# Optimal Economic Restructuring Aimed at an Increase in GDP Constrained by a Decrease in Energy Consumption and CO<sub>2</sub> Emissions

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Abstract—The objective of this paper is finding the way of economic restructuring - that is, change in the shares of sectoral gross outputs - resulting in the maximum possible increase in the gross domestic product (GDP) combined with decreases in energy consumption and CO<sub>2</sub> emissions. It uses an input-output model for the GDP and factorial models for the energy consumption and CO<sub>2</sub> emissions to determine the projection of the gradient of GDP, and the antigradients of the energy consumption and CO2 emissions, respectively, on a subspace formed by the structure-related variables. Since the gradient (antigradient) provides a direction of the steepest increase (decrease) of the objective function, and their projections retain this property for the functions' limitation to the subspace, each of the three directional vectors solves a particular problem of optimal structural change. In the next step, a type of factor analysis is applied to find a convex combination of the projected gradient and antigradients having maximal possible positive correlation with each of the three. This convex combination provides the desired direction of the structural change. The national economy of the United States is used as an example of applications.

**Keywords**—Economic restructuring, Input-Output analysis, Divisia index, Factorial decomposition, E3 models.

# I. STATEMENT OF THE PROBLEM

NONVENTIONAL wisdom and literature sources state that the goals of economic growth and preserving the Earth's atmosphere and natural resources are conflicting with each other. Economic development has typically been at odds with energy saving and environmental protection as they pursue different, often mutually exclusive, goals. On the one hand, it is crucial to meet the basic needs of people living in poverty. On the other hand, natural resources depletion, environmental degradation, global warming, and climate change, which economic development partially stimulates, will heavily impact the national well-being. The imbalance between emissions of greenhouse gases and their absorption leads to a continual increase of their atmospheric concentration and contributes to a warming of the planet via the greenhouse effect. The latest figures state that if the rise in global average temperature exceeds some level, estimated between 2<sup>o</sup>C and 4°C, the losses in the world income may reach 0.2% to 2% and catastrophic global consequences may be imminent. With about 4.1 billion metric tons of carbonadded yearly to the atmosphere directly through human activity, CO2 emissions

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are the important factor that is within our power to curb according to [2], [4].

Tackling the issue of rising greenhouse gas emissions necessitates a reduction in energy consumption in residential and industrial sectors, development of more environmentallyfriendly means of energy production, more efficient technology for industrial and non-industrial transportation, and agriculture as well as advocacy for energysaving habits and behaviors. Special attention should also be paid to environmental policy and legislation. Because CO<sub>2</sub> emissions are man-made to a large extent, environmental policy should focus on doing whatever is necessary to curb them. On the energy side of the problem, we notice that the processes of energy production and consumption are the main sources of CO2 emissions. Also, some of them, like the hydraulic fracturing, undermine the living conditions and have a strong negative impact on the biosphere.

Approaches are known in the literature (see, for example, Lozano and Gutierez [7]) that suggest partial solutions to the problem by focusing on just one objective: GDP, CO<sub>2</sub> emissions, or energy consumption, respectively. In contravention to them, the objective of this research is to resolve all three problems simultaneously. It will be shown that it is possible to achieve this goal through specially-designed economic restructuring of the national economy.

Firstly, we develop mathematical models that suggest particular directions of optimal economic restructuring for gross domestic product (GDP), energy consumption, and CO<sub>2</sub> emissions by using a projected gradient or antigradients respectively, [1]. Secondly, we use a type of factor analysis to construct a directional vector of economic restructuring having maximal positive correlations with each of them. This vector solves the problem, namely, that if the economy is being restructured in its direction, then GDP is increasing while energy consumption and CO<sub>2</sub> emissions are decreasing.

In this paper, we use the fact that the gradient (antigradient) vector points out the direction of steepest increase (decrease) in the function value and its projection on a subspace spanned over the variables of interest retains this property for the function's limitation to the subspace. The proof of the last statement may be found, for example, in Maital and Vaninsky [8]. To find the gradient vector for GDP, we use Leontief's input –output model [6]. For the energy consumption and CO<sub>2</sub> emissions, factorial models similar to the Kaya-identity, Kaya [5] are developed. Projected gradient (antigradient) is found

based on the results of Meerovich [10]), Vaninsky and Meerovich [18], and Vaninsky [13]-[17].

At the next stage, we use the factor analysis approach [11] to find a directional vector of optimal economic restructuring. This vector is constructed as a convex combination of the normalized projected gradient and antigradient vectors obtained at the previous step having maximal positive correlations with each of them. This vector solves the problem: Economic restructuring following its direction results in a maximum possible increase in GDP combined with the decreases in energy consumption and  $\mathrm{CO}_2$  emissions. One of the advantages of the suggested approach is the very limited amount of statistical information needed for the calculations. As an example of applications, we consider the economic restructuring of the U.S. economy of 2009.

The paper uses statistical information of the World Input-Output Database (WIOD) [12]. This research paves the way for the subsequent investigation comprising the entirety of leading national and regional economies aimed at finding the way of international cooperation in economic restructuring intended to combine economic growth, energy conservation, and preserving the atmosphere.

The paper is organized as follows. Section II describes the mathematical model, Section III provides an example of applications and discusses the obtained results. This identity is based on the following factorial decomposition:

# II. MATHEMATICAL MODEL

In this paper, we measure economic growth as the increase in the gross domestic product (GDP) that is what the people of a given country can use to satisfy their needs and wants. The GDP is calculated as the total of its sectoral components. To find the gradient of the GDP and its projection, we use an input-output model developed by Leontief [6] transformed into a structured form. A conventional input-output model relates gross output, intermediate inputs, and final product in a single matrix equation. This equation allows us to estimate the total requirements in the gross output needed to satisfy a desired level of the final product. A matrix equation of the model is this:

$$X = AX + Y, (1)$$

In this paper, we transform the conventional input-output model into a specially-structured form whereby the only quantitative indicator is total gross output. All other elements of the model are relative indicators such as shares of sectoral gross outputs in total or shares of sectoral final product in the corresponding gross output. The suggested approach is based on a mathematical model developed in Vaninsky [13] that considers GDP as an objective function with the structured input-output model as a set of constraints imposed on its arguments. In that publication, it was shown that the projected gradient of GDP is a multiple of a function of the structural arguments and that the components of the projected gradient, corresponding to the sectoral structure of the gross output, are proportional to the deviations of the corresponding final-

product components from the average value. This result is crucial for this paper's objective because it enables us to find the gross-output components of the projected gradient without knowledge of the technological matrix. This is the basis behind the computational simplicity of the suggested approach because the technological matrix may be obviated.

Following Ghosh [3], we transform the model (1) to a structured form. To do that, we divide each row of the matrix (1) by Xi, the gross output of i-sector, correspondingly. We get

$$1 = \sum_{i=1}^{n} C_{ij} + U_{i}, i = 1,...,n,$$
 (2)

where Cij = (AijXj)/Xi is a share of gross output of i-sector obtained from the *j*-sector for technological use, Ui=Yi/Xi is a share of *i*-final product in i-gross output, and n is the number of sectors in the economy. Each equation in (2) corresponds to a particular sector. The sectors are related through variables Di, the shares of i-gross output in total:

$$Di = Xi / X, \tag{3}$$

where *X* is total gross output. As follows from the definition,

$$\sum_{i=1}^{n} D_i = 1. \tag{4}$$

An input-output model, given by (2) through (4), is referred to below as a structured input-output model. In this paper, we follow Vaninsky[13] and append the structured input-output model (2) through (4) with an objective function. The input-output model it becomes a set of constraints imposed on the arguments of the objective function. Since the GDP is a sum of the sectoral components of the vector  $\mathbf{Y}$  in the (1), it may be written as

$$Y = \sum_{i=1}^{n} Y_i = \sum_{i=1}^{n} X_i U_i = \sum_{i=1}^{n} (XD_i) U_i = X \sum_{i=1}^{n} D_i U_i,$$
 (5)

where Y is GDP, equal to the sum of the components of vector Y. The components of the gradient  $\nabla Y$  of the objective function Y are as follows:

$$\frac{\partial Y}{\partial X} = \sum_{i=1}^{n} D_{i} U_{i}, \quad \frac{\partial Y}{\partial D_{i}} = X U_{i}, \quad \frac{\partial Y}{\partial U_{i}} = X D_{i}, \quad \frac{\partial Y}{\partial C_{ij}} = 0 \quad , (6)$$

seeVaninsky [13], [17] for detail.

It is known that the gradient of the limitation of a function to a surface is a projection of the gradient of the function on a tangent subspace, see Maital and Vaninsky [9] for detail. In the problem defined by (2) through (6) we project gradient (5) on the hyperplane defined by (2) and (4) as was proposed in Vaninsky and Meerovich [18] and Vaninsky [14], [15]; details may be found in Maital and Vaninsky[9].

As shown in Vaninsky[17], the projected gradient of the objective function (5) is

$$Proj_{H}\nabla Y = X(U_{1} - \overline{U}, U_{2} - \overline{U}, ..., U_{n} - \overline{U}, \\ -\frac{D_{1}}{n+1}, ..., -\frac{D_{1}}{n+1}, -\frac{D_{2}}{n+1}, ..., -\frac{D_{2}}{n+1}, ..., -\frac{D_{n}}{n+1}, \\ ... -\frac{D_{n}}{n+1}, \frac{nD_{1}}{n+1}, ..., \frac{nD_{n}}{n+1}, 0)$$
(7)

where  $\nabla Y$  is a gradient of function Y, H is a hyperplane defined by (2) and (4),  $Proj_H \nabla Y$  is a projection of  $\nabla Y$  on H, and  $\overline{U} = (U_1 + \ldots + U_n)/n$  stands for the average value of the variables  $U_i$ . The first n components of the projected gradient correspond to the variables  $D_i$  - the shares of i-gross output in total. We compute a projection of the gradient (7) on the subspace spanned over the variables  $D_i$  and get

$$\frac{\partial Y}{\partial D_i} = X_0 (U_i - \bar{U}) \tag{8}$$

with all other components equal to zero. For a directional vector, the factor  $X_0$  may be ignored, and we get

$$\boldsymbol{d}_{GDPi} = (U_i - \bar{U}), \tag{9}$$

where  $d_{GDP}$  is the directional vector of the GDP-maximizing restructuring. This formula shows that in the direction of the projected gradient, the impact of structural variable  $D_i$  on the final product is proportional to the deviation of the corresponding share of the i-final product in the i-gross output from the average value.

In the next step, we find vectors of economic restructuring optimal for the decrease in the  $CO_2$  emissions and energy consumption, respectively. Consider the  $CO_2$  emissions first. A factorial model of the  $CO_2$  emissions is

$$C = \sum C_i = XC_x = \sum X_i C_{xi} = XC_x \sum \left( \frac{X_i}{X} \frac{C_{xi}}{C_x} \right) = XC_x \sum D_i R_{ci}$$
 (10)

where C and  $C_i$  are total and sectoral CO<sub>2</sub> emissions, X and  $X_i$  are total and sectoral gross products,  $C_x$  and  $C_{xi}$  are the carbon intensity of the total and sectoral gross products, respectively, and  $R_{ci}$  stands for the relative carbon intensity of the gross output (the ratio of the  $C_{xi}$  to  $C_x$ .)

Since we are interested in the optimization of the economic structure, we consider the (10) at the base value of  $X = X_0$  and divide both its sides by  $C_0 = X_0 \cdot C_x$ . We get

$$\hat{C} = C/C_0 = \Sigma D_i R_{ci} \,, \tag{11}$$

where  $\hat{C}$  is  $CO_2$  emissions in terms of the base year. Equation (11) is a factorial model of the  $CO_2$  emissions with the factors Di interconnected by (4). A gradient of the function  $\hat{C}$  is

$$\nabla \hat{C} = \langle R_{CI}, R_{C2}, ..., R_{Cn} \rangle , \qquad (12)$$

and, as shown in Meerovoch [10], Vaninsky and Meerovich [18], and Vaninsky [15], the projected gradient on the hyperplane defined by (4) is

$$Proj_{D}\nabla\hat{C} = \langle R_{CI} - \overline{R}_{C}, R_{C2} - \overline{R}_{C}, \dots, R_{Cn} - \overline{R}_{C} \rangle,$$
 (13)

where  $\overline{R}_c = (R_{cI} + R_{c2} + ... + R_{cn})/n$  stands for the average value of the relative carbon intensities. Since our objective is to decrease the CO<sub>2</sub> emissions, the optimal structural change corresponds to the projected antigradient, that is

$$d_C = -Proj_D \nabla \hat{C} = -\langle R_{CI} - \overline{R}_C, R_{C2} - \overline{R}_C, \dots, R_{Cn} - \overline{R}_C \rangle . \quad (14)$$

For the same reasons, the projected antigradient of the energy consumption is

$$d_E = -Proj_D \nabla E = -\langle R_{EI} - \overline{R}_E, R_{E2} - \overline{R}_E, \dots, R_{En} - \overline{R}_E \rangle , \quad (15)$$

where  $R_{Ei}$  and  $\overline{R}_{E}$  stand for the sectoral relative and average relative energy intensity of the gross output respectively.

In what follows, we use formulas of the projected gradient (9) and antigradients (14) and (15) to find a directional vector that has maximum positive correlations with each of them. To find this vector, we use the technique of factor analysis, see[11]. The optimization problem is this:

Maximize
$$Corr(d, d_{GDP})^{2} + Corr(d, d_{E})^{2} + Corr(d, d_{CO2})^{2}$$
Subject to
$$d = \alpha_{1} \cdot d_{GDP} + \alpha_{2} \cdot d_{E} + \alpha_{3} \cdot d_{C}$$

$$\alpha_{1}, \alpha_{2}, \alpha_{3} \ge 0$$

$$\alpha_{1} + \alpha_{1} + \alpha_{1} = 1$$
by changing  $\alpha_{1}, \alpha_{2}, \alpha_{3}$ , (16)

where Corr() stands for the correlation coefficient.

Solution to this problem is a convex combination of the vectors  $d_{GDP}$ ,  $d_E$ , and  $d_C$ that maximizes a sum of squares of its correlation coefficients with the vectors of projected gradient or antigradients respectively (referred to in the statistical literature as the coefficients of determination). To solve the problem, we developed a computational procedure using the Excel's Solver.

The obtained directional vector of the structural change serves the three goals simultaneously. It may be noted that in some special cases such vector does not exist, for example, if the three vectors are collinear or coplanar with an angle of 120<sup>0</sup> between each two of them. However, such situations are very unlikely in practice where typical dimensions of the vectors are in the range from 15 to 500 and may be ignored.

## III. EXAMPLE OF APPLICATIONS AND DISCUSSION

In this section we use data provided by the World Input-Output Database (WIOD) to find the optimal structural change in the U.S. economy of 2009which affords the latest data available at the time of this paper's preparation. The input-

output methodology underlying the WIOD statistical information may be found in Timmer[12].

The U.S. economy is considered as a collection of 34 sectors shown in Table I. Table II presents the shares of sectoral gross outputs, energy, CO<sub>2</sub> emissions in total (columns 2, 4, and 5, respectively), shares of final product in the sectoral gross output (column 3), and the relative energy and CO<sub>2</sub> gross output intensities (columns 6 and 7, respectively). The sector Private Households with Employed Persons, the second smallest by the gross output, was excluded because it had zero energy consumption and CO<sub>2</sub> emissions. Its gross output was added to the sector Public Administration and Defense; Compulsory Social Security which is the largest one. Sectoral amounts of energy consumption and CO2 emissions were calculated by using data of the intermediate output because the data related the sectoral gross outputs were not available to the author. Columns 2 and 3 of the Table II are referred to as  $D_i$  and  $U_i$  in formulas (5) through (8), (10) to (11) etc. respectively. Columns 4 and 5 of the Table II are the sectoral shares in energy consumption and CO2 emissions respectively. They were calculated as  $E_i/E$  and  $C_i/C$ , respectively, as shown by (10) for CO<sub>2</sub> emissions. Columns 6 and 7 of the Table II are energy and CO2 intensities of the sectoral gross output with respect to the total gross output intensities. As follows from (10) they are equal to  $R_{ei}=E_{xi}/E_x$ and  $R_{ci} = C_{xi}/C_x$ , respectively, and may be calculated as  $R_{Ei} =$  $(E_i/E)/(X_i/X)$  and  $R_{ci}=(C_i/C)/(X_i/X)$ , correspondingly, as shown in Table II.

Table III shows the GDP projected gradient and the energy consumption and CO2 emissions projected antigradients. They were calculated by using (9), (15), and (14) respectively by subtracting the corresponding average value from the sectoral values. The gradient and antigradient vectors were normalized as shown in Table IV: The square roots of the sum of squares of the coordinates of each vector were made equal to one, as suitable for the factor analysis, see [11]. The result is shown in columns 2 through 4 of the Table IV. Column 5 of Table IV presents the vector of optimal structure change obtained as a convex combination of the normalized gradient and antigradient vectors that maximizes the sum of squares of correlation coefficients. Recall that the square of the correlationcoefficient is usually referred to as determination coefficient; it represents a part of the variance that may be explained by the correlate. A normalized vector of optimal structural change is shown in column 6.

The optimization procedure was similar to that used in the Factor Analysis, [11]. The computation was performed by using the Excel's Solver.

TABLE I SECTORS INCLUDED IN THE MODEL

| SECTORS INCLUDED IN THE MODEL  Sector   | Abbreviation |
|---|--------------|
| (1)   | (2)          |
| Agriculture, Hunting, Forestry and Fishing  | AHFF         |
| Mining and Quarrying  | MO           |
| Food, Beverages and Tobacco   | FBT          |
| Textiles and Textile Products   | TTP          |
| Leather, Leather and Footwear   | LLF          |
| Wood and Products of Wood and Cork  | WPWC         |
| Pulp, Paper, Paper, Printing and Publishing   | PPPPP        |
| Coke, Refined Petroleum and Nuclear Fuel  | CRPNF        |
| Chemicals and Chemical Products   | CCP          |
| Rubber and Plastics   | RP           |
| Other Non-Metallic Mineral  | ONMM         |
| Basic Metals and Fabricated Metal   | BMFM         |
| Machinery, Nec  | MN           |
| Electrical and Optical Equipment  | EOE          |
| Transport Equipment   | TE           |
| Manufacturing, Nec; Recycling   | MNR          |
| Electricity, Gas and Water Supply   | EGWS         |
| Construction  | C            |
| Sale, Maintenance and Repair of Motor Vehicles and                                    | SMRMRF       |
| Motorcycles; Retail Sale of Fuel<br>Wholesale Trade and Commission Trade, Except of   |              |
| Motor Vehicles and Motorcycles  | WTCT         |
| Retail Trade, Except of Motor Vehicles and Motorcycles;                               | RT           |
| Repair of Household Goods   |              |
| Hotels and Restaurants  | HR           |
| Inland Transport  | IT           |
| Water Transport   | WT           |
| Air Transport   | AT           |
| Other Supporting and Auxiliary Transport Activities;<br>Activities of Travel Agencies | OSAT         |
| Post and Telecommunications   | PT           |
| Financial Intermediation  | FI           |
| Real Estate Activities  | REA          |
| Renting of M&Eq and Other Business Activities   | ROBA         |
| Public Admin and Defense; Compulsory Social Security                                  | PAD          |
| Education   | ED           |
| Health and Social Work  | HSW          |
| Other Community, Social and Personal Services   | OCSPS        |

Notes.

<sup>a</sup>Nec stands for Not elsewhere classified

# International Journal of Engineering, Mathematical and Physical Sciences

ISSN: 2517-9934 Vol:8, No:6, 2014

TABLE II SHARES IN TOTAL AND RELATIVE INTENSITIES

| -      | Shai   | RES IN TOTA                   | AL AND REL          | ATIVE INTE                   | ENSITIES       |                |
|--------|--------|-------------------------------|---------------------|------------------------------|----------------|----------------|
| Sector | Gross  | Final<br>Product <sup>a</sup> | Energy <sup>b</sup> | CO <sub>2</sub> <sup>b</sup> | Relative       | Relative       |
|        | Output |                               |                     |                              | energy         | $CO_2$         |
|        | Guipui | 1104401                       |                     |                              | intensity      | intensity      |
| (1)    | (2)    | (3)                           | (4)                 | (5)                          | (6)= $(4)/(2)$ | (7)= $(5)/(2)$ |
| AHFF   | 0.0138 | 0.1948                        | 0.0087              | 0.0120                       | 0.6324         | 0.8683         |
| MQ     | 0.0141 | 0.2882                        | 0.0153              | 0.0265                       | 1.0851         | 1.8820         |
| FBT    | 0.0313 | 0.5654                        | 0.0110              | 0.0145                       | 0.3525         | 0.4642         |
| TTP    | 0.0024 | 0.2318                        | 0.0021              | 0.0021                       | 0.8757         | 0.8770         |
| LLF    | 0.0001 | 0.1204                        | 0.0000              | 0.0000                       | 0.2562         | 0.3307         |
| WPWC   | 0.0032 | 0.0494                        | 0.0046              | 0.0035                       | 1.4595         | 1.0930         |
| PPPPP  | 0.0172 | 0.3027                        | 0.0185              | 0.0146                       | 1.0764         | 0.8520         |
| CRPNF  | 0.0191 | 0.3211                        | 0.3170              | 0.0445                       | 16.6005        | 2.3315         |
| CCP    | 0.0242 | 0.2638                        | 0.0545              | 0.0319                       | 2.2498         | 1.3169         |
| RP     | 0.0068 | 0.1095                        | 0.0009              | 0.0012                       | 0.1368         | 0.1746         |
| ONMM   | 0.0037 | 0.0655                        | 0.0084              | 0.0262                       | 2.2641         | 7.0978         |
| BMFM   | 0.0193 | 0.0013                        | 0.0170              | 0.0241                       | 0.8792         | 1.2489         |
| MN     | 0.0112 | 0.3628                        | 0.0032              | 0.0039                       | 0.2820         | 0.3495         |
| EOE    | 0.0195 | 0.2874                        | 0.0022              | 0.0026                       | 0.1149         | 0.1318         |
| TE     | 0.0238 | 0.3856                        | 0.0042              | 0.0048                       | 0.1765         | 0.2014         |
| MNR    | 0.0056 | 0.4917                        | 0.0006              | 0.0009                       | 0.1002         | 0.1588         |
| EGWS   | 0.0156 | 0.5117                        | 0.3170              | 0.4855                       | 20.2874        | 31.0718        |
| C      | 0.0466 | 0.8308                        | 0.0159              | 0.0100                       | 0.3420         | 0.2143         |
| SMRMRF | 0.0085 | 0.8131                        | 0.0013              | 0.0014                       | 0.1488         | 0.1657         |
| WTCT   | 0.0407 | 0.4836                        | 0.0051              | 0.0075                       | 0.1250         | 0.1834         |
| RT     | 0.0477 | 0.8638                        | 0.0135              | 0.0187                       | 0.2829         | 0.3920         |
| HR     | 0.0307 | 0.7830                        | 0.0139              | 0.0148                       | 0.4521         | 0.4832         |
| IT     | 0.0137 | 0.3198                        | 0.0242              | 0.0459                       | 1.7602         | 3.3395         |
| WT     | 0.0014 | 0.6473                        | 0.0065              | 0.0134                       | 4.7953         | 9.8579         |
| AT     | 0.0054 | 0.5657                        | 0.0186              | 0.0372                       | 3.4684         | 6.9381         |
| OSAT   | 0.0079 | 0.0926                        | 0.0071              | 0.0134                       | 0.8957         | 1.6881         |
| PT     | 0.0249 | 0.4173                        | 0.0058              | 0.0075                       | 0.2324         | 0.3006         |
| FI     | 0.0979 | 0.3386                        | 0.0061              | 0.0073                       | 0.0624         | 0.0744         |
| REA    | 0.0928 | 0.7063                        | 0.0056              | 0.0023                       | 0.0605         | 0.0248         |
| ROBA   | 0.1157 | 0.2019                        | 0.0171              | 0.0247                       | 0.1479         | 0.2139         |
| PAD    | 0.1195 | 0.9494                        | 0.0455              | 0.0608                       | 0.3811         | 0.5084         |
| ED     | 0.0090 | 0.9015                        | 0.0049              | 0.0037                       | 0.5482         | 0.4049         |
| HSW    | 0.0680 | 0.9737                        | 0.0151              | 0.0207                       | 0.2213         | 0.3049         |
| OCSPS  | 0.0386 | 0.5714                        | 0.0086              | 0.0119                       | 0.2225         | 0.3089         |
|        |        | 0.4416                        |                     |                              | 1.0500         | 2.2210         |

Average

Notes

<sup>a</sup> Share in the sectoral gross output.
<sup>b</sup> Calculated by using intermediate output.

0.4416

 $TABLE\ III$   $G\underline{DP\ Gradient,\ and\ Energy\ and\ CO_2\ Antigradients}$ 

| Sector            | $GDP^a$ | Energy <sup>b</sup> | $CO_2^b$ |
|-------------------|---------|---------------------|----------|
| (1)               | (2)     | (3)                 | (4)      |
| AHFF              | -0.2467 | 1.2198              | 1.3627   |
| MQ                | -0.1534 | 0.7671              | 0.3490   |
| FBT               | 0.1238  | 1.4997              | 1.7668   |
| TTP               | -0.2098 | 0.9766              | 1.3540   |
| LLF               | -0.3211 | 1.5960              | 1.9002   |
| WPWC              | -0.3921 | 0.3928              | 1.1380   |
| PPPPP             | -0.1389 | 0.7758              | 1.3790   |
| CRPNF             | -0.1204 | -14.7482            | -0.1005  |
| CCP               | -0.1777 | -0.3976             | 0.9141   |
| RP                | -0.3321 | 1.7154              | 2.0563   |
| ONMM              | -0.3761 | -0.4119             | -4.8669  |
| BMFM              | -0.4402 | 0.9730              | 0.9821   |
| MN                | -0.0787 | 1.5702              | 1.8815   |
| EOE               | -0.1541 | 1.7373              | 2.0992   |
| TE                | -0.0560 | 1.6758              | 2.0295   |
| MNR               | 0.0501  | 1.7521              | 2.0722   |
| EGWS              | 0.0701  | -18.4351            | -28.8408 |
| C                 | 0.3892  | 1.5102              | 2.0167   |
| SMRMRF            | 0.3716  | 1.7035              | 2.0652   |
| WTCT              | 0.0420  | 1.7273              | 2.0476   |
| RT                | 0.4222  | 1.5694              | 1.8390   |
| HR                | 0.3415  | 1.4001              | 1.7478   |
| IT                | -0.1217 | 0.0920              | -1.1085  |
| WT                | 0.2058  | -2.9431             | -7.6269  |
| AT                | 0.1241  | -1.6162             | -4.7071  |
| OSAT              | -0.3490 | 0.9566              | 0.5428   |
| PT                | -0.0242 | 1.6198              | 1.9304   |
| FI                | -0.1030 | 1.7898              | 2.1565   |
| REA               | 0.2648  | 1.7917              | 2.2061   |
| ROBA              | -0.2397 | 1.7044              | 2.0171   |
| PAD               | 0.5078  | 1.4711              | 1.7226   |
| ED                | 0.4599  | 1.3040              | 1.8260   |
| HSW               | 0.5321  | 1.6309              | 1.9261   |
| OCSPS             | 0.1298  | 1.6297              | 1.9221   |
| Norm <sup>c</sup> | 1.6251  | 25.0487             | 31.9914  |

# Notes

1.8522

2.2310

- <sup>b</sup> Opposite of the sectoral energy (CO<sub>2</sub>) intensity minus average value.

  Square root of the sum of squares of the components.

TABLE IV

NORMALIZED GDP GRADIENT, ENERGY AND CO<sub>2</sub> ANTIGRADIENTS, AND

OPTIMAL PRETRUCTURING VICTOR<sup>A</sup>

|        | OPTIMAL RESTRUCTURING VECTOR <sup>A</sup> |         |         |         |                        |
|--------|---|---------|---------|---------|------------------------|
| Sector | GDP                                       | Energy  | $CO_2$  | Optimal | Optimal,<br>normalized |
| (1)    | (2)                                       | (3)     | (4)     | (5)     | (6)                    |
| AHFF   | -0.1518                                   | 0.0487  | 0.0426  | 0.0408  | 0.0441                 |
| MQ     | -0.0944                                   | 0.0306  | 0.0109  | 0.0179  | 0.0194                 |
| FBT    | 0.0762                                    | 0.0599  | 0.0552  | 0.0580  | 0.0628                 |
| TTP    | -0.1291                                   | 0.0390  | 0.0423  | 0.0364  | 0.0394                 |
| LLF    | -0.1976                                   | 0.0637  | 0.0594  | 0.0551  | 0.0597                 |
| WPWC   | -0.2413                                   | 0.0157  | 0.0356  | 0.0190  | 0.0206                 |
| PPPPP  | -0.0854                                   | 0.0310  | 0.0431  | 0.0340  | 0.0368                 |
| CRPNF  | -0.0741                                   | -0.5888 | -0.0031 | -0.2907 | -0.3145                |
| CCP    | -0.1094                                   | -0.0159 | 0.0286  | 0.0035  | 0.0038                 |
| RP     | -0.2044                                   | 0.0685  | 0.0643  | 0.0597  | 0.0646                 |
| ONMM   | -0.2314                                   | -0.0164 | -0.1521 | -0.0879 | -0.0951                |
| BMFM   | -0.2709                                   | 0.0388  | 0.0307  | 0.0272  | 0.0294                 |
| MN     | -0.0485                                   | 0.0627  | 0.0588  | 0.0580  | 0.0628                 |
| EOE    | -0.0948                                   | 0.0694  | 0.0656  | 0.0635  | 0.0687                 |
| TE     | -0.0345                                   | 0.0669  | 0.0634  | 0.0627  | 0.0679                 |
| MNR    | 0.0308                                    | 0.0699  | 0.0648  | 0.0665  | 0.0719                 |
| EGWS   | 0.0431                                    | -0.7360 | -0.9015 | -0.7973 | -0.8629                |
| C      | 0.2395                                    | 0.0603  | 0.0630  | 0.0661  | 0.0715                 |
| SMRMRF | 0.2286                                    | 0.0680  | 0.0646  | 0.0703  | 0.0761                 |
| WTCT   | 0.0259                                    | 0.0690  | 0.0640  | 0.0655  | 0.0709                 |
| RT     | 0.2598                                    | 0.0627  | 0.0575  | 0.0650  | 0.0704                 |
| HR     | 0.2101                                    | 0.0559  | 0.0546  | 0.0591  | 0.0640                 |
| IT     | -0.0749                                   | 0.0037  | -0.0347 | -0.0169 | -0.0183                |
| WT     | 0.1266                                    | -0.1175 | -0.2384 | -0.1704 | -0.1844                |
| AT     | 0.0764                                    | -0.0645 | -0.1471 | -0.1013 | -0.1096                |
| OSAT   | -0.2147                                   | 0.0382  | 0.0170  | 0.0216  | 0.0234                 |
| PT     | -0.0149                                   | 0.0647  | 0.0603  | 0.0606  | 0.0656                 |
| FI     | -0.0634                                   | 0.0715  | 0.0674  | 0.0661  | 0.0716                 |
| REA    | 0.1629                                    | 0.0715  | 0.0690  | 0.0725  | 0.0785                 |
| ROBA   | -0.1475                                   | 0.0680  | 0.0631  | 0.0603  | 0.0652                 |
| PAD    | 0.3125                                    | 0.0587  | 0.0538  | 0.0626  | 0.0678                 |
| ED     | 0.2830                                    | 0.0521  | 0.0571  | 0.0602  | 0.0652                 |
| HSW    | 0.3275                                    | 0.0651  | 0.0602  | 0.0692  | 0.0749                 |
| OCSPS  | 0.0799                                    | 0.0651  | 0.0601  | 0.0630  | 0.0682                 |
| Notes  |   |         |         |         | -                      |

Notes

In our computations, the weight coefficients were as follows:  $\alpha_{GDP} = 0.0248$ ,  $\alpha_{Energy} = 0.4879$ , and  $\alpha_{CO2} = 0.4873$ . As required by the convex linear combination, all of them are non-negative and sum up to one. The values of the weight coefficients reveal that the vector of optimal change tends to serve more the problem of energy conservation and atmosphere protection than the objective of economic growth. This might not be the case if a different economy was analyzed. The key sectors of economic restructuring, as shown by the components of the normalized vector of optimal structural change, were as follows. The main sectors to be expanded (those having the component's value above 0.07 in our case) were REA (0.0785), SMRMRF (0.0761), HSW (0.0749), MNR (0.0719), FI (0.0716), C (0.0715), WTCT (0.0709), and RT (0.0704). Since the differences among the components do not exceed 10%, they may be considered as the candidates for expansion in any appropriate combination.

Only 6 sectors had negative components: EGWS (-0.8629), CRPNF (-0.3145), WT(-0.1844), AT (-0.1096), ONMM (-0.0951), and IT (-0.0183). These sectors should be shrunken and their shares in the gross output should be transferred to the expanded sectors. As follows from the numerical values of the components, the impacts of these sectors are quite different. The Electricity, Gas and Water Supply sector is the most desirable candidate for contraction.

Since that sector's contraction is usually undesirable, more detailed analysis may be required for finding the subsectors having the least negative impact on the economy. It may be done, for example, by repeating the above computations with key sectors subject to expansion, and all other sectors aggregated to one sector. The new vector of optimal structural change will provide higher resolution of the previously obtained big picture of economic restructuring.

#### IV. CONCLUSIONS

This paper suggests an approach to finding structural change in a national or regional economy, leading to increase in the GDP combined with a decrease in energy consumption and CO<sub>2</sub> emissions. The input-output model in the structured form is used to find the projected gradient of the GDP and factorial models are developed for finding the projected antigradients of the energy consumption and CO2 emissions respectively. A kind of factor analysis was used to compute a resulting vector of structural change satisfying all three goals. The U.S. economy of 2009 was used as an example. The key sectors to be subject to expansion or contraction were determined. The next step of the application of the suggested approach is the detailing of the proposed recommendations on economic restructuring by expansion of the key sectors into subsectors, while contracting the remaining sectors to one aggregated sector. The obtained results are aimed to serve as a basis for economic policy decision-making aimed at serving the goals of economic growth, energy saving, and atmospheric preservation.

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<sup>&</sup>lt;sup>a</sup> Divided by the vector's norm.

# International Journal of Engineering, Mathematical and Physical Sciences

ISSN: 2517-9934 Vol:8, No:6, 2014

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