUSION

The study presented in this paper was on the modeling of microspheres generation process in the context of the modified T-junction. Results obtained by this model were compared with experimental results. From the comparison, it can be concluded that a good agreement has been achieved. Thus the model is a reliable alternative of the measurement, which can be used to optimize the process parameters of the fluid and the device. Additionally, attentions need to be concentrated to the clog issue of the device in order to improve the accuracy and recyclability of the device.

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