

# Power Forecasting of Photovoltaic Generation

S. H. Oudjana, A. Hellal, and I. Hadj Mohammed

**Abstract**—Photovoltaic power generation forecasting is an important task in renewable energy power system planning and operating. This paper explores the application of neural networks (NN) to study the design of photovoltaic power generation forecasting systems for one week ahead using weather databases include the global irradiance, and temperature of Ghardaia city (south of Algeria) using a data acquisition system. Simulations were run and the results are discussed showing that neural networks Technique is capable to decrease the photovoltaic power generation forecasting error.

**Keywords**—Photovoltaic Power Forecasting, Regression, Neural Networks.

## I. INTRODUCTION

THE world population is growing at a rapid pace, and witz. The global energy consumed and demanded also grows. Speculation about the depletion of fossil fuel reserves is a cause of concern for most governments and economies, and together with climate change and energy security issues, drives a massive campaign for clean and renewable energy options that would supplement the current energy production technologies. The issue of reducing CO<sub>2</sub> emission amount makes the whole world concentrate on installing renewable energy resource. Therefore, the interest in the solar and wind energy is consistently increasing whih in these days. However, to equip energy resource holds lots of problems yet so that we cannot rely on such renewable energy generation amount for the national power system. One of the most serious problems is that energy resource is affected by weather condition a lot. Thus, the power produced by energy resource is provided irregularly and depletes the national power system stability and reliability [1], [2].

The forecasts are keys to the reliable and cost effective large scale integration of photovoltaic (PV) systems into electricity grids. In addition, prediction of PV power generation is also required for the planning and resizing of large scale PV plants, balancing control, power system stabilization, green power transactions, power interruption warnings in autonomous power systems and so on [3].

The Short-term photovoltaic power generation forecasting methods are experience forecast, such as electricity elasticity coefficient, integrated power consumption, output and growth rate of consumption, extrapolation forecast and district load

density index method. Such methods need to generation the value, yield and growth rate, and other data [4].

The statistical analysis methods used in the power generation forecasting are regression analysis and time series, such as linear regression model, multiple linear regressions model, nonlinear regression analysis, autoregressive (AR) model, moving average (MA) models, autoregressive moving average (ARMA) model and nonstationary time-series. The statistical analysis methods need some relationship of values and the changes among identify consumption, load, time, total output value of industry in electricity gross domestic product, and then use mathematical models to forecast. The entire process is projected to ongoing mathematical model calibration and adjustment process, which will be taken longer time to complete [5]-[11].

The intelligent methods based power generation forecasting are expert system, grey generation, fuzzy logic, artificial neural networks, which used in the economic environment changes, and other random factors interfere with the power system under load accurately forecast which widely used to analyze numerous uncertainties and the power load forecast correlation. But how accurate will describe the criteria adopted for the artificial uncertainties are relatively difficult. This paper provides neural networks models based on the temperature and irradiance data [12]-[15].

The objective is to develop a forecasting model which will be able to consistently forecast the energy generated by photovoltaic modules using explanatory variables available at most weather stations. The aim of this study is to enable future photovoltaic projects in Ghardaia city (south of Algeria) to be deployed at a much faster rate and at lower costs.

## II. REGRESSION METHOD

Regression is a statistical technique for building a link between an explanatory variables and dependent variable. The aim is to predict the dependent variable when you know the explanatory variable or establish if there is an effect of one variable on another.

### A. Simple Linear Regression

The basic model for a deterministic set of  $n$  observations is given by (1):

$$Y_i = b_0 + b_1 X_i + e_i \quad i = 1, 2, \dots, n \quad (1)$$

$Y_i$ : dependent variable,

$X_i$ : explanatory variable,

$b_0$ : standard estimator,

$b_1$ : explanatory variable estimator.

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Estimators  $b_0$  and  $b_1$  are calculated by the least squares method.

If the power  $P_{i+1}$  (dependent variable) depends only on the corresponding temperature  $T_{i+1}$  (independent variable), the prediction is generated as follows:

$$P_{i+1} = b_0 + b_1 T_{i+1} + e_{i+1} \quad (2)$$

The strength of association between two variables is estimated by the correlation coefficient ( $r$ ). This coefficient ranges from -1 to +1. If it is between 0.8 and 1 (absolute value), the strength of association between two variables is important. Between 0.5 and 0.8 is moderate, and between 0.2 and 0.5 it is weak:

$$r = \frac{\sum_{i=1}^n x_i y_i - \frac{1}{n} (\sum_{i=1}^n x_i) (\sum_{i=1}^n y_i)}{\sqrt{[\sum_{i=1}^n x_i^2 - \frac{1}{n} (\sum_{i=1}^n x_i)^2] [\sum_{i=1}^n y_i^2 - \frac{1}{n} (\sum_{i=1}^n y_i)^2]}} \quad (3)$$

**B. Multiple Linear Regression**

Multiple regression is a generalization of the simple linear regression. The difference is that there are more variables to explain the dependent variable. Thus for  $k$  variables, the model become:

$$\hat{y} = b_0 + b_1 x_1 + b_2 x_2 + \dots + b_k x_k \quad (4)$$

where in  $Y$  is a vector of values of  $y$  while  $X$  is a matrix of independent variables  $x$  described as follows:

$$Y = \begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_n \end{bmatrix}, X = \begin{bmatrix} 1 & x_{11} & x_{12} & \dots & x_{1k} \\ 1 & x_{21} & x_{22} & \dots & x_{2k} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & x_{n1} & x_{n2} & \dots & x_{nk} \end{bmatrix} \quad (5)$$

The estimators are calculated by the  $B$  matrix:

$$B = [b_0 \ b_1 \ b_2 \ \dots \ b_k]^T = (X^T X)^{-1} X^T Y \quad (6)$$

**III. NEURAL NETWORKS**

From the beginning of nineties, new techniques appear to study the electrical load forecasting such as artificial neural networks. These recent techniques quickly became widely used in short-term PV generation forecasting. The mathematical model of an artificial neuron (Fig.1) consists essentially of an integrator that performs a weighted sum of its inputs. The result  $n$  of this sum is then transformed by a transfer function  $f$  which produces the output of a neuron. The  $R$  input neurons correspond to the vector  $P = [p_1, p_2, \dots, p_R]^T$ , whereas  $W = [w_{11}, w_{12}, \dots, w_{1R}]^T$  represents the vector of the weights of the neuron. The output  $n$  of the integrator is given by the following equation:

$$n = \sum_{j=1}^R w_{1,j} p_j - b \quad (7)$$

To verify the performance of the forecasting model, we can calculate the mean absolute percent error:

$$MAPE = \frac{100}{n} \sum_{i=1}^n \frac{|P_i - \hat{P}_i|}{P_i} \quad (8)$$

$P_i$ : Desired Power

$\hat{P}_i$ : Forecast Power

$n$ : Number of sample

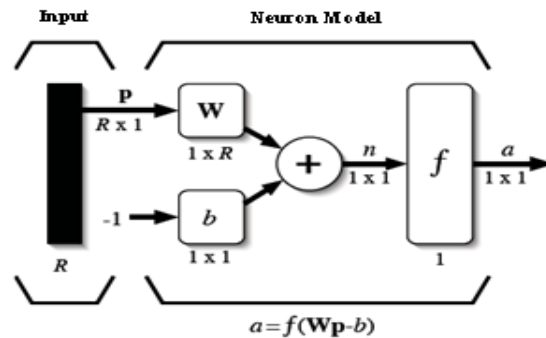


Fig. 1 Model of an artificial neuron

**IV. FORECASTING MODELS**

Three models have been tested and validated using different factors to verify their performances.

**A. Model 1**

This forecasting model requires only the temperature as an explanatory variable or as a database using simple regression and the neural network methods to predict the PV power generation for seven days ahead.

**B. Model 2**

The irradiance (solar radiation) factor at the previous time are used as database to predict the power generation for one week ahead, using the simple regression method and the neural network technique. Table I shows the correlation between the power and the corresponding temperature.

**C. Model 3**

The database of this model depends on two independent variables: the temperature and that of irradiance parameter corresponding to the same day of power forecasting value.

The strength of association between the generated power of photovoltaic module and the temperature is low (Table I). Against by the strength of association between the current power and irradiance factor is very strong. The correlation coefficient  $r = 0.98$  explains the intensity correlation, and the positive sign of this value expresses the proportional relationship of power with the corresponding value of

irradiation, which means that when the irradiation increases the power generated by the PV module increases. Fig. 4 and 5 illustrate the correlation between the generated power of photovoltaic module and temperature, and between power and the irradiance factor corresponding respectively. Fig. 2 and Fig. 3 illustrate the temperature and irradiance of Ghardaia city in 2008.

TABLE I  
EXPLANATORY VARIABLES CORRELATION

Explanatory Variables	Correlation Factor ( $r$ )
Temperature	0.37
Irradiance	0.98

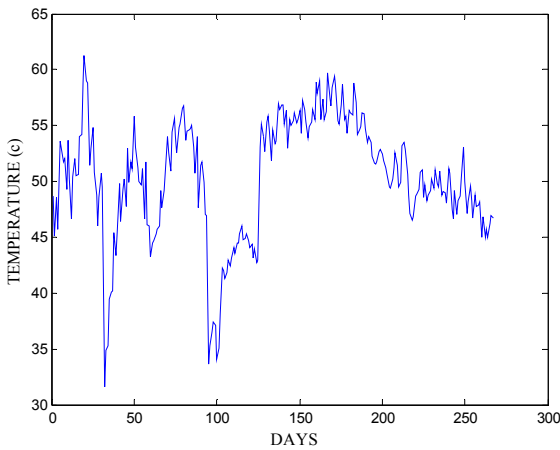


Fig. 2 Temperature Curve

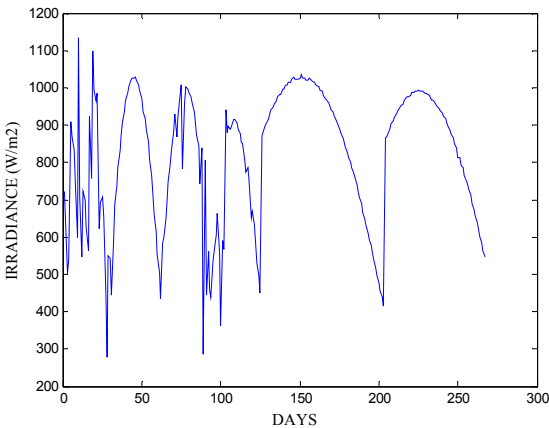


Fig. 3 Irradiance Curve

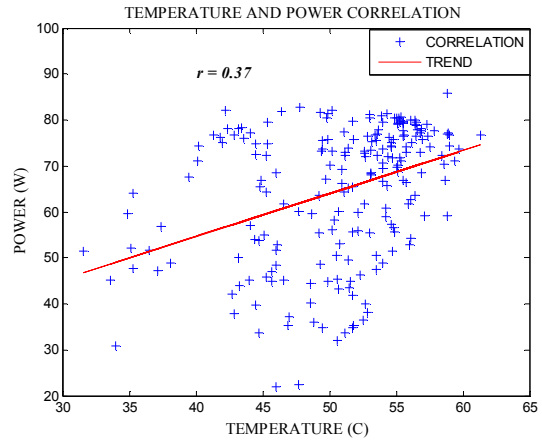


Fig. 4 Temperature vs. Power correlation

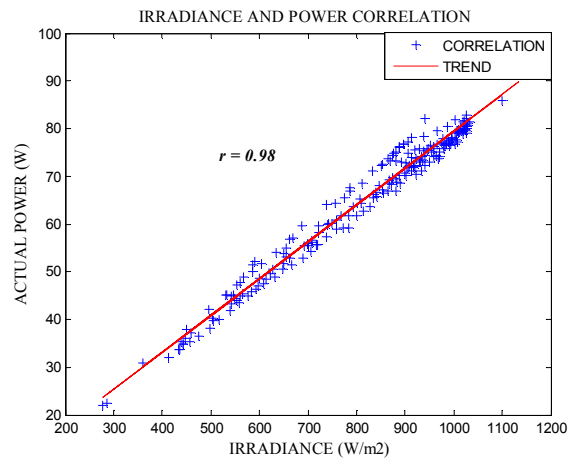


Fig. 5 Irradiance vs. Power Correlation

V. SIMULATIONS

To validate the three forecasting models presented, in terms of the mean relative error, we must test multiple databases. For this, we used three database of 2008: 70%, 80% and 90% of data used to train the neural network by MATLAB code that we can predict the power generated in one week ahead, Table II representing three databases. The three models will be tested using the method of simple regression and neural networks. The performance of each model is verified by the mean absolute percent error MAPE.

The prediction error of Model 1 (Table III) is large because only one independent variable or explanatory (temperature) was used. Its correlation with the PV module power is low, it is necessary to introduce other variables to improve performance. However, it is preferable to use neural networks in this case because it does not require several explanatory variables. Thus, Fig. 6 shows the power forecasting of this model. The difference between the desired power and that achieved using the regression is great because it cannot predict the power associated with changes in temperature. On the

other side, the method of neural network prediction narrowed the power gap to 1.48% that has a correlation with temperature by this intelligent technique.

Since the factor of radiation having a strong correlation with the power of the PV module, the forecast error will obviously decrease compared to model 1, and this is the case shown in Table IV, knowing that the average errors of the three tested is less than 4% using the method of simple linear regression, and the best accuracy is 1.093% using the neural network. Fig. 7 illustrates the application of Model 2 which shows the approach of the forecasting curve to that desired.

By hybridizing the model 1 and model 2, we obtain model 3, that is to say that the explanatory variables used to forecast power of photovoltaic module are temperature and irradiance. The accuracy of prediction using this model is even better (Table V) because the power produced by photovoltaic panel depends on the meteorological factors and the correlation between these variables and power is even stronger. Fig. 8 shows the curve prediction by multiple regression and neural networks and shows that the power curve are realized and that provided nearly superimposed, such that the accuracy of prediction reached 0.217% (Table V) by the NN. This means that the prediction using the parameters of temperature and irradiance is more accurate than using the variable temperature or irradiation. Table VI summarizes the difference between the regression and the neural networks.

TABLE VI  
NEURAL NETWORKS VS. REGRESSION COMPARISON

Regression	Neural Networks
requires a mathematical model	does not require a mathematical model
Several explanatory variables	Few explanatory variables
Small data base	large database
Short execution time	Long execution time

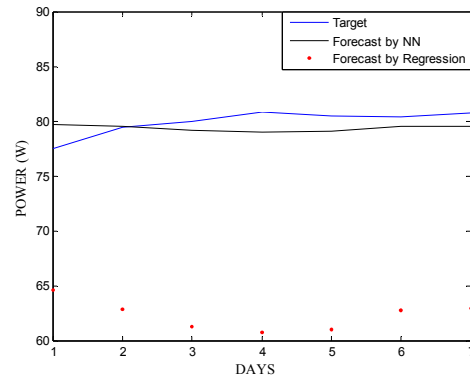


Fig. 6 PV Power Forecasting Using Model 1

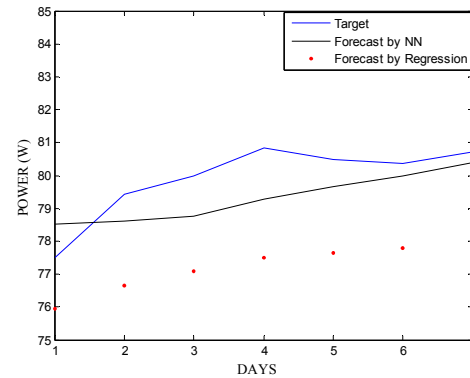


Fig. 7 PV Power Forecasting Using Model 2

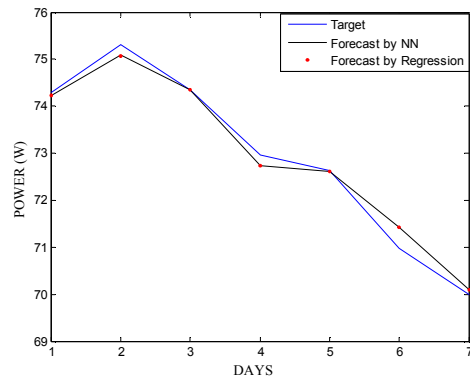


Fig. 8 PV Power Forecasting Using Model 3

TABLE II  
DATA SETS

Set	Test (day)	Validation (day)
01	187	188-194
02	214	215-221
03	240	241-247

TABLE III  
VALIDATION OF MODEL 1 PERFORMANCE BY MAPE (%)

Set	Simple Regression	Neural Networks
01	39.148	2.717
02	21.969	1.484
03	11.754	2.082
<b>Mean (%)</b>	<b>24.290</b>	<b>2.094</b>

TABLE IV  
VALIDATION OF MODEL 2 PERFORMANCE BY MAPE (%)

Set	Simple Regression	Neural Networks
01	4.876	6.070
02	3.250	1.093
03	1.744	3.702
<b>Mean (%)</b>	<b>3.290</b>	<b>3.621</b>

TABLE V  
VALIDATION OF MODEL 3 PERFORMANCE BY MAPE (%)

Set	Multiple Regression	Neural Networks
01	0.708	0.676
02	0.767	0.758
03	0.218	0.217
<b>Mean (%)</b>	<b>0.564</b>	<b>0.550</b>

## VI. CONCLUSION

Short-term photovoltaic power generation forecasting is important to the operation of power system to make decisions

by the dispatching center that cares to ensure electrical network security management while having a reliable and cost effective production system that meets specific environmental constraints.

The work initiated in this paper aimed to achieve a program that can predict the power generated by a PV generator to one week ahead at the site of Ghardaia (south of Algeria) and analyze the relationship between meteorological factors and the power supplied by applying the neural network technique. The regression is a standard statistical method based on a mathematical model. Against by the technique of neural networks does not require a mathematical model, but is based on artificial intelligence.

Before choosing a forecasting model of the power supplied by a photovoltaic module, we must first determine the correlation between independent variables and the desired power. For Model 1, the strength of association between temperature and power is low, so the forecast error is large. But the correlation between the predicted power and the irradiation is strong; consequently the forecast error becomes acceptable using model 2. Model 3 gave us a better accuracy, based mainly on two factors: temperature and irradiance, so that they can be used to short-term electric power of a photovoltaic plant. We conclude that the choice of forecast model output based on the study of the relationship of the explanatory variables with the desired power. Furthermore, this correlation is stronger, the model is better.

#### REFERENCES

- [1] Paul Swanepoel, "A forecasting model for photovoltaic module energy production," M. Sc. thesis, Nelson Mandela Metropolitan University, South Africa, 2010
- [2] Min-Cheol Kang, Jin-Man Sohn, Jong-young Park, Song-Keun Lee, Yong-Tae Yoon, "Development of algorithm for day ahead PV generation forecasting using data mining method," IEEE 54th International Midwest Symposium on Circuits and Systems (MWSCAS), pp.1-4, 2011
- [3] Mitsuru Kudo, Akira Takeuchi, Yousuke Nozaki, Hisahito Endo, Jiro Sumita, "Forecasting electric power generation in a photovoltaic power system for an energy network," Electrical Engineering in Japan, Vol. 167, No. 4, 2009
- [4] Ying-zi Li, Jin-cang Niu, " Forecast of Power Generation for Grid-Connected Photovoltaic System Based on Markov Chain," IEEE Conference on Power and Energy Engineering APPEEC pp.1-4, 2009
- [5] Jingfei Yang, "Power System Short-term Load Forecasting," M. Sc. thesis, Beijing University, China, 2006
- [6] Alexander Bruhns, Gilles Deurveilher, Jean-Sébastien Roy, "A non-linear regression model for mid-term load forecasting and improvements in seasonality," 15th PSCC, Liege, 2005.
- [7] CHEN Hao, "A new method of load forecast based on generalized autoregressive conditional heteroscedasticity model," Automation of Electric Power Systems, Vol.31, No. 15, pp. 51-54, 2007
- [8] ZHANG Zhen-gao, YANG Zheng-ling, " Load derivation in short term forecast using weather factor," A Publication of the Chinese Society of Universities for Electric Power System and Automation, Vo 1. 18 No. 5, pp. 79-83, 2006
- [9] LU Hai-feng, SHAN Yuan-da, "Recursive and adaptive super-short term load forecast method," Power System Technology, Vol. 24, No. 3, pp. 28-31, 2000
- [10] Kang Chongqing, Xia Q ing, Zhang Bom ing, " Review of power system load forecast and its development," Automat ion of Electric Power Systems, Vol. 28, No.17, pp. 1-11, 2004
- [11] WANG Xian, ZHANG Shao hua, "An improved method for short-term electric load forecast using time series techniques," Journal of Shanghai University(Natural Science Edition), Vol. 8, No. 2, pp. 133-136, 2002
- [12] Zhang Tao, Zhao Dengfu, Zhou Lin, Wang Xifan, Xia Daozhi, " Short-term load forecast using radial basis function networks and expert system," Journal of Xi'an Jiaotong University, Vol. 35, NO.4, pp. 331-334, 2001
- [13] A. Yona, T. Senjyu, A.Y. Saber, T. Funabashi, H. Sekine, Kim. Chul-Hwan, "Application of neural network to 24-hour-ahead generating power forecasting for PV system," IEEE General Meeting on Power and Energy Society - Conversion and Delivery of Electrical Energy in the 21st Century, pp.1-6, 2008
- [14] Liang Haifeng, Li Gengyin, Zhou Ming, "An adaptive BP-network approach to short term load forecast," Electric Utility Deregulation, Restructuring and Power Technologies, 2004 (DRPT 2004). Proceedings of the 2004 IEEE International Conference Vol. 2, pp. 505-509, 2004
- [15] Mao Yi; Yang Fan; Wang Caiping, " Short Term Photovoltaic Generation Forecasting System Based on Fuzzy Recognition," Transactions of China Electrotechnical Society, 2011

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