

Applying Sequential Pattern Mining to Generate Block for Scheduling Problems

Meng-Hui Chen, Chen-Yu Kao, Chia-Yu Hsu, Pei-Chann Chang

Abstract—The main idea in this paper is using sequential pattern mining to find the information which is helpful for finding high performance solutions. By combining this information, it is defined as blocks. Using the blocks to generate artificial chromosomes (ACs) could improve the structure of solutions. Estimation of Distribution Algorithms (EDAs) is adapted to solve the combinatorial problems. Nevertheless many of these approaches are advantageous for this application, but only some of them are used to enhance the efficiency of application. Generating ACs uses patterns and EDAs could increase the diversity. According to the experimental result, the algorithm which we proposed has a better performance to solve the permutation flow-shop problems.

Keywords—Combinatorial problems, Sequential Pattern Mining, Estimation of Distribution Algorithms, Artificial Chromosomes.

I. INTRODUCTION

TO find databases' patterns are very important operation of data mining. For example, like association rule [1] and sequential pattern mining [2]. Scheduling Problems are kinds of the combinatorial problems. According to the definition of the combinatorial problems, it's belonging to NP-hard problem. To find the solution of an optimization problem is a common challenge in which an algorithm may be trapped in the local optima of the objective function when the complexity is high, and there are several local optima in solution space. Tsai et al. [3] and Chun et al. [4] have proposed the algorithms for global optimization problems. The importance of these methods is in many different areas such as modern engineering design and systems operation. Holland [5] and Goldberg [6] proposed Genetic Algorithm (GA) as a tool based on biological mechanisms and natural selection theory. GA has gained much attention regarding its potential as an optimization technique for combinatorial optimization problems and has been successfully applied in many different areas.

In our earlier research, ACGA had been combined with EDAs using crossover and mutation operators to improve the performance [7]. Main characteristic of ACGA is EDAs alternate with GAs in the evolutionary progress. This research showed that the EDAs can improve solution quality with genetic operators. Some research used other heuristic to solve PFSP, like ant colony optimization (ACO) [8], variable neighborhood search (VNS) [9], local search [10], [11] and

artificial bee colony (ABC) [12].

In order to obtain the better performance, some research attempts to find some useful fragment. Use fragment to generate Artificial Chromosome (AC) with good fitness [13]. Here we called fragment as block. In previous research [14], [15], we often build the probability model to generate blocks. The blocks focus on the better information in each position. So in this paper, the main idea discusses the relation between jobs and jobs.

II. LITERATURE REVIEW

A. Association Rule and Sequential Pattern Mining

Association rule is important in data mining. Association rule is to identify the most important relationships and it is generated by analyzing historical data and using the criteria support and confidence. Support shows that how frequently the items appear in the database. The confidence is stood for the judgment which let the rule become useful.

Agrawal et al. [16] discover "what items are bought together in a transaction" over basket data was introduced. The problem is to find what items are bought together from a unprocessed dataset of items is considered that finding intra-transaction patterns. Sequential pattern mining shows the data represented as sequences. Sequential patterns mean that the correlation between transactions [17]. The association rule doesn't consider the order of items, and it focuses on the correlation of each items. The simple step of association rule is shown in Fig 1.

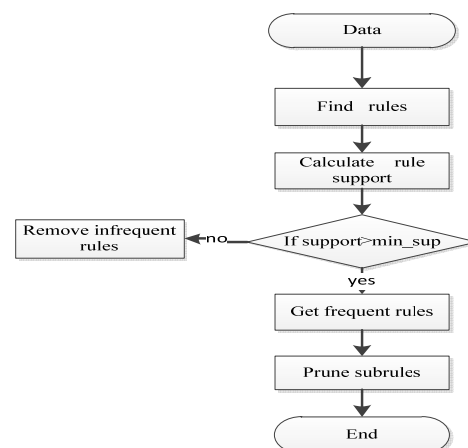


Fig. 1 The flowchart of association rule

B. Estimation of Distribution Algorithms

In EDAs, the problem specific interactions among the

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variables of individuals are taken into consideration. In Evolutionary Computations the interactions are kept implicitly in mind whereas in EDAs the interrelations are expressed explicitly through the joint probability distribution associated with the individuals of variables selected at each generation. The probability distribution is calculated from a database of selected individuals of previous generation. Then sampling of this probability distribution generates an offspring. Neither crossover nor mutation has been applied in EDAs, but the estimation of the joint probability distribution associated with the database containing the selected individuals is not an easy task. The flowchart of EDA is shown in the Fig. 2.

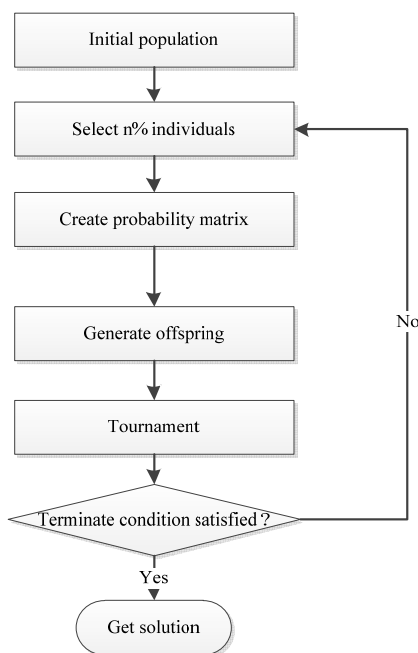


Fig. 2 EDA flowchart

In recently research, some researcher hybrid EDA with other Meta-heuristic algorithms that form a powerful algorithm. In [18], they proposed a new probability model of EDA; capture the variable linkages together with the univariate probabilistic model. A new concept of EDA instead of the most EDAs could use only one statistic information. They combine the new concept of EDA with GA, and join Variable Neighborhood Search (VNS) approach. Their algorithms able get good solution on flow-shop problem.

III. SEQUENTIAL PATTERN MINING TO GENERATE BLOCK

The purposed method in this paper is based on sequential pattern mining and association rule. We proposed an efficient algorithm to solve the combinatorial optimization problems. We called block based on sequential pattern mining as BBSPM. The first stage is getting the excellent solutions from population and store the information from excellent solutions to dominance matrix. The dominance matrix will show the correlation between jobs and jobs. According to the correlation,

we could generate blocks by the criteria support and confidence. Then we use the blocks to generate artificial chromosomes to improve the structure of the solutions. The artificial chromosomes are not always generated by full of blocks, it may combine the blocks and other items. So the other items will be according to the estimation of distribution algorithms to find the strength of each item in each position. The competition between the blocks to make sure to maintain high quality of the blocks in achieves. We developed two types of different combinations mechanism of artificial chromosome. Using these blocks we combination artificial chromosome (AC) with higher advantages which speed up the evolution and convergence. In third stage, we modify the Edge histogram based on sampling algorithm with template (EHBSA) mechanism form EDA [19]. We proposed a rapid convergence approach called modified EHBSA to execute in the later iterations. Modify EHBSA can speed up the convergence and these solutions are close to optimal solution.

The flowchart of BBSPM is represented in Fig. 3. The description of each step is as follow:

Step1. Initial Population

To generate initial solutions randomly.

Step2. Calculate Fitness

Calculate fitness for each solution. In this paper, fitness of the experimental problem is Cmax.

Step3. Update the Dominance Matrix

Collecting the better solutions with higher fitness is to update the dominance matrix. In order to avoiding bad information keep in dominance matrix. We make a mechanism to reset the dominance matrix.

Step4. Using Sequential Pattern Mining to Generate Block

In this step, we set a support to define an useful information and the support means the frequency of each job appeared in each position. If the support was larger than threshold which we set, it would be a candidate block.

Step5. Generate artificial chromosomes

There are two methods to generate artificial chromosomes in this paper. We design two mechanisms to generate artificial chromosomes in order to increasing the diversity and keep the higher quality of fitness.

Step6. Using a Local Search Method to Make the Solutions Evolved and Choose Better Solutions to Next Iterations

We improve the EHBSA of EDA to increase ability of search solutions. Then using tournament selection to choose two solutions and competition between each other, better solution can go to next iteration. Maintain the solutions in population with higher diversity.

The above Step 2 to 6 repeats until meet termination criterion set by user.

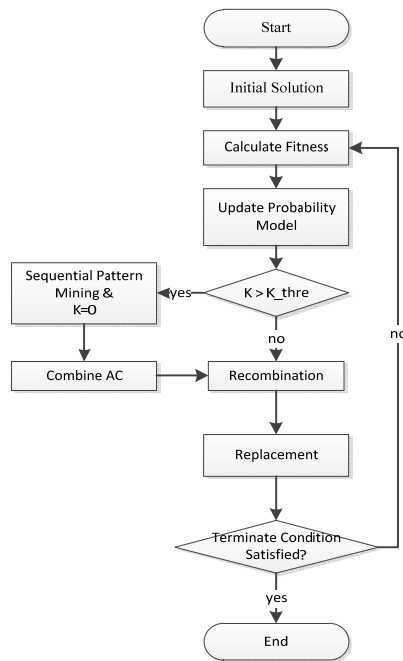


Fig. 3 The architecture of BBSPM

A. Dominance Matrix and Dependency Matrix

Dominance matrix is able to preserve information of high-fitness solutions. Accumulative these jobs positions in each solutions to dominance matrix. Provide useful information for mining blocks and generate AC. In the beginning, calculate fitness for solutions and sort (ascending). Select top N% solutions of population with better fitness value, and store each jobs position in each solution into dominance matrix. In this research, the number of the initial solutions is assigned as 100. We calculate the fitness of all solutions in population; and we select top 30 solutions with higher fitness. Jobs position in each solution is accumulate to dominance matrix. The composition of the matrix is updated by the accumulation of the probability to maintain the competitive approach. The probability matrix is called Accumulative Probability Matrix which is represented as Fig. 4.

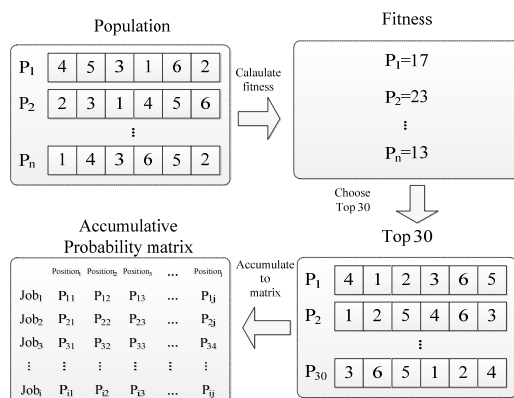


Fig. 4 Accumulative dominance matrix

Accumulate detail is shown in Fig. 4.

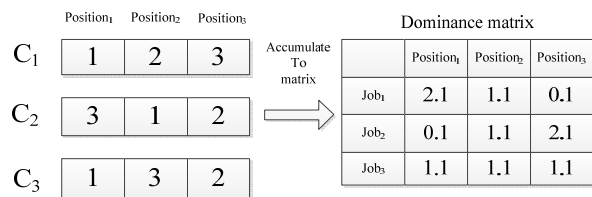


Fig. 5 Accumulate detail of dominance matrix

As Fig. 5, the support of the job1 in position 1 is two times. So by store the correlation between jobs and positions of the solutions which with higher fitness in dominance could shows the strength of each job in each position and the support of each job in each position.

B. Block and Artificial Chromosome Mining Procedure

Each solution has different information in its structure. So if we collect the information of the high-fitness solutions, it would be useful to find high-performance solutions. In this paper, we collect the top n% higher fitness solutions to dominance matrix, and the dominance matrix will show that the times of the each jobs appeared in each position. When the times are bigger, it means that the job has strength in this position. Blocks are design to keep the better information, and combine the blocks to generate artificial chromosomes. Using blocks applied for solving combinational problems has two reasons. One is decreasing the complexity of problems. As shown in Fig. 6, if we could find some information to combine a set of jobs to be grouped together. For example, job 1 with job 8, job 4 with job7, and job10 with job 5, and the total number of feasible solutions will be only 7!. If a longer block is defined, the total number of feasible solutions will be reduced even more abruptly. However, the quality of the blocks will be the key to the block based approach. The other would enhance evolution effect and accelerate the speed of convergence. Because the blocks are combined the better information, it means that the solutions' structure include blocks will cause the schedule order is approach to the order of the optimal solution.

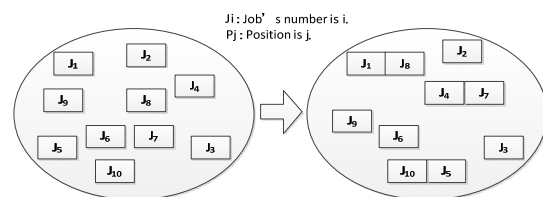


Fig. 6 Complexity reduction

In this paper, the mechanism of generating blocks use sequential pattern mining and dominance matrix. At first, we randomly choose a job within strength in the position according to the dominance matrix, and randomly select two solutions from the top n% fitness solutions. Then find all the support of combining jobs and jobs is higher than the threshold. These all combinations will be the candidate blocks. After weeding out the combinations with the same jobs or positions, the others are the blocks.

Dominance matrix

	Position ₁	Position ₂	Position ₃	Position ₄	Position ₅
J ₁	2.1	1.1	1.1	1.1	0.1
J ₂	1.1	3.1	1.1	0.1	0.1
J ₃	1.1	1.1	2.1	1.1	0.1
J ₄	0.1	0.1	0.1	1.1	4.1
J ₅	1.1	0.1	1.1	2.1	1.1

Find 1-length frequent block

- Support of Job₁ in position₁ = 2.1
- Support of Job₁ in position₂ = 3.1
- Support of Job₁ in position₃ = 2.1
- Support of Job₁ in position₄ = 4.1
- Support of Job₁ in position₅ = 2.1

Find n-len frequent block

- Support of Job₁ in position₅ = 2.1
- Support of Job₂ in position₅ = 0.1

Historical chromosome data

	P ₁	P ₂	P ₃	P ₄	P ₅
C ₁	1	2	3	5	4
C ₂	2	1	5	4	5
C ₃	1	2	5	3	4
C ₄	3	2	1	5	4
C ₅	5	3	2	1	4

Job I is chosen

P₁

J ₁	
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Block length-3

P₁ P₂ ... P₅

J ₁	J ₂	...	J ₄
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In this paper, we design two mechanisms of combinations AC. The first one we called AC-I, AC-I and applied in top 75% of generations. The concept of AC-I is shown in Fig. 8, job 2 has been choose into position1 by roulette wheel selection. Check achieve block that whether any blocks' start position has position1 and job number is 2. If achieve then all elements in block will copy to AC. Otherwise, just insert job to AC which

Figure 1 illustrates the scheduling process of the proposed algorithm. It shows a sequence of blocks being added to a sequence (AC1) based on a roulette-wheel selection process.

Block achieve: A cylinder containing two blocks:

- Block1: 2, 1, 3, 5
- Block2: 7, 8, 4, 6

Start position 1:

Position1: AC1: 2, [empty slot], [empty slot], [empty slot], [empty slot], [empty slot], [empty slot], [empty slot], [empty slot], [empty slot]

Block 1 is selected. Insert block 1 to AC1:

Position2: AC1: 2, 1, 3, 5, 9, [empty slot], [empty slot], [empty slot], [empty slot], [empty slot]

Block 2 is not selected. Insert job 9 which selected by roulette wheel selection:

Position6: AC1: 2, 1, 3, 5, 9, 7, [empty slot], [empty slot], [empty slot], [empty slot]

AC1 is complete:

AC1: 2, 1, 3, 5, 9, 7, 4, 6, 10, 8

Another mechanism of combination AC is AC-II, AC-II executed in last 25% of the number of generations. The concept of AC-II is shown in Fig. 9, all blocks in block achieve will inject to AC at the first time. The remaining jobs which select by roulette wheel selection and insert to the remaining space of AC. At last generation, these blocks in block achieve already have good effect and stability of quality. Inject blocks into AC at first time, can make sure quality of AC and speed up the convergence of AC.

The diagram illustrates the process of inserting a new block into a circular queue and then performing a roulette wheel selection.

Block achieve: A circular queue (cylinder) containing two rows of blocks. The top row has blocks with values 2, 1, 3, and 5. The bottom row has blocks with values 7, 8, 4, and 6. The start position for the top row is labeled "Start position 1" and for the bottom row is labeled "Start position 5".

Insert block into AC first: A horizontal array representing the AC (Access Control) structure. The array has 10 slots. The first slot is labeled "Position 1" and the fifth slot is labeled "Position 5". An arrow points to the fifth slot, indicating that Block 1 is selected and inserted into the AC.

The remain jobs use roulette wheel selection: A horizontal array representing the roulette wheel selection. The array has 10 slots. The first slot is labeled "Position 5". An arrow points to the fifth slot, indicating that job 9 is selected by the roulette wheel selection.

AC-I and AC-II both use roulette wheel selection to select jobs by these probabilities, and each job's probability according to the combination probability which merge by each probability of dominance and dependency matrix. The combination probability (CP_{jobn}) defined as follow:

$$CP_{jobn}=(W_{dom} * P_{jobn}^{dom})+(W_{dep}+P_{jobn}^{dep}) \quad (1)$$

EHBSA is an important evolving process of EDA,

EHBSA/WT is using a template in sampling a new string. In generating each new individual, a template individual is chosen from $P(t)$ (normally, randomly). The n ($n>1$) cut points are applied to the template randomly. When n cut points are obtained for the template, the template should be divided into n segments. Then, we choose one segment randomly and sample nodes for the segment. Nodes in other $n-1$ segments remain unchanged. We denote this sampling method by EHBSA/WT/ n . Since average length of one segment is L/n , EHBSA/WT/ n generates new strings which are different at most L/n nodes on average from their templates.

In this paper, we propose a different rule instead of the origin EHBSA/ WT. As Fig. 10, first step is to randomly select a fragment from chromosome. The second step is to switch each gene in this fragment, and to calculate the fitness in each exchange. Finally selecting the exchange with the best fitness is

as a new AC.

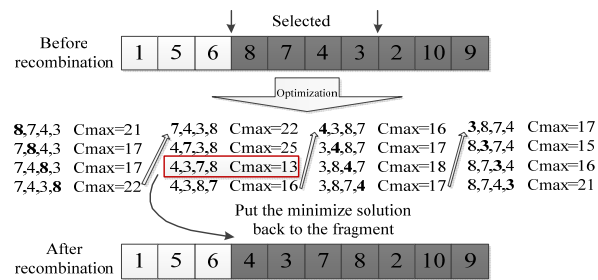


Fig. 10 Modify EHBSA procedure

TABLE I
PERFORMANCE COMPARISON OF TAILLARD'S INSTANCE

Instance	n,m	Opt.	PRED A Error Rate	JEDA Error Rate	SGGA Error Rate	ESGGA Error Rate	BBSPM Error Rate
Ta001	20,5	1278	1.20%	1.16%	1.20%	1.16%	0%
Ta002	20,5	1359	0.88%	0.49%	0.46%	0.36%	0.18%
Ta003	20,5	1081	2.04%	1.73%	1.19%	0.50%	0.04%
Ta004	20,5	1293	0.78%	0.70%	0.90%	0.48%	0.29%
Ta005	20,5	1235	0.82%	1.21%	0.92%	0.70%	0.15%
Ta006	20,5	1195	1.06%	1.54%	1.36%	1.00%	0.26%
Ta011	20,10	1582	0.95%	0.56%	0.82%	0.71%	0.15%
Ta012	20,10	1659	1.24%	1.10%	0.53%	0.28%	0.86%
Ta013	20,10	1496	1.53%	1.50%	1.18%	0.82%	0.76%
Ta014	20,10	1377	1.31%	1.15%	0.77%	0.87%	0.31%
Ta015	20,10	1419	0.98%	0.93%	0.84%	0.66%	0.67%
Ta016	20,10	1397	0.87%	1.50%	0.90%	0.61%	0.58%
Ta041	50,10	2991	3.57%	3.61%	2.95%	3.00%	2.32%
Ta042	50,10	2867	2.34%	3.30%	3.16%	2.75%	1.7%
Ta043	50,10	2839	3.38%	3.90%	3.13%	2.74%	2.37%
Ta044	50,10	3063	1.30%	1.98%	1.40%	1.05%	0.36%
Ta045	50,10	2976	3.09%	3.84%	3.29%	2.15%	1.69%
Ta046	50,10	3006	2.36%	3.00%	2.75%	2.35%	1.03%
Ta081	100,20	6202	5.53%	5.85%	5.96%	5.46%	3.83%
Ta082	100,20	6183	4.02%	4.05%	4.02%	3.37%	3.71%
Ta083	100,20	6271	3.77%	3.91%	3.81%	3.29%	3.27%
Ta084	100,20	6269	2.95%	3.67%	3.44%	3.19%	2.53%
Ta085	100,20	6314	3.97%	4.46%	4.40%	4.05%	3.33%
Ta086	100,20	6364	4.27%	4.58%	4.41%	3.99%	3.28%
Avg.			2.26%	2.49%	2.24%	1.90%	1.40%

IV. EXPERIMENTAL RESULTS

In this section we present the experimental results of the BBSPM and compare the performance of BBSPM with other algorithms. This research adopted the instances of Reeves and Taillard in OR-Library to validate the performance. Executed 30 runs for each instances, n represents the job number and m represents the machine number. Table I shows the performance comparison on Taillard instances. The comparison standard is based on Chen et al. [20]. From the result of BBSPM, the average error rate is 1.4%, outperforms the other algorithms. From the result in Table I, BBSPM has good performance better than the other algorithms.

V. CONCLUSION

In this research, we proposed an algorithm called BBSPM combine sequential pattern mining and EDA. Using sequential pattern mining to generate blocks and the artificial chromosomes are combined by blocks and EDA rule. By the information from two different methods, the artificial chromosomes could get more diversified and effective information. Besides the information from the two different sources, we also design two types of block-based AC generation approaches which are the better combination and competitive rule for artificial chromosomes. Finally, by the modified EHBSA mechanism from EDA, it would be more

powerful convergence approach. From the experimental result validated the idea of application of the AC injection and use modified EHBSA can help the evolutionary algorithm to enhance the searching ability. Furthermore, BBSPM has good performance to escape the local optima in the large instances. The research at the present stage is focus on the permutation flows-hop problems, and we will prepare to try other kinds of combinational problems in future to prove the robust of BBSPM.

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