

A Dose Distribution Approach Using Monte Carlo Simulation in Dosimetric Accuracy Calculation for Treating the Lung Tumor

Md Abdullah Al Mashud, M. Tariquzzaman, M. Jahangir Alam, Tapan Kumar Godder, M. Mahbubur Rahman

Abstract—This paper presents a Monte Carlo (MC) method-based dose distributions on lung tumor for 6 MV photon beam to improve the dosimetric accuracy for cancer treatment. The polystyrene which is tissue equivalent material to the lung tumor density is used in this research. In the empirical calculations, TRS-398 formalism of IAEA has been used, and the setup was made according to the ICRU recommendations. The research outcomes were compared with the state-of-the-art experimental results. From the experimental results, it is observed that the proposed based approach provides more accurate results and improves the accuracy than the existing approaches. The average %variation between measured and TPS simulated values was obtained 1.337 ± 0.531 , which shows a substantial improvement comparing with the state-of-the-art technology.

Keywords—Lung tumor, Monte Carlo, polystyrene, elekta synergy, Monaco Planning System.

I. INTRODUCTION

EFFICIENT dose calculation is the most challenging task in the world for clinical medical physicist. The ultimate goals of the physicists are to deliver the maximum dose to the cancerous tissues and minimum dose to the normal tissues and risk organs and to save the normal tissue. This approach is engaged in variety of cancer treating research.

One of the most significant parameters in dosimetric analysis is Tissue Phantom Ratio (TPR) measurement [1]. Instead of using the available conventional expression, this paper chooses the most valuable 2-point measurement expressions and adaption of interpolation for that purpose. There are many advantages for 2-point measurement and adaption of interpolation such as reducing the computational time, improving the precision and monitoring the quality assurance (QA).

The two well-known patient setup techniques for delivering dose to the carcinoma patients are Source to Surface Distance (SSD) technique and Source to Axis Distance (SAD) or isocentric technique [2]. The SSD technique is more convenient to

assess the percent depth dose (PDD), but it is inconvenient for patients. Actually, human body is inhomogeneous and different organs are sited at different depth from the body surface. On the other hand, the SAD technique is very convenient for delivering dose to the patients. However, the SAD technique required high number of measurements.

Besides, several commercial treatment planning systems use various types of dose calculation algorithm [3]-[5]. The most useful algorithms are three dimensional convolution [6], [7], collapsed cone convolution (CCC) [8], anisotropic analytical algorithm (AAA) [9] and MC Methods [10]-[15]. For high calculation speed, the CCC method is widely applied in commercial treatment planning systems. However, the differences greater than 5% have found at the materials for several densities such as between lung and tissue [16], [17]. The 5% difference is deemed unacceptable for better dosimetry to deliver the dose to the patients [18], [19]. The dose calculation speed is comparatively slow in the MC method. However, it has better accuracy compared to the other algorithms [20]. MC based calculation focuses on the inhomogeneity correction [21]. Photon beam dose calculation which is formulated by using MC methods [22] has adapted the American Association of Physicist of Medicine. The MC base dose calculation been has suggested [23] for commercial treatment planning systems and for the air cavity measurement [24]. Dosimetric accuracy calculation and QA has been estimated using AAA algorithm [25], here, the difference is found to be less than 5% but very greater than 2%. The accuracy is recommended less than 2% for better treatment [26]. Moreover, the population density is so high in our country. Beside this, the carcinoma patients increase day by day due to the illiteracy, poverty, food habited, chain smoking and alcohol. The developing countries like Bangladesh have the limitations of radiotherapy facilities due to the economic constraints.

In this paper, consideration of time, accuracy, number of carcinoma patients and organizational limitations: we have

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proposed a novel method adopting the MC simulation-based treatment planning system for simulation and 2-point measurement technique with adaption of interpolation for measurements. The proposed approach could be more beneficial in cancer treatment in the developing countries. The focus of the present study is to evaluate the accuracy of the TPS for photon calculations using MC simulations in lung irradiation in order to measure accurately the point dose in the lung tumor.

II. TRADITIONAL TPR MEASUREMENT METHOD

Basically, TPR is measured using SAD technique, i.e. isocentric technique which needs huge number of measurement. It is obvious that much measurement is time consuming and may lead to significant human error because of fatigue. Besides, errors may also occur due to complexity of the dosimetry setup. The formula for TPR measurement equation [2] is as in (1)

$$TPR_{(S,Q,d)} = \frac{D_d}{D_{ref}} \quad (1)$$

where D_d is the dose at any depth and D_{ref} is the dose at reference depth

III. PROPOSED APPROACH FOR TPR MEASUREMENT

To avoid the complexity of TPR measurement, this paper adopted the following mathematical model [27] for measurement in inhomogeneous medium. This method has been investigated for inhomogeneous medium and found sound results. This research proposed to adapt this approach with MC method-based treatment planning system. The 2-point measurement equation with adaption of interpolation equation is as in (2)

$$TPR(d, FS_A) = \frac{1}{100} \cdot PDD(d, FS_A \frac{X}{Y}, X) \times \left(\frac{Y}{Z}\right)^2 \times \frac{S_{PA}(FS_A \frac{X}{Y})}{S_{PD}(FS_A \frac{R}{Y})} \quad (2)$$

where d is the depth in cm for required TPR, FS_A is desired field size for TPR measurement, $X = SSD = 100$ cm, $Y = SSD + d = 100 + d$ cm, $Z = SSD + d_r = 100 + \text{reference depth (10 cm)}$, S_{PA} is scattering factor at phantom surface, S_{PD} is scattering factor at depth ($d+SSD$) and $R = SSD + d - d_r$.

It is easier to perform the PDD measurement using fixed surface to source distance (SSD) technique. Its needs only two values at any two points. Then, we convert these values to TPR. This is also less inclined to error because of less difficulty in the dosimetry setup and measurement. The simulated formula could be used to calculate the TPR values for isocentric treatment, otherwise it would have needed complex and elaborate measurement setup changes under SAD formalism. Therefore, the present work will have a big impact on the quality and safety of radiotherapy in the global arena, particularly in the Third World.

IV. MATERIAL AND METHODS

Tumors in lungs are usually radiated either anteriorly (from the front) or posteriorly (from the back). Here, it is assumed that only a single fraction from any one of the above two directions is used and the phantom was designed accordingly. A rectangular piece of polystyrene having density 1.06 g/cc and size 40cm(l) \times 40cm(b) \times 1.5cm(h) has been employed for performing the simulation of lung tissue with extensive tumor (large-mass) which is treated as lung tumor tissue equivalent materials [28]. It has been fixed inside the water phantom in such that the bottom of its remains at a depth of 1.5 cm from the water surface. This was done to represent skin, soft tissue above the body fluids. However, the effect would be very small. It also may simulate cancer tumor on the surface of the lung. The water phantom had a dimension of 40cm \times 40cm \times 40cm. The radiation was applied on the field sizes of 5cm \times 5cm and 10cm \times 10cm. The phantom was made in accordance with the ICRU methodology [29]. The doses were measured along the central beam axis underneath the polystyrene in the phantom. For these dose measurements, an ion chamber with a small volume of 0.125cc was used.

MC based Monaco TPS as a conventional dose calculation system was used in this research. Firstly, a treatment plan has been made for the above inhomogeneous phantom for an SSD of 100 cm which offered isodose distributions for different field sizes at different depths [30]. Then, actual dose measurements were carried out in two dimensions along different horizontal planes corresponding to different depths below the polystyrene inside the water phantom. These were carried out for the specified field sizes and depths as used for the treatment plan. Then, we correlated the treatment plan data and the measured dose to determine the efficacy of our simple inhomogeneous phantom.

The methodology consisted of:

1. The measurements of dose (output) were done with calibrated dosimetry system for different clinical field sizes at 100 cm SSD by using IAEA, TRS-398 protocol [31]. The calibrated ionization chamber was set at reference depth in water phantom. Nowadays, phantoms of other materials are also available for the dosimetry of the teletherapy units but due to equality of density with human tissue, the water phantom has superiority on others [32]
2. IAEA's TRS-398 (2004) protocol [31] was used to obtain the absorbed dose to water at reference depth Z_{ref} in a photon beam of quality Q using the following formula:

$$D_{W,Q}(Z_{ref}) = M_Q \times K_{Q0} \quad (3)$$

where M_Q is the reading of the dosimeter with the reference point of the chamber positioned at Z_{ref} in accordance with the reference conditions [33].

$$M_Q = M_R \times K_{pol} \times K_s \times N_{DW} \times K_{TP} \quad (4)$$

$$M_R = \text{Electrometer reading}$$

$$K_{pol} = \frac{|M_+| + |M_-|}{2M} \quad (5)$$

K_{Pol} = Change in polarity factor to correct the ionization chamber response on change of polarizing voltage. $|M_+|$ = Electrometer reading at voltage $+V_1$. $|M_-|$ = Electrometer reading at voltage $-V_2$. K_S = Ion recombination correction factor to take two electrometers reading on two voltage settings.

$$K_S = \frac{\left(\frac{V_1}{V_2}\right)^2 - 1}{\left(\frac{V_1}{V_2}\right)^2 - \left(\frac{M_1}{M_2}\right)^2} \quad (6)$$

N_{DW} = Calibration factor of electrometer and ionization chamber for absorbed dose to water. K_{TP} = Temperature and pressure correction factor and

$$K_{TP} = \frac{273.2+T}{273.2+T_0} \times \frac{P_0}{P} \quad (7)$$

where P_0 and T_0 are the reference values of pressure and temperature respectively and were taken as 101.3 kPa and 20 °C. K_{Q,Q_0} is a chamber-specific factor which corrects for the difference between the reference beam quality Q_0 and the actual quality being used, Q .

The absorbed dose rate to water at the depth of dose maximum, Z_{max} is

$$D_{W,Q}(Z_{max}) = \frac{D_{W,Q}(Z_{ref})}{TPR(Z_{ref})} \times 100 \quad (8)$$

3. The percentage variation for event of dosimetry had been calculated by comparing the output obtained by the measured value and the simulated value.

V. RESULTS AND DISCUSSION

The 6-MV photon beam direction was fixed along the zero angles of the gantry and collimator. The ion chamber was fixed perpendicular to the central axis radiation beam. The field sizes

of the beam were fixed at 5 cm×5 cm, 10 cm×10 cm and 12 cm×12 cm and the central axis depth doses recorded in units of cGy/MU for different depths. The depth doses were measured at 0.2 cm increment up to 20 cm in water with and without polystyrene. The simulated TPS of depth dose data at 0.2 cm increment up to 20 cm has been collected.

A. Perturbation Calculation

The perturbation measurement and calculation between the polystyrene values and the corresponding without polystyrene values were determined for various field sizes and the results are tabulated in Table I.

TABLE I
PERTURBATION CALCULATION BETWEEN POLYSTYRENE AND WITHOUT POLYSTYRENE

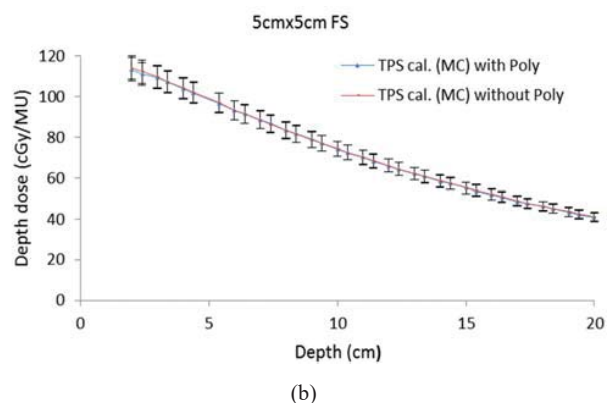
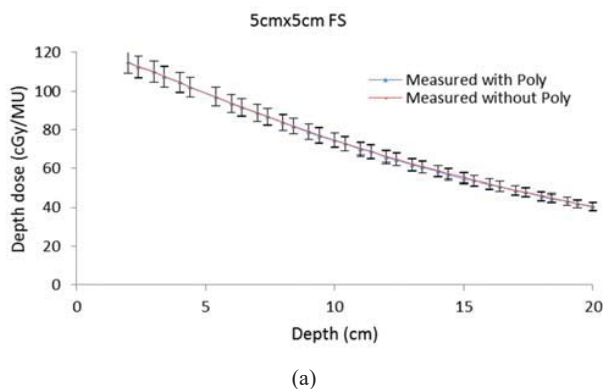
Field size	Measured	TPS Cal.
5cm×5cm	-0.86 to 0.15	0.05 to -0.91
10cm×10cm	-2.05 to 2.02	-0.12 to -1.68
12cm × 12cm	-3.01 to 0.60	-0.22 to -2.08

B. Depth Dose Measurement

The measured depth dose values are recorded and compared with the TPS simulated data for different field sizes. The graphical representation of depth dose of with polystyrene and without polystyrene of measured, and TPS simulated values are shown in Fig. 1. The treatment planning system has calculated radiation dose theoretically and using some mathematical model for inhomogeneous fields by considering the radiation basic beam data of homogeneous fields. The other correction factors were also calculated theoretically like phantom scattered correction factors, collimator scattered correction factors, tissue density correction factors and other perturbation factors [22]. However, for the in-phantom measurements, all correction factors are included with the dosages.

TABLE II
PERCENTAGE OF DEVIATION FOR MEASURED AND TPS SIMULATED VALUES WITH AND WITHOUT POLYSTYRENE

Field size (cm ²)	Measured (bet ⁿ polystyrene and without polystyrene)			TPS simulated (bet ⁿ polystyrene and without polystyrene)		
	Min difference	Max difference	Mean difference	Min difference	Max difference	Mean difference
5×5	-1.20%	-0.60%	-0.27%±0.44%	-0.98%	0.44%	-0.29%±0.39%
10×10	-1.40%	0.36%	-0.62%±0.54%	-1.55%	0.48%	-0.57%±0.40%
12×12	-1.91%	0.94%	-0.84%±0.76%	-0.19%	-0.13%	-0.94%±0.41%



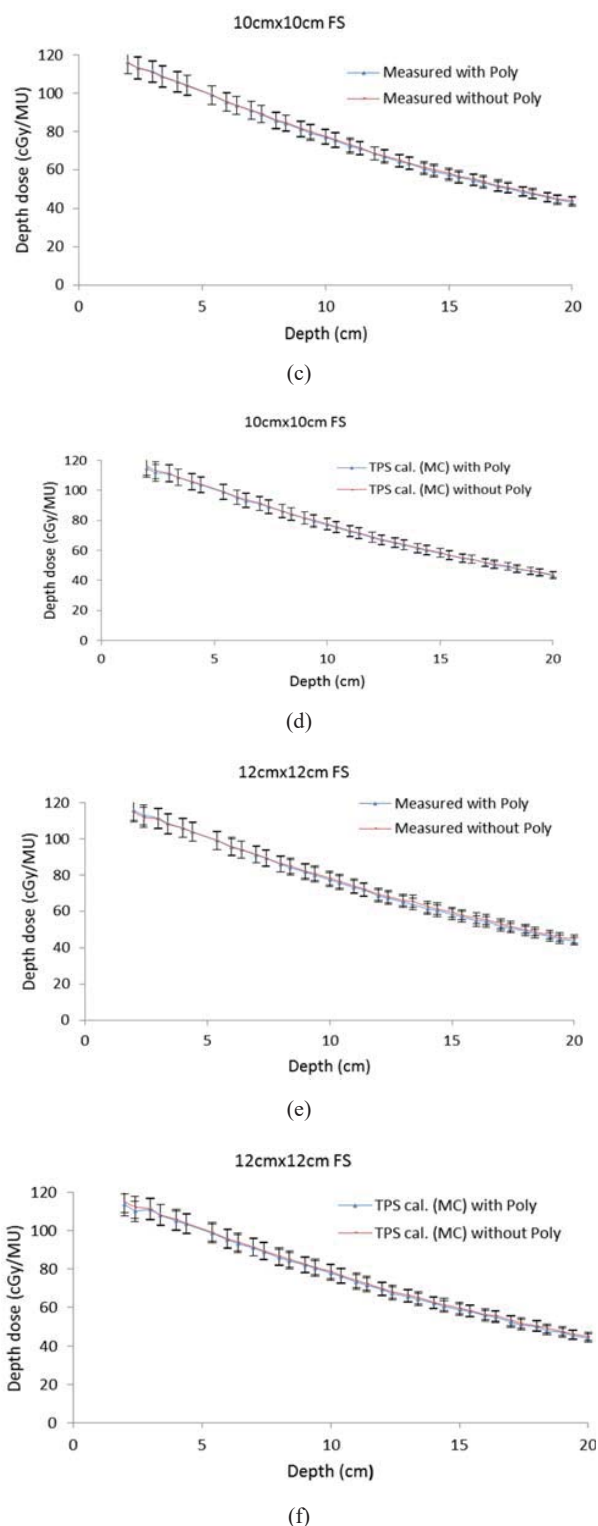


Fig. 1 Comparison of depth dose (Measured and TPS simulated) with polystyrene (inhomogeneous) & without polystyrene (homogeneous) (a) measured value of field size 5 cm² (b) simulated value of field size 5 cm² (c) measured value of field size 10 cm² (d) simulated value of field size 10 cm² (e) measured value of field size 12 cm² (f) simulated value of field size 12 cm²

It was observed from Fig. 1, that the deviations of measured and TPS simulated values were very small. The percentage of deviations of measured (between polystyrene and without polystyrene) and TPS simulated (between polystyrene and without polystyrene) have been carried out and summarized in Table II. These results are very satisfactory since variation up to 3.15% is considered acceptable [34]. Therefore, this shows a good agreement of dose calculation and QA of control data with and without polystyrene in both cases of measurement and treatment planning system.

C. PDD Measurement

The dose rate measurements for the different field sizes are shown in Fig. 2. The corresponding TPS calculated data are also shown in the same graphs. It also compared with another data that was simulated by AAA algorithm [25] in the same graph respectively. The percentage of deviation of PDD between TPS simulation and phantom measure is tabulated in Table III. The difference between the measured and calculated TPS values for the above field sizes can be observed from these graphs, which are very small. The differences between the measured values and the corresponding TPS calculated values were determined for various field sizes, and these were in the range of -0.020% to 2.154%. This result is very satisfactory since variation up to 3.5% is considered acceptable [31]. The average %variation obtained 1.337 ± 0.522 and 1.484 ± 0.725 for 5 cm \times 5 cm and 10 cm \times 10 cm field size, respectively. Therefore, this shows sound results of dose calculation and QA of treatment planning. Application of such techniques will be beneficial to patients for radiotherapy treatment and dose delivery to the targeted area.

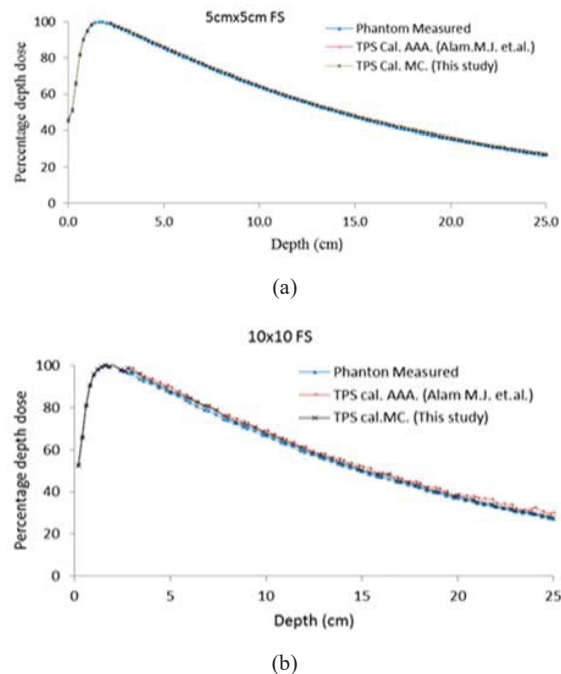
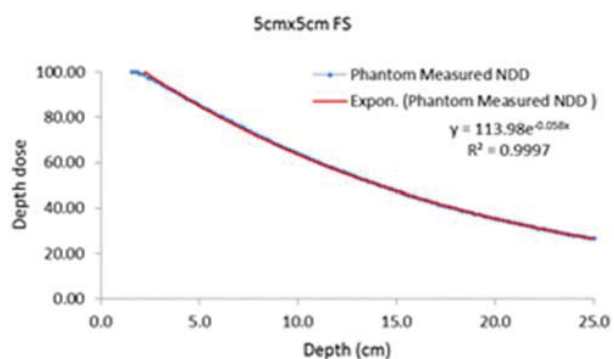


Fig. 2 Percentage depth dose for a 6MV photon beam Monaco TPS and measured using a 0.125 cc Farmer ionization chamber in an inhomogeneous phantom at SSD=100 (a) field size 5 cm \times 5 cm and (b) 10 cm \times 10 cm

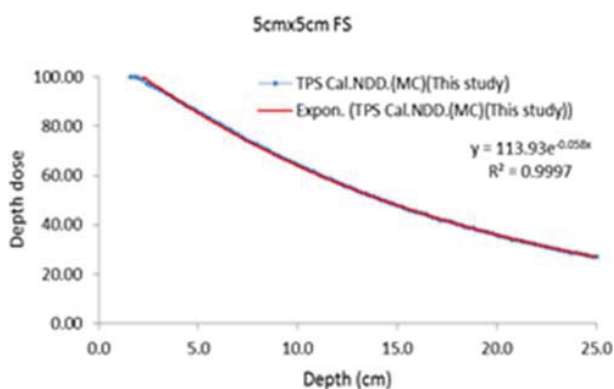
TABLE III
PERCENTAGE DEVIATION OF PDD BETWEEN TPS SIMULATED AND PHANTOM
MEASURED VALUES

Field size	Proposed Approach		Alam et al. [25]	
	Min difference	Max difference	Min difference	Max difference
5cm×5cm	0.270%	2.154%	0.892%	3.592%
10cm×10cm	-0.020%	2.142%	0.008%	3.38%

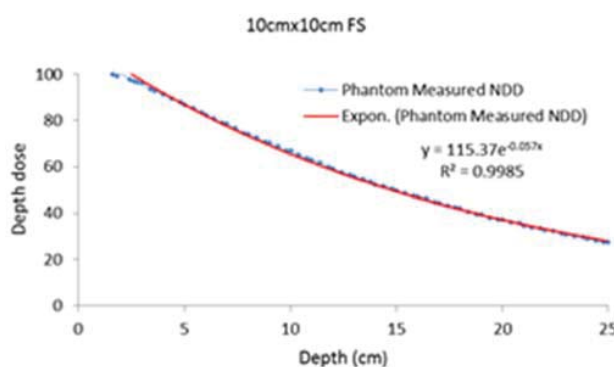
The curve fitting of measured and simulated TPS values of field sizes 5 cm×5 cm and 10 cm×10 cm is shown in Fig. 3. From the curve, it shows the differences between measured values and TPS simulated values vary within ±2%. The results show good agreement with the recommendations. The R^2 values are also summarized in Table IV.



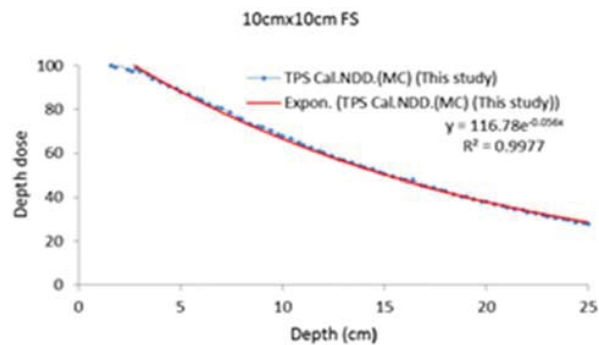
(a)



(b)



(c)



(d)

Fig. 3 Curve fitting of measured and TPS simulated percentage depth dose for a 6-MV photon beam (a) measure value for field sizes 5 cm×5 cm (b) simulated value for field size 5 cm×5 cm (c) measure value for field sizes 10 cm×10 cm and (d) simulated value for field size 10 cm×10 cm

TABLE IV
CURVE FITTING OF R^2 VALUES FOR DIFFERENT FIELD SIZES OF 6 MV PHOTON
BEAM

Field sizes	Measured	Simulated by MC (This study)	Simulated by AAA [25]
5cm×5cm	0.9997	0.9997	0.9998
10cm×10cm	0.9985	0.9977	0.9974

VI. CONCLUSION

For optimum treatment of cancer, the radiation dose must be planned and delivered with a high degree of accuracy. The international commission on radiation units and measurements (ICRU) recommends that the dose should be delivered with a deviation not greater than 5% with respect to a treatment plan, but accuracy of ±3% to ±3.5% in the overall process has been recommended [35], [36]. In this study, the overall deviation between the measured and simulated data was within or near to 2%. The maximum deviation for a very few data points was 3.29% what is beyond the recommended limit, but still within the ICRU recommendation. Therefore, the proposed approach is more efficient and will be beneficiary the developing countries like Bangladesh.

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