

Transient Heat Transfer Model for Car Body Primer Curing

D. Zabala, N. Sánchez and J. Pinto

Abstract—A transient heat transfer mathematical model for the prediction of temperature distribution in the car body during primer baking has been developed by considering the thermal radiation and convection in the furnace chamber and transient heat conduction governing equations in the car framework. The car cockpit is considered like a structure with six flat plates, four vertical plates representing the car doors and the rear and front panels. The other two flat plates are the car roof and floor. The transient heat conduction in each flat plate is modeled by the lumped capacitance method. Comparison with the experimental data shows that the heat transfer model works well for the prediction of thermal behavior of the car body in the curing furnace, with deviations below 5%.

Keywords—Transient heat transfer, car body, lumped capacitance, primer baking.

I. INTRODUCTION

HEAT transfer modeling in furnaces is a matter of interest in different material science applications [1]-[9] and in automotive industry. In this one, corrosion protection is a major concern during the car body assembly. In some process, heating of the car body is needed after the electro-deposition primer application because it is necessary to achieve a prescribed temperature/time range for proper primer curing or baking. Below that range, the polymerization of the resin is incomplete, and the primer will separate from the car surface and above it, the primer will be burned, affecting the final car painting, producing changes in pigmentation and damaging the resin of the primer, resulting in poor adhesion of following paint layers. Due to the temperature in the furnace chamber, radiation and convection are the modes of heat transfer from the furnace to the car structure. In order to design a new furnace or to improve the performance of existing ones, the modeling of the heat transfer process has to be done accurately.

D. Zabala is professor at the Universidad de Carabobo (CIMEC), Carabobo, Venezuela (corresponding author phone: 58-241-6005000 ext 305210; e-mail: dzabala@uc.edu.ve).

N. Sánchez, was student at Universidad de Carabobo, Carabobo, Venezuela. Recently he worked for Moseinca (e-mail: nelsondavid44@hotmail.com).

J. Pinto was student at Universidad de Carabobo, Carabobo, Venezuela. He is now Business Development Engineer at Kraft Foods Venezuela (e-mail: jesus-pinto@hotmail.com).

II. MATHEMATICAL MODEL

A. Energy Balance in car body

The car cockpit is considered like a structure with six flat plates, four vertical plates representing the car doors and the rear and front panels. The other two flat plates are the car roof and floor. The transient heat conduction in each flat plate is modeled by the lumped capacitance method. Fig.1 shows the energy balance done in each panel of the car body. Radiation is considered to be added to the panel from the furnace walls (Q_{rs}), the other surrounding panels (Q_{rop}) and from the gases inside (Q_{ri}) and outside (Q_{re}) the car body. Also, emitted radiation (Q_{rE}) from the panel is considered. Convection is considered from the gases inside (Q_{ci}) and outside (Q_{ce}) the car body.

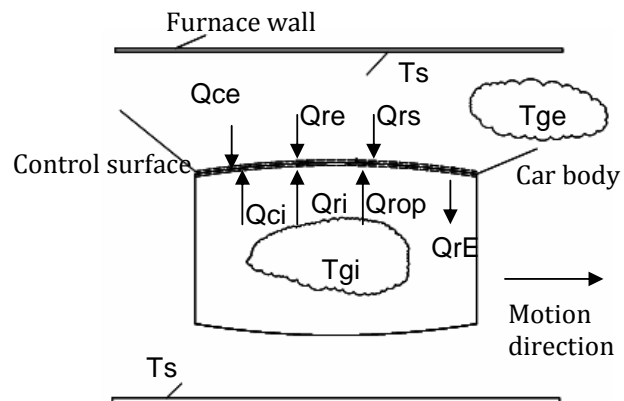


Fig. 1. Energy balance in left side panel

From the Fig. 1, the energy balance for each flat plate “i” is shown in (1):

$$\frac{dE}{dt} = Q_{re} + Q_{ri} + Q_{rs} + Q_{rop} + Q_{ce} + Q_{ci} - Q_{rE} \quad (1)$$

Equation (1) is transformed to (2), in terms of temperature if the lumped capacitance method is valid. This condition is verified by calculation of the Biot number for the car body, as in (3).

$$\rho_a e_i C_a \frac{dT_i}{dt} = \sigma \alpha (T_{ge}^4 + T_{gi}^4 + T_s^4) + h_{ex} (T_{ge} - T_i) + h_{in} (T_{gi} - T_i) + \sigma \alpha \sum_{j=1, j \neq i}^6 T_j^4 - \sigma \epsilon T_i^4 \quad (2)$$

$$Bi = \frac{hL_C}{k} \quad (3)$$

Where the characteristic length L_C is defined as the ratio between the car body volume and surface area, k is the metal thermal conductivity and h is the convection heat transfer coefficient. For each flat plate, L_C is defined according the flat plate orientation. Each flat plate “ i ” is represented by (2), and then the theoretical car body temperature distribution is obtained by solving the system of six coupled ordinary differential equations. These predicted temperatures are compared with the experimental temperatures obtained by the thermocouples attached to the car body. In figure 2, there is an example of the experimental car body temperature measured in different thermocouple locations. The measurement system records the temperature values, so these values were used for comparison with the predicted ones.

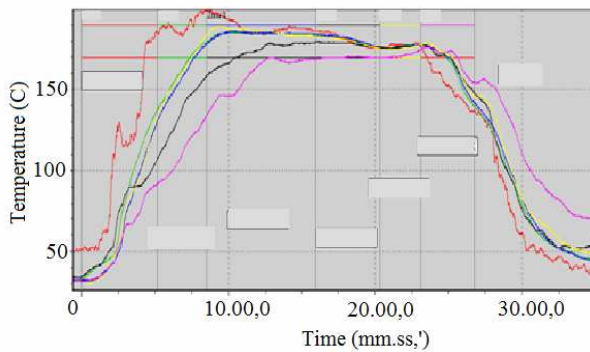


Fig. 2. Car body temperature experimental curves

B. Convection heat transfer coefficients

The convection heat transfer mode inside the furnace is primarily by the diffusion mechanism or natural convection.

Due to the selected structure for the car body parts, two different convection coefficients must be calculated, for vertical and horizontal flat plates. Because the temperature of gas inside the car body is changing during the time, together with the car body temperature, average convection coefficients must be calculated by different average film temperature (T_f). In this way, we obtain convection coefficients, h_{ex} and h_{in} as temperature dependant functions.

Vertical flat plates:

Churchill and Chu correlation [10] can be used for calculation of average Nusselt number (4), valid over the entire range of the Rayleigh number (Ra_L) and depending on the Prandtl number. Also, the Warner and Arpaci correlation

[11], shown in (5), can be used for Nusselt number calculation.

$$Nu_L = \left[0.825 + \frac{0.387 (Ra_L)^{1/4}}{\left(1 + \left(\frac{0.492}{Pr} \right)^{9/16} \right)^{4/27}} \right]^2 \quad (4)$$

$$Nu_L = C (Ra_L)^n \quad (5)$$

In (5), the C and n constants depend on Rayleigh number range. This dimensionless number is defined by (6).

$$C = 0.59, n = 1/4 \text{ if } 10^4 \leq Ra_L \leq 10^9$$

$$C = 0.1, n = 1/3 \text{ if } 10^9 \leq Ra_L \leq 10^{13}$$

$$Ra_L = \frac{\beta g (\Delta T) L^3}{\nu \alpha} \quad (6)$$

Then, the convection heat transfer coefficient is calculated by (7), where k_f is the fluid thermal conductivity at T_f .

$$h = \frac{Nu_L k_f}{L} \quad (7)$$

The characteristic length L , used in (6) and (7), is the plate height for vertical flat plates.

Horizontal flat plates:

The correlation for the average Nusselt number is (5) and the C and n constants depend on the condition of the analyzed surface and the Rayleigh number range, calculated by (6).

For upper surface of hot plate or lower surface of cold plate [12].

$$C = 0.54, n = 1/4 \text{ if } 10^4 \leq Ra_L \leq 10^7$$

$$C = 0.15, n = 1/3 \text{ if } 10^7 \leq Ra_L \leq 10^{11}$$

For lower surface of hot plate or upper surface of cold plate [12].

$$C = 0.27, n = 1/4 \text{ if } 10^5 \leq Ra_L \leq 10^{10}$$

The convection heat transfer coefficient is calculated by (7). In (6) and (7), the characteristic length L is the relationship shown in (8).

$$L = \frac{\text{Area of horizontal plate}}{\text{Perimeter of horizontal plate}} \quad (8)$$

III. RESULTS

External convection heat transfer coefficient, h_{ex} .

The furnace gas temperature, T_{ge} is constant but the car body temperature, T_i changes from the initial value of 301 K to the equilibrium value near 460 K. For that reason, the film

temperature T_f , needed for estimation of gas thermo physical properties, is variable, so the Nusselt number and h_{ex} are variable along the furnace chamber. Gas properties are considered to be similar to air properties (Table I). Results are shown in Tables II to IV. Temperature dependant functions for h_{ex} are shown in Fig. 3 and these values were correlated in terms of the car body temperature (Table V), for being used in (2).

TABLE I
AIR THERMOPHYSICAL PROPERTIES AT T_f , ($T_{ge}=468K$)

T_i (K)	T_f (K)	β (1/K)	α (m^2/s)	ΔT (K)	ν (m^2/s)	K (W/mK)	Pr
303	385.5	0.002594	3.59E-05	165	2.48E-05	3.27E-02	0.6929
333	400.5	0.002496	3.83E-05	135	2.64E-05	3.38E-02	0.69
363	415.5	0.002406	4.11E-05	105	2.83E-05	3.49E-02	0.6888
393	430.5	0.002322	4.37E-05	75	3.00E-05	3.59E-02	0.6876
423	445.5	0.002244	4.64E-05	45	3.19E-05	3.70E-02	0.6864
453	460.5	0.002171	4.92E-05	15	3.37E-05	3.80E-02	0.6856

TABLE II
EXTERNAL CONVECTION COEFF, VERTICAL FLAT PLATES, $*L=0.68m$

T_i (K)	T_f (K)	Ra_L (6)	Nu_L (4)	h_{ex} (W/m ² K)
303	385.5	1.49E+09	138.4	6.65
333	400.5	1.03E+09	123.4	6.13
363	415.5	6.71E+08	108.2	5.55
393	430.5	4.09E+08	93	4.91
423	445.5	2.11E+08	76	4.13
453	460.5	6.05E+07	52.4	2.93

TABLE III
EXTERNAL CONVECTION COEFFICIENT FOR FLOOR, $*L=0.3m$ (8)

T_i (K)	T_f (K)	Ra_L (6)	Nu_L (5)	h_{ex} (W/m ² K)
303	385.5	1.28E+08	75.5	8.23
333	400.5	8.82E+07	66.8	7.52
363	415.5	5.76E+07	57.9	6.74
393	430.5	3.51E+07	49.1	5.89
423	445.5	1.81E+07	39.4	4.85
453	460.5	5.19E+06	25.8	3.27

TABLE IV
EXTERNAL CONVECTION COEFFICIENT FOR ROOF, $*L=0.3m$ (8)

T_i (K)	T_f (K)	Ra_L (6)	Nu_L (5)	h_{ex} (W/m ² K)
303	385.5	1.28E+08	28.7	3.13
333	400.5	8.82E+07	26.2	2.95
363	415.5	5.76E+07	23.5	2.74
393	430.5	3.51E+07	20.8	2.49
423	445.5	1.81E+07	17.6	2.17
453	460.5	5.19E+06	12.9	1.63

*data provided by car manufacturer

TABLE V
CORRELATION FOR EXTERNAL CONVECTIVE COEFFICIENT

Flat Plate	h_{ex} (W/m ² K)=f($T_i(K)$)	R^2
Vertical	$-8.333E-5Ti^2+0.039Ti+2.448$	0.9971
Floor	$-1.069E-4Ti^2+0.049Ti+3.201$	0.9972
Roof	$-4.444E-5Ti^2+0.024Ti-0.0832$	0.9954

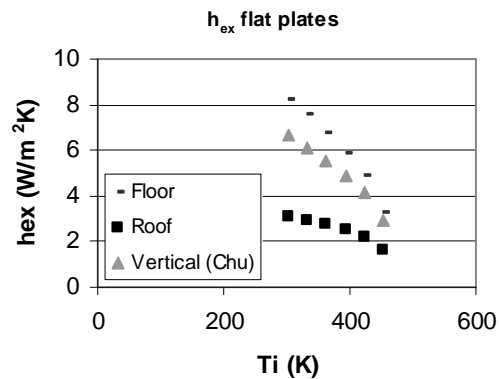


Fig.3. Flat plate h_{ex} vs car body temperature

Internal convection heat transfer coefficient, h_{in} .

The internal gas temperature, T_{gi} is variable with the time and it is experimentally measured with a thermocouple as it is shown in Fig. 4. After approximately 9 minutes, the internal gas temperature reaches a stable value.

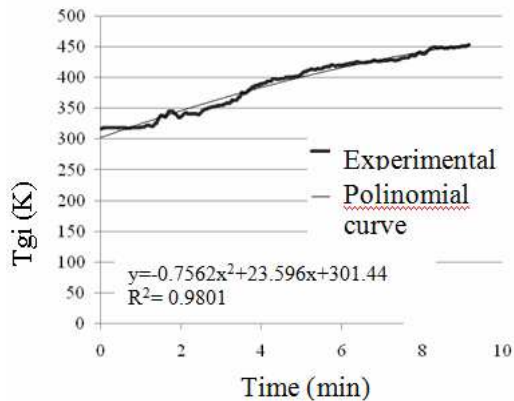


Fig.4. Internal gas temperature (Tgi) vs time

TABLE VI
AIR THERMOPHYSICAL PROPERTIES AT T_f , (T_{gi} VARIABLE)

T_i (K)	T_f (K)	β (1/K)	α (m ² /s)	ΔT (K)	ν (m ² /s)	K (W/mK)	Pr
304	314	0.003185	2.46E-05	19.9	1.73E-05	2.73E-02	0.705
335	350	0.002857	2.99E-05	30.1	2.09E-05	3.00E-02	0.7
367	383.6	0.002607	3.54E-05	33.2	2.45E-05	3.25E-02	0.6934
403	416.1	0.002403	4.11E-05	26.2	2.83E-05	3.49E-02	0.6887
435	443.6	0.002254	4.60E-05	17.2	3.16E-05	3.68E-02	0.6866
450	455	0.002198	4.82E-05	10	3.30E-05	3.76E-02	0.6858

TABLE VII
INTERNAL CONVECTION COEFF, VERTICAL FLAT PLATES, $L=0.68m$

T_i (K)	T_f (K)	Ra_L (6)	Nu_L (4)	h_{in} (W/m ² K)
304	314	4.6E+08	96.7	3.89
335	350	4.23E+08	94.2	4.16
367	383.6	3.07E+08	85.3	4.08
403	416.1	1.67E+08	70.9	3.64
435	443.6	8.25E+07	57.4	3.11
450	455	4.26E+07	47.2	2.61

TABLE VIII
INTERNAL CONVECTION COEFFICIENT FOR FLOOR, $L=0.3m$ (8)

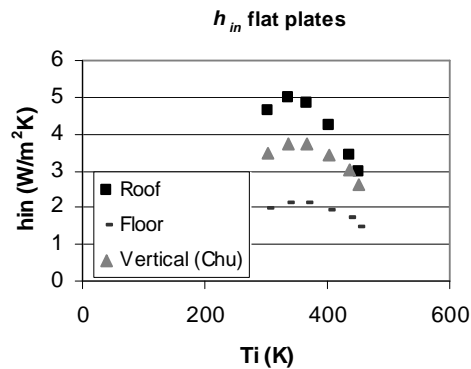
T_i (K)	T_f (K)	Ra_L (6)	Nu_L (5)	h_{in} (W/m ² K)
304	314	3.95E+07	21.4	1.95
335	350	3.64E+07	21	2.1
367	383.6	2.64E+07	19.4	2.1
403	416.1	1.43E+07	16.6	1.93
435	443.6	7.08E+06	13.9	1.71
450	455	3.66E+06	11.8	1.48

TABLE IX
INTERNAL CONVECTION COEFFICIENT FOR ROOF, $L=0.3m$ (8)

T_i (K)	T_f (K)	Ra_L (6)	Nu_L (5)	h_{in} (W/m ² K)
304	314	3.95E+07	51.1	4.66
335	350	3.64E+07	49.7	4.97
367	383.6	2.64E+07	44.6	4.84
403	416.1	1.43E+07	36.4	4.24
435	443.6	7.08E+06	27.9	3.42
450	455	3.66E+06	23.6	2.96

Here, T_f is also variable, so the Nusselt number and h_{in} are variable along the furnace chamber. The air thermophysical properties are shown in Table VI. Results are shown in Tables VII to IX. Temperature dependant functions for h_{in} are shown in Fig. 5 and these values were correlated in terms of the car body temperature (Table X), for being used in (2).

Flat Plate	h_{in} (W/m ² K)=f(T_i (K))	R^2
Vertical	$-1.381E-4T_i^2 + 0.095T_i - 12.353$	0.9953
Roof	$-1.706E-4T_i^2 + 0.117T_i - 14.98$	0.9977
Floor	$-6.566E-5T_i^2 + 0.046T_i - 6.083$	0.9936

Fig. 5. Flat plate h_{inB} vs car body temperature

Biot numbers

The maximum Biot number was calculated for each flat plate, using the highest value of the estimated convective coefficient. Biot values in Table XI are considerably lower than 0.1, so the lumped capacitance method is valid [13].

TABLE XI
MAXIMUM BIOT NUMBER ($k=80.2 \text{ W/mK}$)

Flat Plate	$h \text{ (W/m}^2\text{K)}$	Bi
Vertical	6.65	0.056
Roof	8.23	0.031
Floor	4.97	0.019

Car body temperature

The mathematical model shown in (2) was solved using the 4th order Runge- Kutta method and the temperature for each flat plate is compared with the experimental values (Figures 6 to 11).

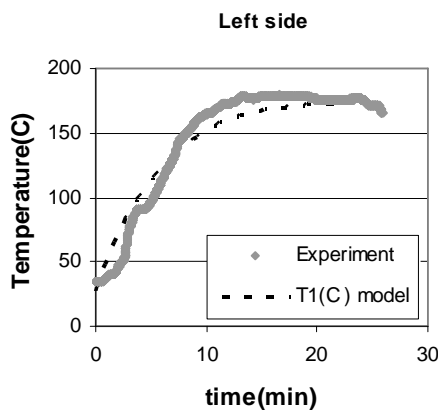


Fig.6. Left side, car body temperature vs time

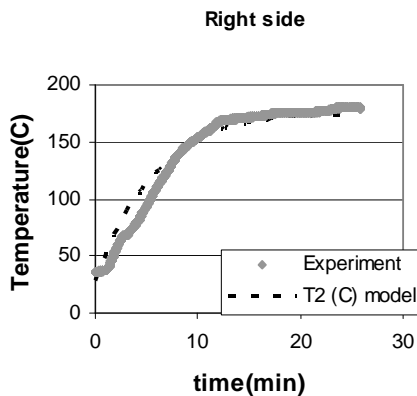


Fig.7. Right side, car body temperature vs time

In general, the model results are in good agreement with the trend in all the experimental curves. The highest deviation (4,7%) was found for the rear panel (Fig. 9) and the minimum deviation (1,4%) was for the floor (Fig. 11), calculated as in (9). These results validate the model and it can be used for evaluating furnace modifications.

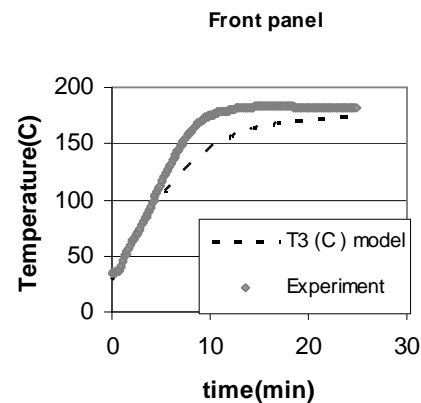


Fig.8. Front side, car body temperature vs time

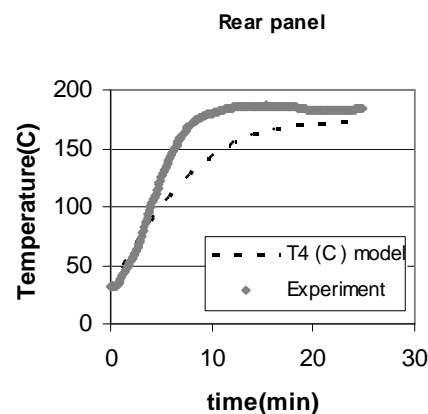


Fig. 9. Rear side, car body temperature vs time

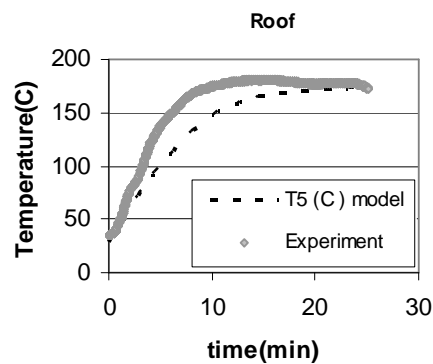


Fig.10. Roof, car body temperature vs time

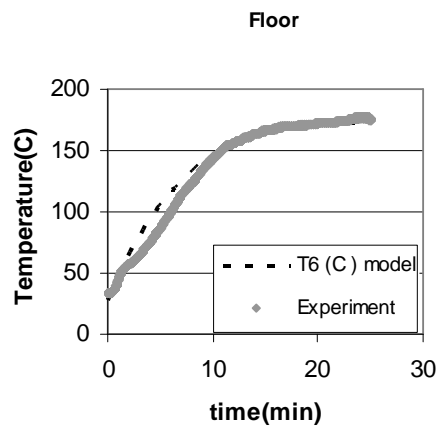


Fig.11. Floor, car body temperature vs time

APPENDIX
TABLE XII
GENERAL DATA

Absorptivity, α	0.101 ^a
Emissivity, ϵ	0.88 ^a
Ca (J/kg K)	447 ^b
ρ (kg/m ³)	7870 ^b
σ (W/m ² K ⁴)	5.67.10 ⁻⁸

^a data provided by primer manufacturer^b data provided by car manufacturer

TABLE XIII
PARTICULAR DATA

Plate	1	2	3	4	5	6
	left	right	front	rear	roof	floor
Thickness (mm)	1	1	1.33	1.44	1	1.4
Initial T (K)	301	301	301	301	301	301

$$\%dev = \frac{\sum_{i=1}^n \left| \frac{T(K)_i \text{exp} - T(K)_i \text{calc}}{T(K)_i \text{exp}} \right|}{n} \times 100 \quad (9)$$

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