Acoustic Source Localization Based on the Extended Kalman Filter for an Underwater Vehicle with a Pair of Hydrophones

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Abstract—In this study, we consider a special situation that only a pair of hydrophone on a moving underwater vehicle is available to localize a fixed acoustic source of far distance. The trigonometry can be used in this situation by using two different DOA of different locations. Notice that the distance between the two locations should be measured. Therefore, we assume that the vehicle is sailing straightly and the moving distance for each unit time is measured continuously. However, the accuracy of the localization using the trigonometry is highly dependent to the accuracy of DOAs and measured moving distances. Therefore, we proposed another method based on the extended Kalman filter that gives more robust and accurate localization result.

Keywords—Localization, acoustic, underwater, extended Kalman filter.

I. INTRODUCTION

OCALIZATION and navigation for an underwater vehicle are important tasks and have been studied widely in several decades [1]- [6]. Acoustic signal has a special position in the tasks because it spreads much farther than other signals such as sonar signal and vision signal. If the acoustic source is localized, the acoustic source can be a target or a landmark for an underwater vehicle and help the vehicle find its position and a direction to move. An array of hydrophones is mostly used to localize the acoustic source [9]- [10]. A pair of hydrophones can give direction of arrival (DOA) based on time difference of arrival (TDOA) between the two hydrophones [11]- [18]. TDOA is generally obtained by the method of general cross-correlation (GCC) which compute cross-correlation of the signals received by each hydrophones and find the time where a maximum peak arise. By the trigonometry, the location in two-dimensional space can be specified at least three hydrophone. More accurate localization is also possible by the method of beamforming using several hydrophones. Generally speaking, the more hydrophones are used, the more accurate localization is possible.

B. Kang and J. Shin are with the Department of Electrical Engineering, Pohang University of Science and Technology, San 31, Hyojadong, Namgu, Pohang, Kyungbuk, 790-784, Korea (e-mail: anbabo, shinshingo@postech.ac.kr)

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PooGyeon Park is with the Division of IT Convergence Engineering and the Department of Electrical Engineering, Pohang University of Science and Technology, San 31, Hyojadong, Namgu, Pohang, Kyungbuk, 790-784, Korea (e-mail: ppg@postech.ac.kr). However, the use of sensors are mostly restricted in underwater vehicle because the power and space of the vehicle are limited and the cost should be also considered. In this study, we consider a special situation that only a pair of hydrophone on a moving underwater vehicle is available to localize a fixed acoustic source of far distance. The trigonometry can be used in this situation by using two different DOA of different locations. Notice that the distance between the two locations should be measured. Therefore, we assume that the vehicle is sailing straightly and the moving distance for each unit time is measured continuously. However, the accuracy of the localization using the trigonometry is highly dependent to the accuracy of DOAs and measured moving distances. Therefore, we propose another method based on the extended Kalman filter that gives more robust and accurate localization result.

The paper is organized as follows: in Section II, the underwater acoustic source localization problem of consideration is formally stated and deterministic localization using the trigonometry is presented; in Section III, the methods of determining the location of an acoustic source using the extended Kalman filter is formulated; in Section IV, the simulation results are presented and two methods are compared; finally concluding remarks are given in Section V.

II. PROBLEM STATEMENT



Fig. 1. Acoustic source localization for an underwater vehicle

The considered acoustic source localization problem is illustrated on Fig.1. The underwater vehicle is moving straitly and the direction of moving is set as x-axis. The location of the vehicle at current time n is denoted by $(x_v(n), 0)$ and a fixed acoustic source is denoted by (x_s, y_s) . The DOA on current time n and the moving distance between current and prior measurement time is obtained with measurement noises and denoted by $\theta(n)$ and l(n), respectively.

From the definition of tangent function, three triangular The state and the measurement functions are linearized acequations are made by tangent function to $\left(\frac{\pi}{2} - \theta(n-1)\right)$ and $\left(\frac{\pi}{2} - \theta(n)\right)$:

$$\tan\left(\frac{\pi}{2} - \theta(n-1)\right) = \frac{x_s}{y_s},\tag{1}$$

$$\tan\left(\frac{\pi}{2} - \theta(n)\right) = \frac{x_s - l}{y_s},\tag{2}$$

$$x(n) - x(n-1) = l$$
 (3)

The location of the acoustic source can be given by using Equation (1)-(3) as

$$x_s = \frac{l \tan\left(\frac{\pi}{2} - \theta(n-1)\right)}{\tan\left(\frac{\pi}{2} - \theta(n-1)\right) - \tan\left(\frac{\pi}{2} - \theta(n)\right)},\qquad(4)$$

$$y_s = \frac{l}{\tan\left(\frac{\pi}{2} - \theta(n-1)\right) - \tan\left(\frac{\pi}{2} - \theta(n)\right)}$$
(5)

However, this calulated equations can be useful solution when the noise of oberver is exact or near zero. A little bit more noise can make large error. Thus different methods should be applied to estimate accurate position information in noisy environment, and one of those methods is the extended Kalman filter.

III. LOCALIZING AN ACOUSTIC SOURCE USING EXTENDED KALMAN FILTER

Consider a discrete nonlinear system given by

$$\mathbf{x}(n+1) = \mathbf{F}(n, \mathbf{x}(n)),\tag{6}$$

$$\mathbf{y}(n) = \mathbf{C}(n, \mathbf{x}(n)) + \mathbf{v}_1(n)$$
(7)

where n is the time step, $\mathbf{x}(n)$ is the state vector, $\mathbf{y}(n)$ is the measurement vector, $\mathbf{v}_1(n)$ is the measurement noise. We assume that $\mathbf{v}_1(n)$ have a zero-mean with covariance Q(n).

To estimate the location of the acoustic source, we use a model of the extended Kalman filter as follows. The state vector is $\mathbf{x}(n) = [x_1 \ x_2 \ x_3]^T$, where x_1 is the distance between acoustic source (x_s) and vehicle $(x_v(n))$ on the xaxis, x_2 is the position of acoustic source on y-axis (y_s) , and x_3 is the distance between previous position and current position of robot on x-axis (l(n)). The measurement vector is $\mathbf{y}(n) = [y_1 \ y_2 \ y_3]^T$, where y_1 and y_2 are the angle between acoustic source and vehicle at previous time step and current time step, respectively $(\theta(n-1), \theta(n))$, and $y_3 = l(n)$. The linear system and nonlinear measurement functions are used as follows:

$$\mathbf{F}(n, \mathbf{x}(n)) = \begin{bmatrix} x_1 - x_3 \\ x_2 \\ x_3 \end{bmatrix}, \qquad (8)$$

$$\mathbf{C}(n, \mathbf{x}(n)) = \begin{bmatrix} \tan^{-1}\left(\frac{x_2}{x_1}\right) \\ \tan^{-1}\left(\frac{x_2}{x_1-x_3}\right) \\ x_3 \end{bmatrix}.$$
 (9)

cording to

$$\mathbf{F}(n+1,n) = \frac{\partial \mathbf{F}(n,\mathbf{x})}{\partial \mathbf{x}} \bigg|_{\mathbf{x}=\hat{\mathbf{x}}(n|y_n)},$$
(10)

$$\mathbf{C}(n) = \frac{\partial \mathbf{C}(n, \mathbf{x})}{\partial \mathbf{x}} \bigg|_{\mathbf{x} = \hat{\mathbf{x}}(n|y_{n-1})}.$$
 (11)

Then, the system model can be approximated as

$$\mathbf{x}(n+1) = \mathbf{F}(n+1, n)\mathbf{x}(n), \tag{12}$$

$$\mathbf{y}(n) = \mathbf{C}(n)\mathbf{x}(n) + \mathbf{v}_1(n) \tag{13}$$

where

and

$$\mathbf{F}(n+1,n) = \begin{bmatrix} 1 & 0 & -1 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$
(14)

$$\mathbf{C}(n) = \begin{bmatrix} \frac{-\hat{x}_{2}(n|y_{n-1})}{\hat{x}_{1}^{2}(n|y_{n-1}) + \hat{x}_{2}^{2}(n|y_{n-1})} \\ -\hat{x}_{2}(n|y_{n-1}) \\ \frac{-\hat{x}_{2}(n|y_{n-1})}{(\hat{x}_{1}(n|y_{n-1}) - \hat{x}_{3}(n|y_{n-1}))^{2} + \hat{x}_{2}^{2}(n|y_{n-1})} \\ 0 \\ \frac{\hat{x}_{1}(n|y_{n-1}) \\ \hat{x}_{1}^{2}(n|y_{n-1}) + \hat{x}_{2}^{2}}{\hat{x}_{1}(n|y_{n-1}) - \hat{x}_{3}(n|y_{n-1})} \\ \frac{\hat{x}_{1}(n|y_{n-1}) - \hat{x}_{3}(n|y_{n-1})}{(\hat{x}_{1}(n|y_{n-1}) - \hat{x}_{3}(n|y_{n-1}))^{2} + \hat{x}_{2}^{2}(n|y_{n-1})} \\ 0 \\ \frac{0}{\hat{x}_{2}(n|y_{n-1})} \\ \frac{1}{(\hat{x}_{1}(n|y_{n-1}) - \hat{x}_{3}(n|y_{n-1}))^{2} + \hat{x}_{2}^{2}} \end{bmatrix}$$
(15)

Mean and covariance of the prior density are as follows:

$$E(\mathbf{x}(n)|\mathbf{y}(1)\cdots\mathbf{y}(n-1)) = \widehat{\mathbf{x}}(n|\mathbf{y}(n-1))$$

= $\mathbf{F}(n, n-1)\widehat{\mathbf{x}}(n-1|\mathbf{y}(n-1)),$ (16)
 $V(\mathbf{x}(n)|\mathbf{y}(1)\cdots\mathbf{y}(n-1)) = \mathbf{K}(n|n-1)$
= $\mathbf{F}(n, n-1)\mathbf{K}(n-1|n-1)\mathbf{F}^{T}(n, n-1)$ (17)

where $E(\cdot)$ is expectation operator and $V(\cdot)$ is covariance operator. The posterior density is now Gaussian with mean and covariance as follows:

$$E(\mathbf{x}(n)|\mathbf{y}(1)\cdots\mathbf{y}(n)) = \widehat{\mathbf{x}}(n|\mathbf{y}(n))$$
(18)

$$= \widehat{\mathbf{x}}(n|\mathbf{y}(n-1)) + \mathbf{G}_f(n) \left(\mathbf{y}(n) - \mathbf{C}(n)\widehat{\mathbf{x}}(n|\mathbf{y}(n-1))\right),$$

$$V(\mathbf{x}(n)|\mathbf{y}(1)\cdots\mathbf{y}(n)) = \mathbf{K}(n|n)$$

$$= (\mathbf{I} - \mathbf{G}_f(n)\mathbf{C}(n))\mathbf{K}(n|n-1).$$
(19)

where I is identity matrix, and $G_f(n)$ is the Kalman gain matrix

$$\mathbf{G}_{f}(n) = \mathbf{K}(n|n-1)\mathbf{C}^{T}(n) \left(\mathbf{C}(n)\mathbf{K}(n|n-1)\mathbf{C}^{T}(n) + Q(n)\right)^{-1}$$
(20)

The proposed algorithm is summarized in TABLE I

International Journal of Electrical, Electronic and Communication Sciences ISSN: 2517-9438 Vol:6, No:10, 2012

TABLE I THE PROPOSED ALGORITHM FOR ACOUSTIC SOURCE LOCALIZATION

$$\begin{aligned} \widehat{\mathbf{x}}(n|\mathbf{y}(n-1)) &= \mathbf{F}(n,n-1)\widehat{\mathbf{x}}(n-1|\mathbf{y}(n-1)) \\ \mathbf{K}(n|n-1) &= \mathbf{F}(n,n-1)\mathbf{K}(n-1|n-1)\mathbf{F}^{T}(n,n-1) \\ \mathbf{G}_{f}(n) &= \mathbf{K}(n|n-1)\mathbf{C}^{T}(n) \left(\mathbf{C}(n)\mathbf{K}(n|n-1)\mathbf{C}^{T}(n) + Q(n)\right)^{-1} \\ \widehat{\mathbf{x}}(n|\mathbf{y}(n)) &= \widehat{\mathbf{x}}(n|\mathbf{y}(n-1)) + \mathbf{G}_{f}(n) \left(\mathbf{y}(n) - \mathbf{C}(n)\widehat{\mathbf{x}}(n|\mathbf{y}(n-1))\right) \\ \mathbf{K}(n|n) &= \left(\mathbf{I} - \mathbf{G}_{f}(n)\mathbf{C}(n)\right)\mathbf{K}(n|n-1) \end{aligned}$$



Fig. 2. MSE of Acoustic Source Localization with errors of 2° in DOA and 20% in moving distance



Fig. 3. MSE of Acoustic Source Localization with errors of 2° in DOA and 40% in moving distance

IV. SIMULATION RESULTS

The acoustic source localization scenario is as follows: The location of the source is 1 kilometers apart along the moving direction of vehicle and 500 meters apart along the perpendicular direction from the location of the vehicle at time



Fig. 4. MSE of Acoustic Source Localization with errors of 5° in DOA and 20% in moving distance



Fig. 5. MSE of Acoustic Source Localization with errors of 5° in DOA and 40% in moving distance

0, that is, $(x_s, y_s) = (1000, 500)$ and $x_v(0) = 0$. The vehicle is moving with the speed of 1m/s. The DOA of each time is measured but have error which has normal distribution with 2 or 5° of standard deviation. The distance between the current and prior location of the vehicle is also measured with an error of less than 20 or 40%. The simulation results are illustrated in Fig2, Fig3, Fig4, and Fig5 with errors of $(2^\circ, 20\%)$, $(2^\circ, 40\%)$, $(5^\circ, 20\%)$, and $(5^\circ, 40\%)$, respectively. The mean square error (MSE) is defined by

$$MSE(n) = E(x_s - (x_v(n) + \mathbf{x}(1)))^2 + (y_s - (\mathbf{x}(2)))^2,$$
(21)

that is the distance between the source location and estimated source location.

V. CONCLUDING REMARKS

In this study, we considered a special situation that only a pair of hydrophone on a moving underwater vehicle is available to localize a fixed acoustic source of far distance. The trigonometry can be used in this situation by using two different DOA of different locations. Notice that the distance between the two locations should be measured. Therefore, we assumed that the vehicle is sailing straightly and the moving distance for each unit time is measured continuously. However, the accuracy of the localization using the trigonometry is highly dependent to the accuracy of DOAs and measured moving distances. Therefore, we proposed another method based on the extended Kalman filter that gives more robust and accurate localization result.

ACKNOWLEDGMENT

This research was supported by the MKE(The Ministry of Knowledge Economy), Korea, under the ITRC(Information Technology Research Center) support program supervised by the NIPA(National IT Industry Promotion Agency) (NIPA-2012-(H0301-12-1003)) and NIPA-2012-(H0301-12-2002)). This research was supported by World Class University program funded by the Ministry of Education, Science and Technology through the National Research Foundation of Korea (R31-10100). This research was supported by "Development of technologies for an underwater robot based on artificial intelligence for highly sophisticated missions", which is supported by KORDI.

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