Designing Intelligent Adaptive Controller for Nonlinear Pendulum Dynamical System

R. Ghasemi, M. R. Rahimi Khoygani

Abstract—This paper proposes the designing direct adaptive neural controller to apply for a class of a nonlinear pendulum dynamic system. The radial basis function (RBF) neural adaptive controller is robust in presence of external and internal uncertainties. Both the effectiveness of the controller and robustness against disturbances are importance of this paper. The simulation results show the promising performance of the proposed controller.

Keywords—Adaptive Neural Controller, Nonlinear Dynamical, Neural Network, RBF, Driven Pendulum, Position Control.

I. INTRODUCTION

TISTORICALLY pendulums were used as gravimeters to measure the acceleration of gravity in geophysical surveys, and even as a standard of length. Generally, they used to regulate pendulum clocks, in scientific instruments such as accelerometers, seismometers and widely in aerospace technology, robotics and etc. [1]. Many researches on modern control theory and intelligent control theory it as study object and many new control theories and methods are developed, because it consists of some physical subjects such as the simple harmonic motion, the period of oscillation, the acceleration of gravity, the center of mass, the moment of the inertia, momentum, etc. [1]. The Nonlinear Driven Pendulum Dynamical system poses a challenging control problem. However, the comparatively complex system is hard for low cost microcontrollers to process in many control systems. Intelligent computational techniques such as Artificial Neural Network (ANN), Fuzzy Logic theory (FL), Genetic Algorithm (GA) and etc., which have given novel solutions to the control nonlinear system problems [2]-[6].

Neural Networks (NNs) play a significant role in control engineering, especially in nonlinear system control. Due to their public approximation abilities, learning, and adaptation abilities, they are used to estimation unknown nonlinear functions. This makes them one of the effective tools in nonlinear controller system design. Active research has been carried out in NN controller by using the fact that NNs can estimate a wide range of nonlinear functions to any desired degree of accuracy under certain conditions.

The real capability of RBF Neural Networks for modeling and learning has rapidly increased in recent years. The weight update laws of the RBF networks are derived in such a way that the closed loop system is stable and the output tracking error converges to 0 with time. When the approximation error of the RBF networks are taken into account, the weight update laws are modified in [7] for closed loop stability. But in this paper we have shown that the same update law can maintain the closed loop stability with a bounded tracking error. Though, the proposed adaptive control scheme is implementable only for a class of nonlinear pendulum dynamical system, however there are many practical systems f for utilization.

There are literatures present which have taken linearization model of nonlinear Driven Pendulum dynamical System for implementing the various control schemes [8]-[12]. The paper aims to studying Position control the nonlinear Driven Pendulum dynamical system under the step input. To solve this problem, proposed a direct adaptive control scheme to achieve output tracking. The main advantage of a direct adaptive control scheme over an indirect adaptive control scheme is that in a direct adaptive control scheme there is no need for explicit system identification. In indirect adaptive control scheme, the system is generally identified off-line from its input-output data and the controller is designed based on the identified system model. The identified model should be accurate enough for better performance of the controller. Moreover stability is a critical issue in indirect adaptive control. But in direct adaptive control, the controller is designed in such a way that the closed loop stability is maintained while the tracking error converges to 0 with time. Theory of direct adaptive control is analyzed to demonstrate the effectiveness of the control scheme simulation is developed with in Simulink and Matlab for evaluation of the control strategy.

The contents of this paper are organized as follows: Section II Provided Mathematical modeling. Section III direct adaptive neural controller by RBF neural network; Section IV simulation and results; finally, in Section V presented a brief conclusion.

II. MATHEMATICAL MODELING

It is obvious that in order to analysis and control of a physical system, it is necessary to construct the mathematical modeling. In the above picture, there is a DC motor with a propeller on the lead of a suspended stick. After applied voltage, the propeller spins and generates torque T to pull up the pendulum. It is the most benefits of driven pendulum that enables us controlling its behavior with regulating the applied voltage. Therefore, the control variable for this system is the angle of the pendulum settled and the manipulated variable is the voltage fed to the motorized-propeller. The schematic

Reza Ghasemi and Mohammad Reza Rahimi Khoygani joined the Department of Control Engineering, Damavand Branch, Islamic Azad University, Damavand, Iran (e-mail: Rezaghasemi @Damavandiau.ac.ir, Mohamad.reza.rahimi67@gmail.com).

picture of the suspended pendulum control system is given in Fig. 1.

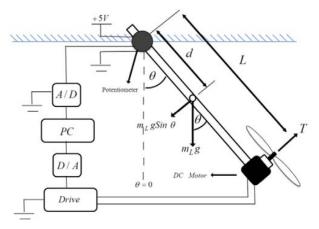


Fig. 1 The Driven Pendulum system

The rational equation between V voltage which applied to DC motor and thrust T, can be written as follows:

$$T = Km \, V \tag{1}$$

According to Newton's laws and angular momentum, the motion equation of driven pendulum is derived as:

$$J.\ddot{\theta} + c.\dot{\theta} + m_L.g.d.\sin\theta = T$$
⁽²⁾

The generated trust T in above equations is not manipulated variable for control system since the pendulum is adjusted by applied voltage.

$$\ddot{\theta} = \frac{K_m V - c.\dot{\theta} - m_L.g.d.\sin\theta}{J}$$
(3)

where, m=weight of the pendulum, L=Length of pendulum, J=inertia moment, g=acceleration of gravity, V=voltage DC motor, T=the thrust which is provided by DC motor, θ =angular position, c=viscous damping coefficient, d=the distance from suspending point to center of mass. For numerical simulation of the nonlinear model for the driven pendulum system, it is required to represent the nonlinear equations (4) into standard state space form:

$$\frac{d}{dt}X = F(x,u) \tag{4}$$

Now these equations may be represented into state space form by considering the state variables as following;

$$X_1 = \theta , X_2 = \dot{\theta} = \dot{X}_1 , \dot{X}_2 = \ddot{\theta}$$
(5)

Then, the final state space equation for the driven Pendulum system may be written as:

where

$$\frac{d}{dt}X = \frac{d}{dt}\begin{bmatrix} X_1\\ X_2 \end{bmatrix} = \frac{d}{dt}\begin{bmatrix} \theta\\ \dot{\theta} \end{bmatrix}$$
(6)

$$\begin{aligned} \dot{x}_1 &= x_2 \\ \dot{x}_2 &= f(x) + g(x)u + d(x) \\ y(x) &= h(x) = x_1, u = V \\ f(x) &= -J^{-1}(cx_2 + m_L g.d.\sin(x_1)) \\ g(x) &= K_m J^{-1} \end{aligned}$$

d(x) is disturbance The pendulum angle θ is the variable of interest, and then the output equation may be written;

$$Y = [x] = CX = \begin{bmatrix} 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$
(8)

III. DIRECT ADAPTIVE NEURAL CONTROLLER

Artificial Neural Networks (NNs) which are inspired by biological nervous systems are promising and powerful tools in identification and modeling of non-linear systems due to their effective suitability in earning capabilities and data processing. Radial basis function (RBF) networks are feedforward networks; they are typically configured with a single hidden layer of units whose activation function is selected from a class of functions called basis functions. While similar to back propagation in many respects, radial basis function networks have several advantages. They usually train much faster than back propagation networks. They are less susceptible to problems with non-stationary inputs because of the behavior of the radial basis function hidden units. The structure RBF neural network is shown in Fig. 2.

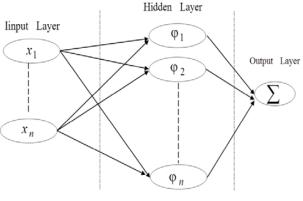


Fig. 2 The RBF neural network

The problem arises with Feedback Linearization Control (FLC) techniques when the nonlinear functions f(x) or g(x) or both are unknown. For such cases different function approximators like neural networks or fuzzy systems can be used to estimate these nonlinear functions.

A. f(x) Is Unknown: Using FLC

In this section we have assumed that the function f(x) is

unknown while the function g(x) is known. f(x) is approximated by a RBF network. Feedback linearization is a common approach used in controlling nonlinear systems that has attracted lots of research in recent years. The central idea is to algebraically transform nonlinear systems dynamics into (fully or partly) linear ones. The approach involves coming up with a transformation of the nonlinear system into an equivalent linear system through a change of variables and a suitable control input, so that linear control techniques can be applied. As can be seen from Fig. 2, the RBFN has a single output thus the network weight constitutes a vector Win this case. Then the control law;

$$u = \frac{1}{g(x)} \left[-\hat{f}(x) - k_v r + \dot{x}_{2d} + \lambda e^{(1)} \right]$$
(9)

where e is output tracking, $\hat{f}(x)$ is approximated f(x), r is power denotes respective derivatives, k_v and λ are positive design parameters, the closed loop error dynamics becomes;

$$\dot{r} = -k_v r \tag{10}$$

where

$$r = e^{(1)} + \lambda_1 e \cdot e^{(1)} = \dot{e} \tag{11}$$

Using (7), the output tracking error is defined as;

$$e = y_d - y = x_{1d} - x_1 \tag{12}$$

where y_d is ideal output system, and y is real output system. There exist weights such that;

$$f(x) = W^T \varphi(x) + \varepsilon \tag{13}$$

 ε is the estimation error, W is the ideal network weights, that can be approximated f(x), therefore, network weights are constant. Here have assumed that the estimation error ε =0. Therefore, Let f(x) be approximated as

$$\hat{f}(x) = \hat{W}^T \varphi(x) \tag{14}$$

when the structure of the neural network is known, a suitable learning rule should be appointed to educate the network. This weight-updating mechanism is usually defined in such a way that the stability of the observer is guaranteed. Where \hat{W} is updated using the update law

$$\hat{W} = -F\phi(x)r \tag{15}$$

where parameter matrix F is taken as the diagonal matrix of appropriate dimension .The structure direct adaptive neural controller by RBF neural network for this section is shown in Fig. 3.

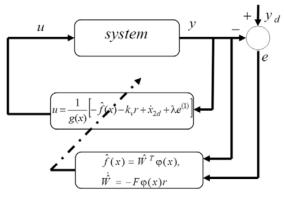


Fig. 3 The structure direct adaptive neural controller

B. When f(x) and g(x) Are Unknown: Using FLC and SMC

It is difficult to achieve closed loop stability when both f and g are unknown. It is assumed that |g(x)|>0. An additional sliding mode term is added with the control input to maintain the closed loop stability. Sliding Mode Control (SMC) is a kind of control technique of variable structure control systems. Sliding mode control technique is based on forcing the error vector into desired dynamic and holding in this dynamic. The line whereof was discussed was called as surface, switching surface, sliding surface over time. The basic philosophy at the sliding mode control is to generate control strategy at the sliding surface. The control law when both f and g are unknown:

$$u = u_1 + u_2 \tag{16}$$

where

$$u_1 = \frac{1}{\hat{g}(x)} \left[-\hat{f}(x) - k_v r + \dot{x}_{2d} + \lambda e^{(1)} \right]$$
(17)

Therefore, Let f(x) and g(x) be approximated as;

$$\hat{f}(x) = \hat{W}^T \varphi(x)$$

$$\hat{g}(x) = \hat{P}^T \psi(x)$$
(18)

where $\hat{f}(x)$ and $\hat{g}(x)$ are estimated,

$$u_{2} = \frac{|\hat{g}(x)|}{g_{1}} |u_{1}| \operatorname{sgn} r$$
(19)

where g_1 is lower bound of g, the structure direct adaptive neural controller by RBF neural network for this section is shown in Fig. 4.

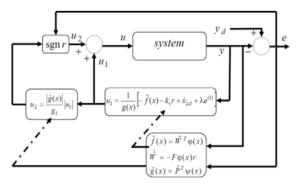


Fig. 4 The structure direct adaptive neural controller

IV. SIMULATION AND RESULTS

The proposed controller has been applied on the nonlinear pendulum dynamical system. If the value of d = 0.03 m, ml = 0.36 kg, $g = 9.8 \text{m/s}n^2$, $J = 0.0106 \text{ Kg}m^2$, c = 0.0076 Nms/rad, Km = 0.0296. The basic concepts of controllers and the mathematical model of system are presented in past sections.

A. f(x) Is Unknown:

The parameters K_v and λ are chosen as 20 and 15, respectively. The number of neurons for the RBF network is taken as 30. The centers of the RBF network are chosen randomly between 0 and 1 and weights are initialized to very small values. The parameter matrix F is taken as the diagonal matrix with elements 1. The output tracking result and output tracking error are shown in Fig. 5.

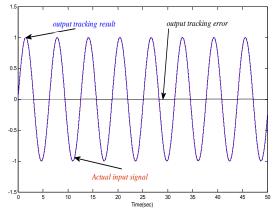


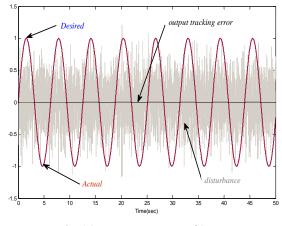
Fig. 5 The output tracking and control input

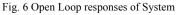
The output tracking responses and output error in presence disturbances with power 0.001 and Frequency signal 1000 are illustrated in Fig. 6 which demonstrated the responses are very appropriate.

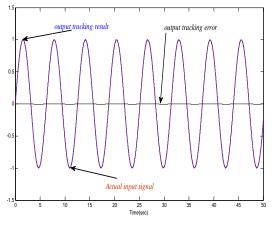
B. f(x) And g(x) Are Unknown

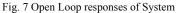
Where r, K_v and λ are same as that of previous case, the lower bound of g is set to $g_1 = 1$. The number of neurons for both RBF networks is taken as 30. The centers of the RBF networks are chosen randomly between 0 and 1. The weights

of the networks are initialized such that the initial estimation of g is greater than the lower bound g_1 . The parameter matrices F and G are taken as diagonal matrices with diagonal elements 5 and 1, respectively. Tracking result and tracking error are shown in Fig. 7.









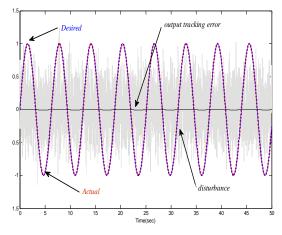


Fig. 8 Open Loop responses of System

In Fig. 8 observed the output tracking responses and output error with disturbances to power 0.001 and Frequency signal 1000 stays stable.

V. CONCLUSION

The strategy for adaptive neural network control of driven pendulum system nonlinearity and the input nonlinearity have been assumed to be unknown and RBF networks have been used to approximate those nonlinearities. Feedback linearization techniques have been successfully used over the past decades to design controllers for nonlinear systems. The controller design becomes difficult when the functions of system are unknown completely. Direct adaptive control with the update laws for the networks used to establish stability of the closed loop system. A sliding mode term was added to the adaptive control law to maintain the boundedness of the closed loop system. The simulation results show the promising performance of the proposed controller.

REFERENCES

- M.R.Rahimi, R. Ghasemi, D.Sanaei, "Designing Discrete Time Optimal Controller for Double inverted pendulum system," *International Journal on Numerical and Analytical Methods in Engineering*, Vol.1,N. 1, pp. 3–7, 2013.
- [2] Y. Becerikli, A.F. Konar, and T. Samad, "Intelligent optimal control with dynamic neural networks", *Elsevier Journal of Neural Networks*, Vol. 16, 2003, pp 251–259.
- Vol. 16, 2003, pp 251–259.
 [3] M. A. Abido, "Optimal Design of Power–System Stabilizers using Particle Swarm Optimization", *IEEE Transactions on Energy Conversion*, Vol. 17, No. 3, Sep 2002, pp. 406-413.
- [4] K.M. Passino, and S. Yurkovich, Fuzzy Control, Addison Wesley Longman, Inc., California, 1998.
- [5] T. I. Liu, E. J. Ko, and J. Lee, "Intelligent Control of Dynamic Systems", Journal of the Franklin Institute, Vol. 330, No. 3, pp. 491-503, 1993.
- [6] Astrom K. J., and McAvoy Thomas J., "Intelligent control", J. Proc. Cont. 1992, Vol. 2, No 3, pp 115-127.
- [7] F.L. Lewis, S. Jagannathan, A. Yesildirek, Neural Network Control of Robot Manipulators and Nonlinear Systems, Taylor & Francis, 1999.
- [8] S. Srinivasulu Raju, T.S. Darshan and B. Nagendra, "Design of Quadratic Dynamic Matrix Control for Driven Pendulum System", International Journal of Electronics and Communication Engineering, pp. 363-370, Vol. 5, 2012.
- [9] Farmanbordar. A," Stabilizing a Driven Pendulum Using DLQR Control", IEEE International Conference on Modelling Symposium (AMS), pp. 123 - 126, May 2011.
- (AMS), pp. 123 126, May 2011.
 [10] Mohammad bagheri, A." A New Approach to Control a Driven Pendulum with PID Method ", IEEE International Conference on Computer Modelling and Simulation, pp. 207 211, 2011.
- [11] Kizmaz.H, Aksoy. S, Muhurcu.A, "Sliding mode control of suspended pendulum", IEEE International Conference on Modern Electric Power Systems (MEPS),pp.1-7, 2010.
- [12] MRRahimi Khoygani, RGhasemi, DSanaei, "Design Controller for a Class of Nonlinear Pendulum Dynamical System", IAES International Journal of Artificial Intelligence (IJ-AI), Vol. 2, No. 4, December 2013, pp. 159~168.

Reza Ghasemi was born in Tehran, Iran in 1979. He received his B.Sc. degrees in Electrical engineering from Semnan University in 2000 and M.Sc. degrees and Ph.D. in control engineering from Amirkabir University of Technology, Tehran, Iran, in 2004 and 2009, respectively. His research interests include large-Scale Systems, Adaptive Control, Robust Control, Nonlinear Control, and Intelligent Systems.Dr. Reza Ghasemi joined the Department of Electrical Engineering, Damavand Branch, Islamic AzadUniversity, Damavand, Iran, where he is currently an Assistant Professor of electrical engineering (e-mail: Rezaghasemi@Damavandiau.ac.ir).

Mohammad Reza Rahimi Khoygani was born in Isfahan, Iran in 1988. He received his B.Sc. degrees in Electrical Power Engineering from the Islamic Azad University KhomeiniShahr in 2012, Isfahan, Iran. And in 2012, he is a M.Sc. student in Department of Electrical Engineering, Damavand Branch, Islamic Azad University, Damavand, Iran. His research interests include Nonlinear Control, Fuzzy control, Optimal control and Robust control systems (e-mail: Mohamad.reza.rahimi67@gmail.com).