

# Throughput Analysis over Power Line Communication Channel in an Electric Noisy Scenario

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**Abstract**—Powerline Communications –PLC– as an alternative method for broadband networking, has the advantage of transmitting over channels already used for electrical distribution or even transmission. But these channels have been not designed with usual wired channels requirements for broadband applications such as stable impedance or known attenuation, and the network have to reject noises caused by electrical appliances that share the same channel. Noise control standards are difficult to complain or simply do not exist on Latin-American environments. This paper analyzes PLC throughput for home connectivity by probing noisy channel scenarios in a PLC network and the statistical results are shown.

**Keywords**—Power Line Communications, OFDM, Noise Analysis, Throughput Analysis, PLC, Home Network.

## I. INTRODUCTION

COMMUNICATIONS by power lines, PLC, begun as an slow analog communications technology, and recently it has become in a wide band technology that has been compared with wireless LAN solutions [1]. Nevertheless, high-speed home network solutions have been developed to provide connectivity by wireless or wired mediums including 802.11 –WLAN–, 802.15–WPAN– and high speed 1394. One of PLC's greatest advantages is the use of low power residential lines with non impact over the electrical circuits, sharing the medium for both power and communications solutions. Electric companies invest on wired Internet access to achieve low cost solution for fixed Internet access as last mile solution and they can use the system to gain control over energy meters and it can be used for demotic applications using electrical appliances networks.

The initial PLC standard for PLC home networking is HomePlug 1.0 [2] for LAN connectivity at every power outlet, and it has been implemented in a wide variety of commercial

equipments such as routers, bridges, wireless access points, audio end points, speakers, VoIP phones, security cameras. HomePlug AV, supports entertainment applications such as HDTV and home theater throughout the home without new wires and provides this capabilities at competitive costs [3]. Recently, Telecommunications Industry Association (TIA) has adopted HomePlug 1.0 published in its standard TIA 1113, as the first multi-megabit power line communications standard approved by American National Standards Institute [4]. The first an only ANSI PLC standard defines operations, functions, and interface characteristics of a system for medium speed networking using the medium of power line wiring based on OFDM.

For PLC implementations on electrical Latin-American environments most of the noise control regulations are difficult to complain or simply does not exist, that's why this paper tries to analyze the effects of noisy electrical wired channels over the network throughput in common scenarios.

In the first part a Power Line Communications background is shown. In section III we will show a classification of the analyzed noise according to Zimmermann and Doster's work [5] and [6]. The probed scenarios are explained in section IV, and finally, in section V some graphical and analytical results are given.

## II. PLC BACKGROUND

This section is going to show the use of OFDM technology in PLC, a model of an electrical low power channel in a communications environment and a mathematical model of a PLC channel.

### A. Orthogonal Frequency-Division Multiplexing -OFDM

In OFDM a whole channel is divided into many narrow sub-channels which are transmitted in parallel. With OFDM technique, the duration of a symbol is increased and the Inter Symbol Interference –ISI– is reduced [7].

HomePlug 1.0 uses 84 OFDM sub-carriers equally spaced as the physical layer. The first subcarrier started at 4.49MHz and the last one is at 21MHz, in a bandwidth of 16.21MHz. To avoid intersymbol interference in the time-domain and intercarrier interference in the frequency domain, a cyclic prefix comprising the last 172 samples from the inverse fast Fourier transform (IFFT) interval of 256 samples is added to

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the beginning of the IFFT interval to form a 428-sample OFDM symbol. HomePlug 1.0 used the Robust Mode of OFDM when the channel is degraded and in this mode all subcarriers are activated [8]. The 84 subcarriers distribution is shown in Fig. 1.

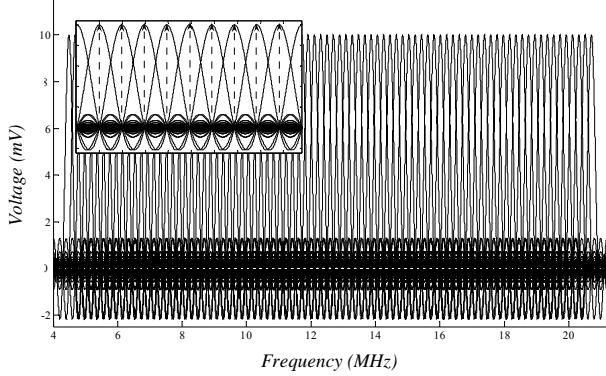


Fig. 1 OFDM spectral distribution

### B. Features of PLC Transmission Channel

An electric transmission line has been designed to transmit power in low frequency and causes a variance of the impedance because of the fact that a wide variety of appliances are connected to the outlet. Some statistical analysis and achieved measurements has shown a medium impedance of 100 to 150 ohms. However those values tend to decrease with frequencies below 2MHz. The attenuation of a powerline increases with the distance according to the impedance components that are composed by resistance per unit length,  $R'$ , inductance per unit length,  $L'$ , conductance per unit length,  $G'$ , and capacitance,  $C'$ , per unit length. The parameters have a closed relationship with the frequency and the line impedance can be described as follows [9]:

$$Z_L = \sqrt{R'(f) + j\omega f \cdot L'(f) / G'(f) + j\omega f \cdot C'(f)} \quad (1)$$

where  $\omega = 2\pi f$ . Another component to analyze is the propagation constant  $\gamma$  whose equation is formulated in (2).

$$\gamma(f) = \sqrt{[R'(f) + j\omega f \cdot L'(f)] \cdot [G'(f) + j\omega f \cdot C'(f)]} \quad (2)$$

It's also usual to describe the propagation constant as a function of the next complex equation.

$$\gamma(f) = \alpha(f) + j\beta(f) \quad (3)$$

where  $\alpha(f)$  as the real part, represents the line attenuation factor and  $\beta(f)$ , as the imaginary part, is the line phase factor and the angle variation between the transmitted and received signals.

### C. Mathematical Model of a PLC Channel

In [9], a PLC channel is described as a discrete-time impulse response in a path  $i$  with a certain delay  $\tau_i$  and certain attenuation factor  $C_i$  as is shown in (4).

$$h(t) = \sum_{i=1}^N C_i \cdot \delta(t - \tau_i) \quad (4)$$

In PLC channels the equation (4) is defined for frequency ranges between 500 KHz to 30 MHz [10]. The transfer function in the frequency domain can be described as follows.

$$H(f) = \sum_{i=1}^N g_i \cdot e^{[-(a_0 + a_1 f^k) l_i]} \cdot e^{-j\omega f \tau_i} \quad (5)$$

Where  $g_i$  is a weighting factor representing the product of the reflection and transmission factors along the path;  $l_i$  is the path length. The adjustable parameters  $a_0$ ,  $a_1$  and  $k$  are used to show the attenuation of the channel with  $k$  values from 0,5 to 1 and  $N$  paths from 5 to 50 for the above range of frequencies.

### III. ANALYZED NOISE ON PLC CHANNELS

It is not possible to analyze power line channels as a traditional noisy channel with additive white Gaussian noise (AWGN), Zimmermann et al, [5] and [6], classifies PLC channels into five classes according to Fig. 2.

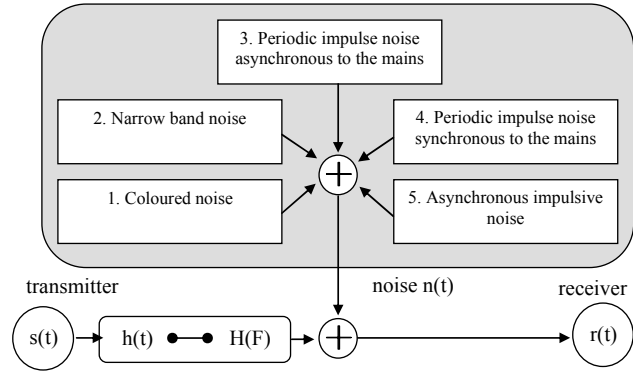


Fig. 2 Classification of Noise on PLC Channels

The coloured noise, narrow band noise and periodic impulsive noise are usually modeled as background noise because they remain stationary from seconds to even hours. Periodic impulsive noise synchronous to the mains and asynchronous impulsive noise may cause bit or burst errors over the transmission, although they are time variant.

A complete theoretical analysis on shown noises in Fig. 2 can be found on [5], [6], [11], [12] and [13].

### IV. PROBED SCENARIOS

In order to probe the throughput variations caused by noisy channels in electrical Latin-American environments, five scenarios were created with a PLC network, in a common electrical distribution home network, with 120 AC volts and 60Hz, the Fig. 3 shows the basic implementation. The electric noise source is connected in the outlet over the same electrical circuit using common wall sockets depending upon the scenario. In a first stage, the noise source is connecting at the Tx host side, the measurements are taken and the noise source

is connected at the receptor side for finally measurements.

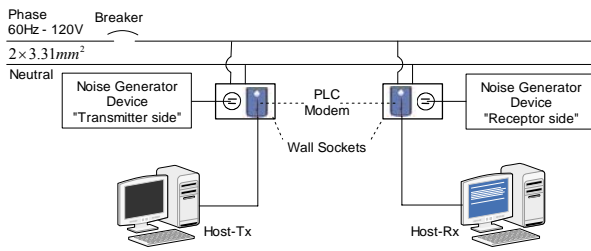


Fig. 3 Basic Networking Model

The probed scenarios are:

#### A. Scenario1 "Base Scenario"

Traffic is generated over a free electrical generated noise by sending files between 20MB to 100MB, in steps of 20MB incremented once every 50 samples. The collected data is delay, bit length on the frames and throughput.

This scenario is intended to evaluate transmission on normal conditions, and to compare results in noisy scenarios. The same files and variations are going to be used in every single scenario in order to collect data.

#### B. Scenario2

The channel is exposed to a 500 watts inductive load in the 90% of the transmission time that was taken in scenario 1.

#### C. Scenario3

In this scenario, an astable inductive load is connected to the electrical network. The periods of the generation are 2.5 sg, 5 sg and 10sg and are called  $t_{LAT}$ . Every single period has the same value during the whole transmission.

#### D. Scenario4

An inductive and resistive load of 40 watts is connected to the electric channel. The load is attached during all transmission time.

#### E. Scenario5

An electronic and resistive load is connected along the channel during the transmission time, an as in the last scenario the load is attached during all transmission time.

### V. RESULTS

As a first approach, the effects of the probed noise sources over the low voltage home network are shown and the scenarios are compared.

In the second results part, the noises that affected the probed channel are analyzed with the statistical resources.

#### A. PLC Throughput Results

In a protocol analyzer installed on the transmitter equipment, the total time for the transference was analyzed for the transmission path between the hosts. The total bit length was also measured and the data the throughput was calculated, in Mbps, with the scenarios described before. The obtained throughput is compared within the base scenario and the noise

effect over the channel is obtained.

#### 1) Scenario1 vs. Scenario2

The Fig. 4 shows the throughput for: scenario without noise generation (scenario1), scenario2 with the noise source is connected at the Tx side and scenario2 with the noise source attached at the Rx Host side.

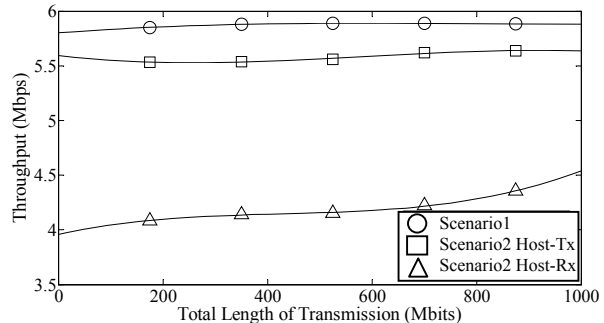


Fig. 4 Throughput, Scenario 1 Vs Scenario 2

When the noise is generated at the transmission side, is possible to see a throughput reduction of 5% compared with the throughput obtained in the scenario 1, but when the noise generation occurs in Rx side, as probed in scenario 2, the throughput decreases in 29% compared with the base scenario. In the last case, the 58% of the transmitted bits are transferred during the noise generation, afterwards, the throughput increases and time decreases as it is shown in Fig. 5, with files of 20MB, 40MB, 60MB, 80MB and 100 MB. Fig. 5 a), b), c), d) and e) shows the instant in which the inductive load is turned off. In Fig. 5 f), when the transmitted file is 100MB of length, the throughput is constant along the communication.

#### 2) Scenario3 vs. Scenario1

As explained for scenario 3, three comparisons had been made according to the times of  $t_{LAT}$ .

In the Fig. 6 (a), the throughput for  $t_{LAT}=10sg$  is shown. The throughput decreases when the astable load is connected at the Tx-host side in 0.82% and the throughput diminish in 0.96% when the load is attached at the Rx side.

For  $t_{LAT}=5sg$ , the throughput has a higher alteration for lower bit-lengths as it shows in Fig. 6 (b). The decrease for this compared scenario is 1.28% and 1.89% for the astable inductive load connected at the Tx-side and at the Rx- side, respectively.

The last compared scenario, with  $t_{LAT}=2.5sg$ , shows throughput differences of 1.45% with the load at the Tx-side and of 5% with the load at the Rx-side. These differences can be seen in Fig. 6 (c), always compared with the scenario 1

It is also possible to analyze the transmission time with the throughput for each period of the scenario 3 with the transmitted file of 60MB; this case is shown in Fig. 7.

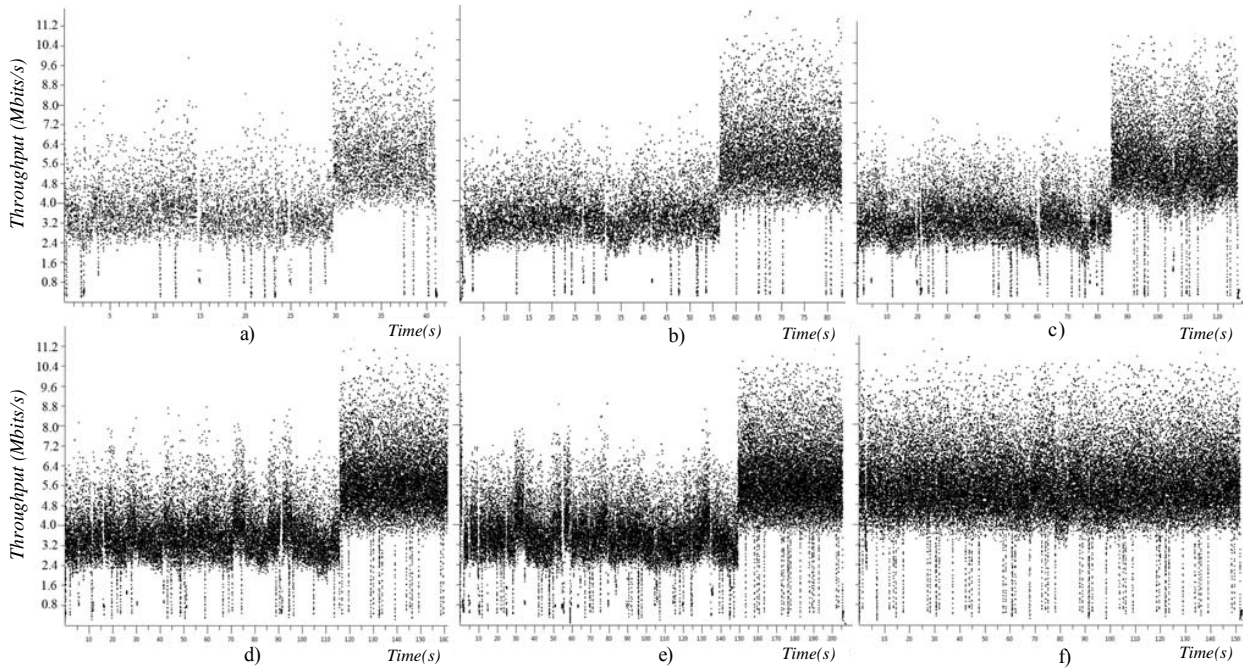


Fig. 5 Scenario 2 at Rx side, with files of a) 20MB, b) 40MB, c) 60MB, d) 80MB and e) 100MB. f) At the Tx-side with 100MB

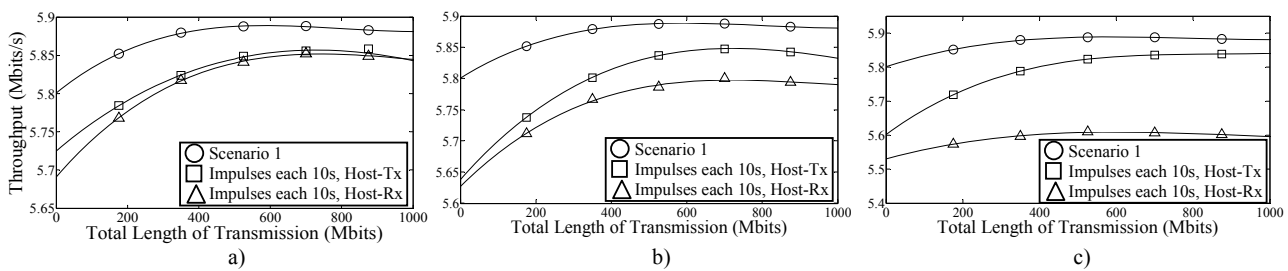


Fig. 6 Throughput for scenario3 for astable period times of a) 10sg, b) 5sg, c) 2.5sg

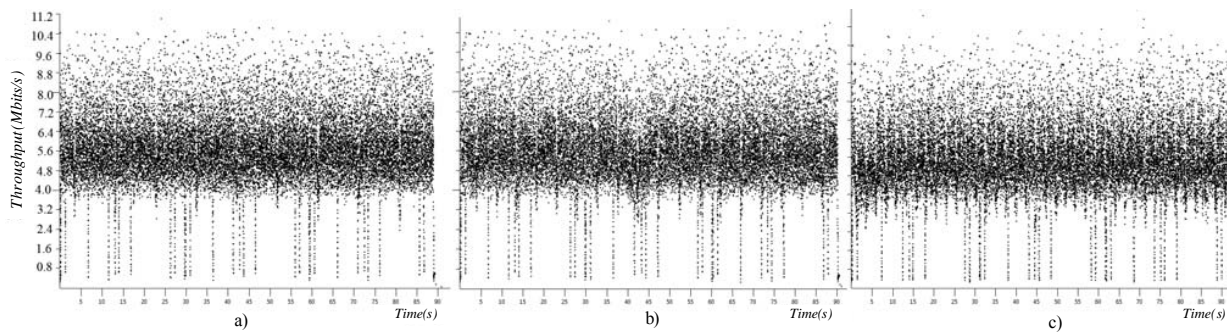


Fig. 7 Scenario 3 at the Rx-side with a transmission of 60MB with  $t_{IT}$  of a) 10sg, b) 5sg and c) 2.5sg

It is possible to see, on each case, white spaces on the graph that occurs in the edge of the load activation at the  $t_{IT}$  period, as seen on Fig. 7. When the load is attached at the Tx-side those space are not possible to distinguish. Although most of the graphs and data are not available for this paper we can provide them upon an e-mail request.

### 3) Scenario4 vs. Scenario1:

The throughput result shows that there is a decrease of

0.33% when this kind of load is connected at the Tx-side and there is a decrease of 5.66 at the Rx-side. As it occurs in most of the cases, the throughput is minimal affected when the noise is generated at the Tx-side, but it is meaningfully affected when the noise is connected at the Rx-side.

The throughput results for the scenario 4 are shown in Fig. 8. It is interesting to see that the maximum loss occurs with bit-lengths transmission of less than 400Mbits and with noise

generated at the Rx-side.

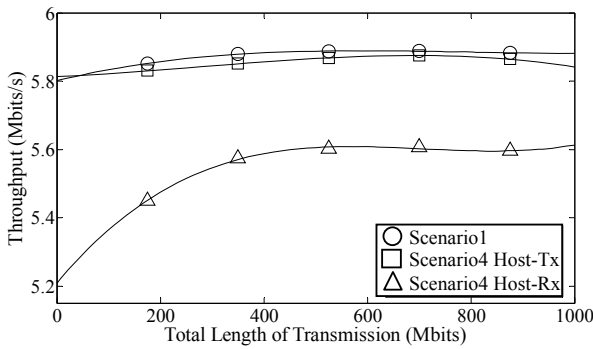


Fig. 8 Throughput for scenario 4

#### 4) Scenario5 vs. Scenario1:

In the scenario 5 the differences are very small compared with scenario 1 only a decrease of 0.24% and 0.26% with the load attached at the Rx-side and at the Tx-side respectively.

The results can be seen on Fig. 9:

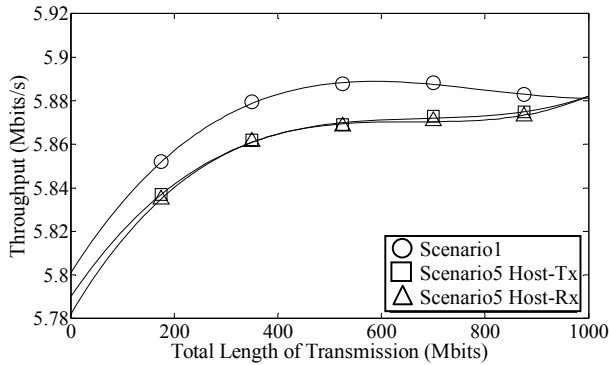


Fig. 9 Throughput for Scenario5

A summary of the throughput affection in all the scenarios compared with scenario 1 for PLC is shown in Table I. The results show a major throughput decrease with the characterized impulsive noise.

TABLE I  
THROUGHPUT REDUCTION FOR EVERY SINGLE SCENARIO COMPARED WITH  
BASE SCENARIO

Scenario1 compared with:	Load connected at:		Represented noise set
	Host-Tx (%)	Host-Rx (%)	
Scenario 2	5.00	29.0	Impulsive Noise
Scenario 3 10s	0.82	0.96	
Scenario 3 5.0s	1.28	1.89	
Scenario 3 2.5s	1.45	5.00	Background Noise
Scenario 4	0.33	5.66	
Scenario 5	0.24	0.26	

#### B. Noise Affecting PLC Channels

The noises that are affecting the PLC channel during the probed scenarios, can be analyzed as impulsive noise and as

generalized background noise, both of them are specified as follows:

##### 1) Impulsive Noise

In the generated noise within the scenario 3, the waveforms that are showing in Fig. 10 was obtained.

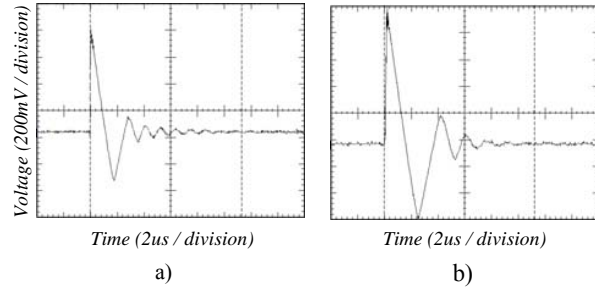


Fig. 10 Impulsive noise obtained within the scenario 3 a) case1, b) case2

The impulsive noise can be modeled by the equation (6):

$$n_s(t) = \sum_{i=1}^{I_s} A_i \sin[2\pi f_i(t - t_{arr,s}) + \alpha_i] e^{\left(-\frac{t-t_{arr,s}}{\tau_i}\right)u\left(\frac{t-t_{arr,s}}{\tau_i}\right)} \quad (6)$$

Where  $A_i$  defines the amplitude of the impulse,  $f_i$  and  $\alpha_i$ , the frequency and phase of the  $i$ -esime impulse,  $t_{arr,s}$  specifies the time where the impulses starts,  $t_{w,s}$  the time on seconds of the signal  $u(t)$  that is the shape of the pulse.

In order to calculate the power of the impulses, the relation of Zimmermann and Dostert [5],[6], is written in the equation (7):

$$P_{n_s}(t) = \frac{1}{t_{w,s}} \int_{t_{arr,s}}^{t_{arr,s}+t_{w,s}} n_s(t)^2 dt \quad (7)$$

The results of the analysis can be seen in the Table II.

TABLE II  
RESULTS OF THE SCENARIO 3

Impulse	Duration $t_{w,s}(\mu s)$	Amplitude $A_i(mV)$	Frequency $f_i(Khz)$	Power dBm
Case 1	11.27	766	778	14.69
Case 2	11.10	975	403	16.53

In the scenario 2, the impulses waveforms were analyzed in time domain and frequency domain as it is shows in the Fig. 11.

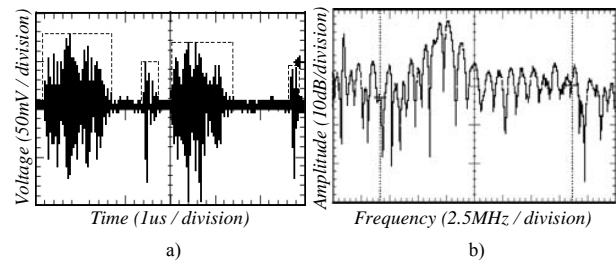


Fig. 11 Impulsive noise measured for scenario 2

The noise presented in scenario 2 has the duration of  $t_{w,s}$  with a time between impulses of  $t_{arr,s}$  and an amplitude  $A_i$ . This noise is presented during the complete period in which the inductive load is connected. In the spectral waveform of the Fig. 11 (b), de reference level is -45dBm spam of 25MHz, and the range limited by the cursors lines is the bandwidth of the PLC technology.

In order to generalize the noise 200 samples of the noises are taken and analyzed with a statistical tool. The amplitudes obtained are modeled by a Weibull Probability Density Function (PDF), as it is suggested for similar noises on ADSL analysis [14], [15].

The PDF Weibull can be described by equation (8) where  $a$  is the continuous variable of amplitude,  $\alpha$  is a scale factor and  $\beta$  is a shape parameter, with all positive values [16].

$$f(a) = \frac{\beta}{\alpha} a^{\beta-1} \exp \left[ - \left( \frac{a}{\alpha} \right)^\beta \right], \quad a > 0 \quad (8)$$

The PDF obtained with the Weibull approach appears in the Fig. 12 (a), with the calculated parameters.

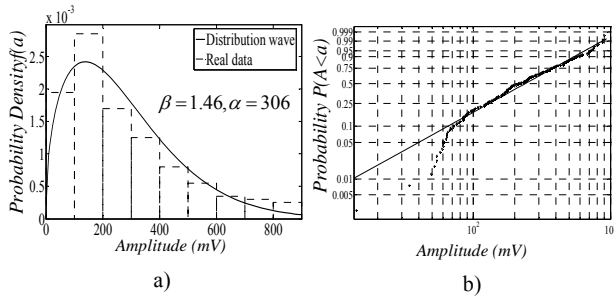


Fig. 12 Weibull Distribution a) PDF, b) Amplitude function

The Fig. 12 (b) shows the cumulative theoretical probability for Weibull distribution.

The next two variables are represented for an Exponential PDF that is symbolized by the equation (9), where  $x$  represents the continuous variable of the distribution and is equivalent to the impulses duration  $w$ , while the inter-arrival times is expressed by  $r$ .

$$f(x) = \lambda e^{-\lambda x}, \quad x \geq 0 \quad (12)$$

The representation of the probability density function of  $w$  is shown in Fig. 13 (a), where a higher probability of impulses duration can be found before of 16  $\mu$ s.

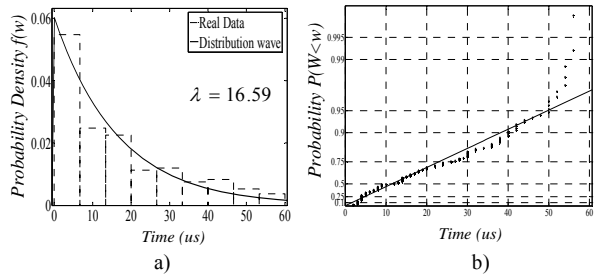


Fig. 13 Exponential function for the impulses duration a) PDF b) Distribution Function

The inter-arrival time between impulses has a probability density function  $f(r)$  as it is shown in Fig. 14 (a). There are not impulses for times below of 40  $\mu$ s. The plotted data fitted the theoretical function.

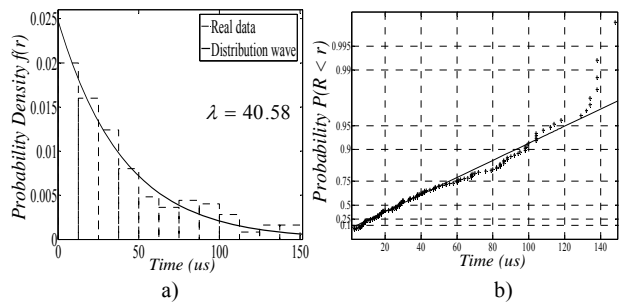


Fig. 14 Exponential function distribution for inter-arrival times between impulses a) PDF b) Exponential probability

As a summary of the analyzed variables, the Table III shows the distributions and its parameters.

TABLE III  
MEAN AND VARIANCE FOR THE ANALYZED

Variable	Distribution	Mean	Variance
Amplitude( $a$ )	Weibull	277.2mV	37244mV <sup>2</sup>
Duration( $w$ )	Exponential	16.595 $\mu$ s	275.39 $\mu$ s <sup>2</sup>
Inter-arrival times( $r$ )	Exponential	40.58 $\mu$ s	1646.5 $\mu$ s <sup>2</sup>

## 2) Generalized Background Noise

The set of noise belong to the background noise do not show an important affection to the throughput on the communication network when the load is connected at the Tx side. The phenomenon is explained by the low power density of this kind of noises in the range of frequencies used by PLC, see Fig. 15.

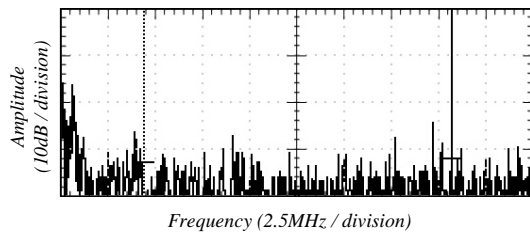


Fig. 15 Spectral Plot for the Background Generalized Noise. Spam 25MHz, Center 12.5MHz, Reference -47dB

## VI. CONCLUSION

In a Powerline communications network for home broadband application, if electrical noises control standards do not apply or do not exist, for implementation of such a technology, it is necessary to analyze if the mean throughput achieved in a noisy scenario is the most convenient, according to the applications and to the channel capacity requirements.

The impulsive noise generated near the receiver host is the noise that more affected throughput, and if that noise is generated by a high power inductive appliance, the affectation is even worst.

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