Modified Montgomery for RSA Cryptosystem

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Abstract—Encryption and decryption in RSA are done by modular exponentiation which is achieved by repeated modular multiplication. Hence efficiency of modular multiplication directly determines the efficiency of RSA cryptosystem. This paper designs a Modified Montgomery Modular Multiplication in which addition of operands is computed by 4:2 compressor. The basic logic operations in addition are partitioned over two iterations such that parallel computations are performed. This reduces the critical path delay of proposed Montgomery design. The proposed design and RSA are implemented on Virtex 2 and Virtex 5 FPGAs. The two factors partitioning and parallelism have improved the frequency and throughput of proposed design.

Keywords—RSA, Montgomery modular multiplication, 4:2 compressor, FPGA.

I. INTRODUCTION

THE growth of data communications and other internet services has made security a vital service to electronic communications. Four basic services like confidentiality, integrity, authentication and non repudiation are required by communication systems. RSA is a popular public key cryptosystem for encryption and digital signatures [1]. Encryption, decryption and digital signatures are modular exponentiation operations which are achieved by repeated modular multiplications. The security of RSA cryptosystem depends on inability to efficiently factorize the modulus of size 1024 bits or more. Hence the security of RSA will be more if the operands are of large size. But for the large size operands, high throughput rate for RSA is hard to achieve. Many researchers have worked to improve the throughput of RSA by improving the modular multiplication design.

In 1985, P.L. Montgomery [2] proposed an efficient method for modular multiplication which replaces trial division by modulus with series of additions and shift operations. The critical operation in Montgomery design is addition of large size operands. To avoid the carry propagation during addition several architectures are proposed in literature such as systolic array modular multipliers [3], [4] and carry save adder (CSA) architectures [5]-[11]. McIvor et al. [5], [6] proposed two Montgomery modular multiplication architectures: five-totwo CSA (three levels of carry save logic) and four-to-two CSA with two additional registers (two levels of carry save logic and extra control logic). These designs take input (except the modulus) and give output in carry save format. This avoids repeated output/input format conversion, lengthy and costly conventional additions. Also, the critical path delay of Montgomery architectures with carry save adders is word length independent [6]. The New Montgomery multiplication proposed by K. Manochehri et al. [8] has higher throughput than [5], [6] as it calculates quotient in parallel with the summation of partial sum and partial product. H. Thapliyal et al. [9] have used 4:2 compressor and carry save adder in fiveto-two CSA and novel hardware unit in 4:2 CSA to reduce the critical path delay. M.D. Shieh [11] proposed new modular exponentiation architecture with unified multiplication/square module in which the number of operands was reduced by mathematical manipulation. The critical path was reduced to 4 to 2 CSA with limited overhead but it could be used only for H algorithm of modular exponentiation.

The work in this paper is based on rearrangement of logic operations for addition with 4:2 compressor. It extends from existing 4:2 compressor applied in 4:2 CSA Montgomery [9]. Parallel and partitioned computations have reduced the critical path delay of proposed Montgomery modular multiplication. Our work has high throughput and is suitable for both H and L binary methods of RSA Modular Exponentiation. Section II gives brief introduction to Montgomery algorithms. Section III discusses the Modified Montgomery design. Section IV gives implementation results on FPGAs. Finally section V concludes the paper.

II. MONTGOMERY MODULAR MULTIPLICATION

Montgomery modular multiplication treats the digits of multiplier from least significant bit to most significant bit, performs shift down of partial result instead of shift up, and add rather than subtracting multiples of the modulus. It is most efficient method for performing modular multiplication in which the quotient only depends on the least significant digit of operands and the time consuming division is avoided by shifting modular addition. It is suitable for both hardware and software implementations. This has led to extensive research in Montgomery modular multiplication and form the basis of most of the reported high performance RSA hardware architectures. Montgomery's algorithm computes modular multiplication with inputs A, B and n. Inputs A and B are in Montgomery's domain and n is k bit modulus. Then the output is S such that $S=A \times B \times r^{-1} \mod n$ where $r=2^k$. The transformations between the n-residue (Montgomery domain) and the integer set are done using Montgomery's modular multiplication (MMM).

• A, the n residue of a is obtained as follows

MMM (a, r^2 , n) = $a \times r^2 \times r^{-1} \mod n$

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 $A=a \times r \mod n$ (1)

The n residue to integer value is obtained as follows

a=MMM (A, 1, n) = $A \times 1 \times r^{-1} \mod n$ (2)

Algorithm 1 MMM (A, B, n)

- // Montgomery's modular multiplication algorithm
- // Inputs: A and B (multiplier and multiplicand in

// Montgomery's domain, k bits)

// n (k bits modulus), A, B < n

// Output S= A×B×r⁻¹ mod n, where r= 2^{k}

- 1. S=0;
- 2. for i=0 to k-1
- 3. { $q[i]=(S+A_i \times B) \mod 2$;
- 4. $S = (S + A_i \times B + q[i] \times n)/2;$
- 5. if $(S \ge n)$
- 6. S=S-n;
- 7. return S;

After k iterations if the final result $S \ge n$ then an extra operation S=S-n is needed. To remove this subtraction, C.D. Walter [12] kept the range of convergence at [0, 2n) and increased the number of iterations from k to k+2. Thus the bit width of the operands and the value of r were changed accordingly.

Algorithm 2 Walter MMM (A, B, n)

- // Walter's Montgomery modular multiplication algorithm // Inputs: A (multiplier in Montgomery's domain, k+2 bits $//A_{k+1}=0$
- // B (multiplicand in Montgomery's domain, k+1 bits)

// n (k bit modulus), A, B < 2n

- // Output S= A×B×r⁻¹ mod n, where r= 2 $^{k+2}$,
- $/\!/\; 0 \leq S < 2n$
 - 1. S=0;
 - 2. for i=0 to k+1
 - $\{q[i]=(S+A_i \times B) \mod 2;$ 3.
 - $S = (S + A_i \times B + q[i] \times n)/2;$ 4.
 - 5. return S;

To further simplify the quotient computation the multiplicand B can be shifted up by one bit to make B₀=0 [8]. The price for this simplification is one extra iteration by making $A_{k+2} = 0$.

Algorithm 3 Modified MMM (A, B, n)

- // Montgomery's modular multiplication algorithm // Inputs A (k+3 bit multiplier) $A_{k+2}=0$, $A_{k+1}=0$ // B (k+2 bit multiplicand) $B_0=0$ // n (k bit modulus) // Output $S = A \times B \times r^{-1} \mod n$, where $r = 2^{k+3}$ 1. S=0; 2. for i=0 to k+2
 - 3. $\{q[i]=S_0 \mod 2;$
 - 4. $S=(S + A_i \times B + q[i] \times n)/2;$
 - return S; 5

Step 4 in algorithm 3 requires addition of long operands. To avoid long carry propagation delay, carry save logic can be applied to solve the problem. Therefore step 3 and 4

$$q[i] = (S1_0 + S2_0) \mod 2;$$
 (3)

S1, S2 =
$$(S1+S2+A_i \times (B1+B2) + q[i] \times n)/2;$$
 (4)

In [13] a Modified 4:2 CSA Montgomery has been presented where the input and output operands are in carry save format. Each iteration computes quotient for next iteration. It has two levels of carry save logic with additional control logic to determine the operands for addition. Algorithm 4 considers the Walter approach and extends the operands and bit width of r accordingly for the design in [13].

Algorithm 4 Modified 4:2 Carry Save Montgomery Modular Multiplication (A1, A2, B1, B2, n)

//Inputs A1, A2 (carry save format of multiplier, k+3 bits.

- $// A1_{k+2}=0, A2_{k+2}=0, A1_{k+1}=0, A2_{k+1}=0$
- // B1, B2 (k+2 bit multiplicand B10=0, B20=0
- // n (k bits modulus). $r=2^{k+3}$
- // Output S1[k+3], S2[k+3]
- $// = (A1+A2) \times (B1+B2) \times r^{-1} \mod n$
- 1a. (S1[0], S2[0]) = (0,0)
- 1b. P1[-1]=0, P2[-1]=0;
- 1c. carry=0;
- 1d. D1, D2= CSR (B1+B2+n)
- /*Pre-computation of operands */
- 1e. $q[0]=0; // S1[0]_0 \oplus S2[0]_0$
- 1f. (carry, $A_0 = A1_0 + A2_0 + carry$);
- 2a. for i in 0 to k+2 loop
- 2b. if $(A_i=0 \text{ and } q[i]=0)$ then P1[i]=0, P2[i]=0; elsif($A_i=1$ and q[i]=0) then P1[i]=B1, P2[i]=B2; elsif($A_i=0$ and q[i]=1) then P1[i]=0, P2[i]=n; else P1[i]=D1, P2[i]=D2; endif;
- 2c. S1[i+1], S2[i+1]
- =CSR(S1[i]+S2[i]+P1[i]+P2[i])/2;
- 2d. $q[i+1]=(S1[i+1]_0 \oplus S2[i+1]_0);$
- 2e. (carry, A_{i+1})= $A1_{i+1}$ + $A2_{i+1}$ +carry);
- end loop;
- /* Steps 2a-2d are parallel to step 2e */ 3.return (S1[k+3], S2[k+3]);

The critical path delay in algorithm 4 is 4:1 MUX + 2Full Adders+1XOR. It requires only 1 XOR delay to compute quotient whereas 4:2 and 5:2 CSA Montgomery designs [5], [6] have quotient delay of 2 XOR + 1 AND. In [9], the authors used 4:2 compressor to reduce critical path delay in Montgomery designs [5], [6]. The addition operation S1[i] + S2[i] + P1[i] + P2[i] with 4:2 compressor [14] is shown in Fig 1. In this paper, a Modified Montgomery design is proposed which uses 4:2 compressor for addition of operands S1[i]+S2[i]+P1[i]+P2[i] such that logic operations are partitioned over two iterations to perform parallel computations.

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Fig. 1 Addition with 4:2 compressor

III. PROPOSED MONTGOMERY MODULAR MULTIPLICATION

The features of proposed design are:

 There are 2 phases: pre-computation and computation. Modular Multiplication iterations span from i =0 to k+2 with additional iteration i= -1. During this iteration shift down of result gives the same value 0

- (2) In pre-computation three operands B1, B2 and n are added. Intermediate result BX is stored in register. Also DX is computed. BX and DX are used when operands are added.
- (3) Each ith iteration computes S1[i+1], S2[i+1]= S1[i]+S2[i]+P1[i]+P2[i] with 4:2 compressor by applying 2P approach: parallelism and partitioning.
- (4) Each iteration computes quotient for next iteration q[i+1] and multiplier bit A_{i+2} .
- (5) Also each iteration computes intermediate results SP[i], MC[i] and SX[i+1] and PX[i+1]
- (6) Multiplier bit A_{i+1} and quotient bit q[i+1] determines operands P1[i+1], P2[i+1] and PX[i+1] for next iteration.

<u>Algorithm 5 Proposed Modified 4:2 Compressor</u> <u>Montgomery Modular Multiplication (A1, A2, B1, B2, n)</u>

```
// Inputs: A1, A2 (carry save format of multiplier,

// k+3 bits)

// A1<sub>k+2</sub>=0, A2<sub>k+2</sub>=0, A1<sub>k+1</sub>=0, A2<sub>k+1</sub>=0

// B1, B2 (k+2 bit multiplicand) B1<sub>0</sub>= 0, B2<sub>0</sub>= 0

// n (k bits modulus), r=2<sup>k+3</sup>

// Output

//S1[k+3],S2[k+3]=(A1+A2)×(B1+B2)×r<sup>-1</sup> mod n

1.1a. (S1[-1], S2[-1])= (0,0)

1b. P1[-1]=0, P2[-1]=0, PX[-1]=0, SX[-1]=0

1c. carry=0

2. 2a. BX=B1\oplus B2;

2b. D1= (BX • n) + (BX • B1);

2c. D2= BX \oplus n;
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2d. DX= D1 \oplus D2; /* D1, D2=CSR (B1 + B2 + n) */ 2e. carry, $A_0 = A1_0 + A2_0 + carry$; 3. for i in -1 to k+2 loop 3a. $SP[i] = SX[i] \oplus PX[i];$ parallel $MC[i] = (SX[i] \bullet P1[i]) + (\overline{SX[\iota]} \bullet S1[i]);$ 3b. $S2[i+1] = (SP[i] \oplus (MC[i],0))/2;$ parallel $S1[i+1]=((SP[i] \bullet (MC[i],0)) + (\overline{SP[\iota]} \bullet P2[i]))/2;$ 3c. $SX[i+1] = S1[i+1] \oplus S2[i+1];$ parallel $\{q[i+1] = S1[i+1]_0 \oplus S2[i+1]_0;$ if $(A_{i+1}=0 \text{ and } q[i+1]=0)$ then P1[i+1]=0; P2[i+1]=0; PX[i+1]=0; elsif ($A_{i+1}=1$ and q[i+1]=0) then P1[i+1]=B1; P2[i+1]=B2; PX[i+1]=BX; $elsif(A_{i+1}=0 \text{ and } q[i+1]=1)$ then P1[i+1]=0; P2[i+1]=n; PX[i+1]=n; else P1[i+1]=D1; P2[i+1]=D2; PX[i+1]=DX end if: ł

parallel carry, $A_{i+2} = A1_{i+2} + A2_{i+2} + carry;$

4. Return (S1 [k+3], S2[k+3]);

/* Steps 3a to 3c are parallel with computation of A_{i+2} */

During pre-computation, D1 and D2 are computed with multiplexer in carry path. Intermediate result, BX is used for 4:2 addition when multiplier bit is 1 and quotient bit is 0. Also DX is computed and used when both multiplier and quotient bits are 1.

Step 3 of algorithm 5 iterates to perform the computations. Each iteration performs lower 2 levels of addition and first level of addition for next iteration of Fig. 1. Based on quotient and multiplier bits of next iteration P1, P2 and PX are determined.

- P1[i+1]=0, P2[i+1]=0 then PX[i+1]=0 (0 ⊕ 0=0)
- P1[i+1]=B1, P2[i+1]=B2
- then $PX[i+1]=BX (B1 \oplus B2=BX)$ • P1[i+1]=0, P2[i+1]=n
- P1[i+1]=0, P2[i+1]=nthen PX[i+1]=n (0 \oplus n=n) • P1[i+1]=D1, P2[i+1]=D2
- P1[i+1]=D1, P2[i+1]=D2then PX[i+1]=DX (D1 \oplus D2=DX)

IV. IMPLEMENTATION RESULTS AND ANALYSIS

A. Synthesis Results

The proposed Montgomery design and RSA modular exponentiation (encryption) are coded in VHDL and synthesized in XILINX ISE 8.1i (Virtex 2) and XILINX ISE 12.4 (Virtex 5 XC5VLX50 package FF1153 speed -3). The synthesis results of proposed Montgomery design for operand size 512, 1024 and 2048 bits are in Tables I-III. Area is in terms of number of slices. Frequency is in MHz. Area and frequency (minimum period) are generated in

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synthesis report. Throughput is calculated as bit length multiplied by the frequency and divided by number of clock cycles. The proposed Montgomery design takes k+6 clock cycles where k is bit length of operands. Table I give detailed area results on Virtex 2 and Virtex 5 FPGAs.

TABLE I AREA RESULTS FOR PROPOSED MONTGOMERY ON VIRTEY 2 FPG A S

| AREA RESOLISTOR I ROLOSED MONTGOMERT ON VIRTEA 211 GAS | | | | | | |
|--|--------------------|--------|------------------|-------|-------|--|
| Bit Len | FPGA Technology | Slices | Slice Flip Flops | LUTs | Freq | |
| Len | rechnology | | | | | |
| 512 | XC2V1500 | 4211 | 5288 | 7955 | 253.7 | |
| 1024 | XC2V3000 | 9213 | 10963 | 16917 | 250.5 | |
| 2048 | XC2V4000 | 17140 | 21544 | 32001 | 246.3 | |
| | | | | | | |

| TABLE II Area Results for Proposed Montgomery on Virtex 5 FPGAS | | | | | | |
|--|--------------|------------------|---------------|-------|----------------|--|
| Bit Len | FPGA Tech | Slice Flip Flops | Slice LUTs | Freq | Throu ghput | |
| 512 | XC5VLX50 | 5142 | 4637 | 534.7 | 528.5 | |
| 1024 | XC5VLX50 | 10267 | 9247 | 530.7 | 527.6 | |
| 2048 | XC5VLX50 | 20509 | 18463 | 530.7 | 529.1 | |

Tables I and II show that when the proposed design is implemented on Virtex 2 and Virtex 5 FPGAs, there is little difference in number of slice flip flops but the difference in LUTs is large. Each slice on Virtex 2 FPGA has two 4 input function generator which can be programmed as 4 input LUTs. Whereas there are four 6 input LUTs in SLICEL and SLICEM on Virtex 5 FPGAs. Therefore to implement a function on Virtex 2 requires more LUT combining and hence more number of LUTs to implement a design. The frequency results are more than double on Virtex 5 FPGAs. This is due to improved version of wiring architecture named "Diagonally symmetric interconnect pattern" [15]. This type of architecture reduces the delays, thus making more logic blocks accessible with a smaller number of hops (switch blocks).

TABLE III FPGA Implementation of Montgomery Modular Multipliers

| | Bit | FPGA | Area ,A | Freq | Throughp | T/A |
|---------|------|----------|----------|--------|------------|---------|
| | Len | Tech | (Slices) | (MHz) | ut Rate, T | (Mbps/ |
| | | | | | (Mbps) | Slices) |
| $[6]^1$ | 512 | XC2V1500 | 5170 | 126.7 | 126.4 | .024 |
| | 1024 | XC2V3000 | 10332 | 101.7 | 101.6 | .009 |
| $[6]^2$ | 512 | XC2V1500 | 5782 | 122.03 | 121.5 | .021 |
| | 1024 | XC2V3000 | 11520 | 111.3 | 111.1 | .009 |
| [7] | 512 | XC2V1500 | 1678 | 89.3 | 29.71 | .017 |
| | 1024 | XC2V3000 | 3334 | 88.9 | 29.60 | .008 |
| | 2048 | XC2V6000 | 6782 | 87.1 | 29.02 | .004 |
| [8] | 512 | XC2V1500 | 3125 | 72.1 | 71.82 | .022 |
| | 1024 | XC2V3000 | 6243 | 79.2 | 79.05 | .012 |
| [10] | 512 | XC2V3000 | 2902 | 121.5 | 120.3 | .041 |
| | 1024 | XC2V3000 | 4512 | 114.2 | 113.4 | .025 |
| [11] | 512 | XC2V1500 | 4029 | 221.9 | 220.2 | .054 |
| | 1024 | XC2V3000 | 8000 | 219.06 | 218.2 | .027 |
| our | 512 | XC2V1500 | 4211 | 253.7 | 250.8 | .059 |
| | 1024 | XC2V3000 | 9213 | 250.5 | 249.07 | .027 |
| | 2048 | XC2V4000 | 17140 | 246.3 | 245.61 | .014 |

1: designed with Five-to-two CSA

²: designed with four-to-two CSA

Table III compares the results with related implementation on Virtex 2 FPGA. It shows that proposed design has more than double the frequency and throughput when compared to 4:2 CSA Montgomery [6]² proposed by McIvor. This is because the critical path delay of proposed design is 3 XOR+4:1 MUX as compared to 4:1MUX+2 Full adders + 2 XOR+ 1 AND of [6]². Proposed Montgomery design has highest frequency amongst the designs where no output/input format conversion is done at the end of modular multiplication [5]-[9], [11]. When compared with [10] where the format conversion is done using carry save addition, our frequency and throughput is double at the cost of area. The design in [16] is a semisystolic. Also the approach in [11], [16] are only applicable for RSA MSB method. The proposed design can be used in both RSA MSB and LSB binary modular exponentiation methods. Table III shows our design has highest throughput/area ration for 512 bits.

TABLE IV

| | RSA MODULAR EXPONENTIATION ON VIRTEX 2 FPGAS | | | | | |
|------|--|------------|--------|------------|-------|-------|
| Bit | H/L | FPGA | Slices | Slice Flip | LUTs | Freq |
| Len | | Technology | | Flops | | _ |
| 512 | Н | XC2V3000 | 6270 | 7960 | 11760 | 224.6 |
| | L | XC2V3000 | 11290 | 13506 | 21488 | 224.5 |
| 1024 | Н | XC2V6000 | 12930 | 16296 | 24005 | 222.6 |
| | L | XC2V6000 | 24259 | 28231 | 44829 | 222.1 |

| TABLE V | | | | | | |
|---------|--------|---------------|----------------|------------|--------|--|
| | RSA Mo | DULAR EXPONEN | TIATION ON VIR | tex 5 FPGA | As | |
| Bit | H/L | FPGA | Slice Flip | LUTs | Freq | |
| Len | | Technology | Flops | | | |
| 512 | Н | XC5VLX50 | 7795 | 7479 | 491.64 | |
| | L | XC5VLX50 | 12932 | 13124 | 496.03 | |
| 1024 | Н | XC5VLX50 | 15478 | 14888 | 441.2 | |
| | L | XC5VLX50 | 25736 | 27137 | 445.05 | |

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|---------------------------------------|---------|-----|----------|------------------|-----------|----------------------|-----------------|
| | Bit Len | H/L | FPGA | Area, A (Slices) | Fre (MHz) | Throughput, T (Mbps) | T/A Kbps/slices |
| [6]] | 512 | L | XC2V3000 | 11304 | 102.31 | 5.10 | 0.45 |
| [6]. 1024 | 1024 | L | XC2V6000 | 23208 | 95.90 | 4.79 | 0.20 |
| [11] | 512 | Н | XC2V3000 | 6294 | 168.38 | 9.28 | 1.47 |
| [11] 102 | 1024 | Н | XC2V6000 | 12537 | 152.49 | 8.44 | 0.67 |
| [16] | 512 | Н | XC2V3000 | 7832 | 218.72 | 11.87 | 1.51 |
| 1024 | 1024 | Н | XC2V6000 | 15826 | 215.83 | 11.85 | 0.74 |
| | 512 | Н | XC2V3000 | 6270 | 224.65 | 11.68 | 1.86 |
| 512 | 312 | L | XC2V3000 | 11290 | 224.58 | 13.05 | 1.15 |
| Our | 1024 | Н | XC2V6000 | 12930 | 222.69 | 11.65 | 0.90 |
| 1024 | 1024 | L | XC2V6000 | 24259 | 222.12 | 12.98 | 0.53 |

| TABLE VI |
|---------------------------------------|
| RESULTS OF RSA MODULAR EXPONENTIATION |

¹: designed with Five-to-two CSA

RSA modular exponentiation (encryption) is implemented using proposed Modified Montgomery design. Both LSB and MSB binary method of RSA are coded in VHDL. Synthesis result for RSA MSB (H) and LSB (L) for 512 and 1024 bits are given in Tables IV-VI. Detailed results for RSA modular exponentiation are given in Tables IV and V. For implementation the bits for exponent are taken 17 bits. Tables IV and V show the difference in LUTs and frequency due to different FPGA technology. The RSA design in this paper has frequency higher than [6], [11] and [16]. Also area results for RSA MSB (H) are lower than [16] since we are reusing registers for storing the final result instead of new registers (only in MSB method). RSA encryption can be done faster by choosing the values for e=3, 17, or 65537(2¹⁶+1) [17]. Binary representation of 65537 is 100000000000001. Taking this value and calculating the number of Montgomery modular multiplication (MMM) cycles in modular exponentiation gives:

MSB design- 17 squarings + 2 multiplications= 19

Montgomery cycles in MSB= $19 \times (k + 6)$

LSB design- 17 squarings + 2 multiplications

(Squarings and multiplications can be done in parallel)=17

Montgomery cycles in LSB= $17 \times (k+6)$

Throughput of RSA given in tables is calculated using 19 \times (k+6) MMM cycles for MSB and 17 \times (k+6) MMM cycles for LSB binary modular exponentiation. The throughput in [16] is better than our RSA design. The H algorithm of binary method for RSA modular exponentiation in [11], [16] adds carry save values of message M to get binary M. This requires additional conversion cycles. Thus our overall performance will be better when compared with [16]. If throughput / area is taken as efficiency factor then our RSA design has highest value among related designs as shown in Table VI.

V. CONCLUSIONS

The proposed Montgomery modular multiplication partitions the logic operations of addition with 4:2 compressor which facilitates parallel computations and reduced delay. Though the area requirements of design are high but the proposed design has high throughput /area ratio. It is suitable for applications where high throughput is required and area is not a limitation.

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