

Assessment of Hargreaves Equation for Estimating Monthly Reference Evapotranspiration in the South of Iran

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Abstract—Evapotranspiration is one of the most important components of the hydrological cycle. Evapotranspiration (ET_o) is an important variable in water and energy balances on the earth's surface, and knowledge of the distribution of ET is a key factor in hydrology, climatology, agronomy and ecology studies. Many researchers have a valid relationship, which is a function of climate factors, to estimate the potential evapotranspiration presented to the plant water stress or water loss, prevent. The FAO-Penman method (PM) had been recommended as a standard method. This method requires many data and these data are not available in every area of world. So, other methods should be evaluated for these conditions. When sufficient or reliable data to solve the PM equation are not available then Hargreaves equation can be used. The Hargreaves equation (HG) requires only daily mean, maximum and minimum air temperature extraterrestrial radiation. In this study, Hargreaves method (HG) were evaluated in 12 stations in the North West region of Iran. Results of HG and M.HG methods were compared with results of PM method. Statistical analysis of this comparison showed that calibration process has had significant effect on efficiency of Hargreaves method.

Keywords—Evapotranspiration, Hargreaves equation, FAO-Penman method.

I. INTRODUCTION

THE Penman-Monteith (FAO-56 PM) equation is suggested as the standard method for estimating evapotranspiration (ET_o) by the International Irrigation and Drainage Committee and Food and Agriculture Organization (FAO). On the other hand, the Hargreaves-Samani (HS) equation is an alternative method compared with the FAO-56 PM equation.

In arid areas, the lack of proper management of the erratic precipitation accentuates the problem of aridity. Agriculture should in the foreseeable future gain more value and momentum [16]. Many researchers around the world Penman-Monteith lysimeters as compared to the standard method and the most accurate and reliable method for calculating reference evapotranspiration have been introduced [3]. Evapotranspiration (ET_o) is an important variable in water and energy balances on the earth's surface, and knowledge of the distribution of ET is a key factor in hydrology, climatology,

agronomy and ecology studies [15]. Thus, most irrigation engineers use ET_o and crop coefficients to estimate different crop water requirements [4]. The FAO-Penman method (PM) in estimating ET_o had been recommended as a standard method [1]. This method requires many data and these data are not available in every area of world. The need for full weather data limits the widespread use of the Penman-Monteith [8], [13]. So, other methods that require fewer data should be evaluated for these conditions. In this research the equation of HG calibrate by Penman Monthis method.

Salako found that the daily means of PM ET_o values were significantly correlated with those of the HG method ($P < 0.0001$, r^2 from 0.72-0.93) and pan ET_o values ($P < 0.0001$, r^2 from 0.91-0.93). He also reported that the regression equations developed for three agroecological zones of Nigeria can be used to estimate PM ET_o values for similar climatic zones where data requirements cannot be met but data for the HG or pan method are available [12].

Jabloun and Sahli evaluated the Hargreaves equation. They reported that the results obtained from the comparison of ET_o daily estimates by the Hargreaves equation with FAO-56 PM, estimates taken as reference throughout different Tunisian locations showed a systematic overestimation at inland sites but that at coastal sites, the Hargreaves equation tends to underestimate ET_o values. They suggested that further research would be required to adjust the Hargreaves coefficients to local conditions for obtaining better accuracy [7].

II. MATERIAL AND METHODS

The area under study was the North West region of Iran (Fars Province), between 27.2 and 31.2 N in latitude and between 51.9 and 54.4 E in longitude. This area covers approximately 2592890.16 hectares. The region is categorized as a semiarid climate based on different climate classification that show on Fig. 1. Measured weather data sets we obtained from 12 stations across the study area. The mean annual precipitation for the region ranges from 138 to 856 mm. This climate variability is one of the major constraints facing dry land agriculture. The spatial distribution of selected stations can be seen from Fig. 1. Also, Information about the selected stations is shown in Table I.

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TABLE I
LOCALIZATION, METEOROLOGICAL DATA, AND CLIMATE OF THE 12 SELECTED STATIONS IN THIS STUDY

| Station | Latitude (degree) | Longitude (degree) | Climate (De Martonne) | Elevation a.m.s.l (m) | Records Period | Percipitation (mm) | Tmax (°C) | Tmin (°C) | Tdew (°C) | U10 (Knot) | Rhmean (%) | n (hr) |
|------------|----------------------|-----------------------|-------------------------|--------------------------|-------------------|-----------------------|--------------|--------------|--------------|---------------|---------------|-----------|
| Abadeh | 31.166 | 52.616 | Arid | 2030 | 2005-2012 | 138.5 | 22 | 6.5 | -3 | 16 | 35 | 9.3 |
| Eghlid | 30.883 | 52.716 | Semi – Arid | 2300 | 2008-2012 | 341 | 19.4 | 6.1 | 0.9 | 18 | 32 | 9.1 |
| Boanat | 30.45 | 53.633 | Semi – Arid | 2151 | 2003-2012 | 248.4 | 20.8 | 6.5 | -2.5 | 16 | 34 | 9 |
| Sepidan | 30.283 | 51.983 | Humid | 2200 | 2005-2012 | 856.8 | 19.5 | 9.6 | 1 | 14 | 39 | 9.1 |
| Mavdasht | 29.933 | 52.883 | Semi – Arid | 1620 | 2008-2012 | 504.7 | 23.9 | 11.5 | -1 | 11 | 43 | 9 |
| Izad Khast | 31.55 | 52.116 | Arid | 2142 | 2006-2012 | 159.4 | 20.7 | 7.1 | 0 | 13 | 33 | 9.3 |
| Fasa | 28.95 | 53.65 | Semi – Arid | 1450 | 2004-2012 | 310.4 | 28 | 10.6 | 3.2 | 12 | 40 | 9.3 |
| Lamerd | 27.336 | 53.15 | Arid | 500 | 2009-2012 | 227.8 | 33.8 | 16.8 | 3.3 | 11 | 43 | 9.4 |
| Lar | 27.7 | 54.333 | Arid | 806 | 2007-2012 | 215.2 | 31.7 | 15.1 | 2.3 | 12 | 44 | 9.4 |
| Neyriz | 29.2 | 54.316 | Arid | 1795 | 2007-2012 | 213.3 | 25.7 | 13 | 3 | 11 | 36 | 9.8 |
| Safashahr | 30.616 | 53.166 | Semi – Arid | 2324 | 2002-2012 | 232 | 19.8 | 2.93 | 3.6 | 9.3 | 36.91 | 16.5 |
| Zarghan | 29.783 | 52.716 | Semi – Arid | 1600 | 2005-2012 | 338.7 | 24.6 | 7.3 | 2.5 | 11 | 42.5 | 9 |

Tmin=minimum air temperature, Tmax=maximum air temperature, Tdew=dew point temperature, U10=wind speed at 10 m height, RHmean=mean relative humidity, n=mean monthly total sunshine hours. **The classification of the climatic regions based on De Martonne method



Fig. 1 Meteorological stations used in the study

To calculate wind speed at two-meter height, the equation proposed by Allen et al. (1998) was used [1]:

$$u_2 = \frac{4.87 \cdot u_{10}}{\ln(67.8 \cdot 10 - 5.42)} \quad (1)$$

where U_2 is the average 24-hour wind speed at a height of 2 m and U_{10} is average 24-hour wind speed at a height of 10 m.

The solar radiation was calculated by using:

$$R_s = \left(0.25 + 0.5 \frac{n}{N}\right) \cdot R_a \quad (2)$$

where R_s is the net solar radiation ($\text{MJ m}^{-2} \text{ day}^{-1}$), N is the maximum possible sunshine hours (h), n is the number of actual sunshine hours (h), and R_a is the extraterrestrial radiation ($\text{MJ m}^{-2} \text{ day}^{-1}$).

Allen proposed the FAO-Penman-Monteith method as a standard method to estimate, evaluate and calibrate the ET reference value. This method has been used by many researchers [2], [4], [9]-[11] and the equation can be rewritten as:

$$ET = \frac{0.408 \Delta (R_n - G) + \gamma \frac{900}{T + 273} u_2 (e_s - e_a)}{\Delta + \gamma (1 + 0.34 u_2)} \quad (3)$$

where ETo is the reference evapotranspiration (mm day^{-1}), R_n , G , and T are net radiation values at the crop surface ($\text{MJ m}^{-2} \text{ day}^{-1}$), soil heat flux density ($\text{MJ m}^{-2} \text{ day}^{-1}$), and mean daily air temperature at 2 m height ($^{\circ}\text{C}$), respectively. Also, u_2 , e_s , e_a , $(e_s - e_a)$, Δ , and γ are wind speed at 2 m height (m s^{-1}), saturation vapor pressure (kPa), actual vapor pressure (kPa), saturation vapor pressure deficit (kPa), slope of the saturation vapor pressure curve ($\text{kPa}/^{\circ}\text{C}$), and psychrometric constant ($\text{kPa}/^{\circ}\text{C}$), respectively.

The Hargreaves equation can be written as [5], [6]:

$$ET_o = C(T_{\text{mean}} + 17.8)(T_{\text{max}} - T_{\text{min}})^{0.5} R_a \quad (4)$$

where T_{mean} , T_{max} and T_{min} are mean, maximum and minimum temperatures ($^{\circ}\text{C}$), respectively, and R_a is extraterrestrial radiation ($\text{MJ m}^{-2} \text{ day}^{-1}$) converted to equivalent evaporation in mm day^{-1} with a factor of 0.408.

The climate of each region was determined by using the De Martonne model as [14]:

$$I = \frac{P}{T + 10} \quad (5)$$

where P is mean of annual precipitation (mm) T ($^{\circ}\text{C}$) is mean of annual temperature, I is the Demartonne drought index.

To estimates by the PM and HG models were compared using simple error analysis and the linear regression method. Both methods were compared before and after adjustments were applied. For each location, the following parameters were also calculated [13]: root mean square error (RMSE).

$$RMSE = \left[\frac{\sum_{i=1}^n (X_{\text{Harg}} - X_{\text{PM}})^2}{n} \right]^{1/2} \quad (6)$$

where X_{Harg} , X_{pm} , and n are the evaporation values estimated by the Hargreaves and Penman- Monteith methods and data number, respectively.

III. RESULTS AND DISCUSSION

Monthly ETo values for all the stations were estimated by the FAO-Penman-Monteith (PM) and Hargreaves-Samani (HG) methods, and the results were compared. Table II shows the monthly and annual values of RMSE. A comparison shows that the lowest monthly RMSE index belonged to the Sepidan Station, with humid climate and with a value of 0.095 in December. The highest RMSE, with a value of 3.132, was recorded at the Fasa Station under a Semi-Arid climate in April. Annually, the highest and lowest RMSE values of 1.407 and 0.467 were at the Eghlid and Abadeh stations, with Semi-Arid and Arid climates, respectively. The results showed that the RMSE values in warm months were higher than those as presented in Table III, the monthly and yearly values of the C coefficients in the HG method were estimated. For the monthly results, the lowest value of C was 0.0018 for (Zarghan) Station in October, while it was for (Izadkhash) Station in Jan. Zarghan were located in semi-arid climate and Izadkhash were located in arid climate. Also, as shown in

Table III, the highest C value, 0.0042, was obtained for Lar Station under an arid climate in April.

The annual results showed that the lowest and highest C values were obtained for Boanat and Lar Stations, 0.0023 and 0.0029, respectively. According to Table III annual C coefficient was different for each station. The lowest C value was obtained at Zarghan Station with a value of 0.0018 in a Semi-Arid, while the greatest difference was obtained at Lar, Safashahr, Neyriz, Abadeh Stations, with a Different values. The climate at the Lar Station is Arid, which of Zarghan is semi-arid. As Table III shows, C coefficients were lower than 0.0023 for Izadkhash, Zarghan, Marvdasht, safashahr, and Lamerd Stations, all with arid climate, and Sepidan station with humid climate. This implies that the ETo values estimated by the Hargreaves method were higher than those by the Penman-Monteith method. For stations with C coefficient higher than 0.0023, the ETo values estimated by the Hargreaves method were lower than those by Penman-Monteith method.

TABLE II
THE VALUES OF RMSE BETWEEN ETO-HARG AND ETO-PM

| Station | jan | feb | mar | apr | may | june | july | aug | sep | Oct | nov | dec | yearly |
|------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|-------|--------|
| Abadeh | 0.142 | 0.489 | 0.377 | 0.422 | 0.486 | 0.625 | 0.457 | 1.015 | 0.268 | 0.387 | 0.309 | 0.179 | 0.467 |
| Eghlid | 0.154 | 0.672 | 0.253 | 0.98 | 0.771 | 0.717 | 0.468 | 0.869 | 0.358 | 0.637 | 0.464 | 0.27 | 1.047 |
| Boanat | 0.291 | 0.767 | 0.228 | 1.294 | 1.082 | 0.748 | 0.958 | 0.915 | 0.662 | 0.844 | 0.507 | 0.482 | 0.918 |
| Sepidan | 0.142 | 0.154 | 0.291 | 0.384 | 0.499 | 0.815 | 0.714 | 0.682 | 0.623 | 0.537 | 0.15 | 0.095 | 0.489 |
| Mavdasht | 0.499 | 1.198 | 0.494 | 2.862 | 1.438 | 1.018 | 1.405 | 0.406 | 1.058 | 1.037 | 1.208 | 1.167 | 0.991 |
| Izad Khash | 0.815 | 1.554 | 0.491 | 2.575 | 1.14 | 1.158 | 1.414 | 0.463 | 1.237 | 0.782 | 1.348 | 1.492 | 0.857 |
| Fasa | 0.714 | 1.835 | 0.309 | 3.132 | 1.428 | 1.214 | 1.316 | 0.646 | 0.817 | 1.027 | 1.264 | 1.463 | 0.707 |
| Lamerd | 0.682 | 1.754 | 0.35 | 3.026 | 1.65 | 1.431 | 1.018 | 1.482 | 0.605 | 1.246 | 1.21 | 0.722 | 0.688 |
| Lar | 0.623 | 1.494 | 0.492 | 2.121 | 1.352 | 1.351 | 0.912 | 0.747 | 0.548 | 1.089 | 0.84 | 0.458 | 0.826 |
| Neyriz | 0.537 | 0.825 | 0.134 | 0.971 | 0.794 | 0.851 | 0.619 | 0.496 | 0.362 | 0.576 | 0.447 | 0.289 | 0.955 |
| Safashahr | 0.15 | 0.586 | 0.116 | 0.572 | 0.456 | 0.656 | 0.354 | 0.808 | 0.29 | 0.371 | 0.198 | 0.221 | 0.606 |
| Zarghan | 0.095 | 1.15 | 0.334 | 1.946 | 1.101 | 0.968 | 0.952 | 0.89 | 0.684 | 0.826 | 0.849 | 0.799 | 0.724 |

TABLE III
THE MONTHLY C VALUES IN THE HG METHOD FOR DIFFERENT MONTHS FOR INVESTIGATED STATION

| Station | Jan | Feb | Mar | Apr | May | June | July | Aug | Sep | Oct | Nov | Dec | yearly |
|------------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| Abadeh | 0.0021 | 0.003 | 0.0025 | 0.0032 | 0.0034 | 0.0032 | 0.0025 | 0.0034 | 0.0023 | 0.0022 | 0.0029 | 0.0028 | 0.0025 |
| Eghlid | 0.0023 | 0.0029 | 0.0024 | 0.0034 | 0.0032 | 0.003 | 0.0024 | 0.0031 | 0.0022 | 0.0021 | 0.0029 | 0.0027 | 0.0024 |
| Boanat | 0.0024 | 0.0027 | 0.0023 | 0.0033 | 0.0031 | 0.0027 | 0.0024 | 0.0028 | 0.0021 | 0.002 | 0.0027 | 0.0027 | 0.0023 |
| Sepidan | 0.0021 | 0.0027 | 0.0023 | 0.0032 | 0.0029 | 0.0026 | 0.0023 | 0.0027 | 0.0021 | 0.002 | 0.0026 | 0.0028 | 0.0024 |
| Mavdasht | 0.0021 | 0.0027 | 0.0022 | 0.0035 | 0.0028 | 0.0026 | 0.0024 | 0.0025 | 0.0021 | 0.0019 | 0.0027 | 0.0026 | 0.0026 |
| Izad Khash | 0.002 | 0.0027 | 0.0022 | 0.0033 | 0.0027 | 0.0027 | 0.0024 | 0.0024 | 0.0022 | 0.0019 | 0.0026 | 0.0026 | 0.0029 |
| Fasa | 0.0021 | 0.0029 | 0.0022 | 0.0035 | 0.0028 | 0.0027 | 0.0023 | 0.0024 | 0.0022 | 0.0019 | 0.0027 | 0.0025 | 0.0029 |
| Lamerd | 0.0021 | 0.0031 | 0.0022 | 0.0039 | 0.0032 | 0.0029 | 0.0024 | 0.0025 | 0.0023 | 0.0019 | 0.0029 | 0.0028 | 0.0028 |
| Lar | 0.0023 | 0.0034 | 0.0026 | 0.0042 | 0.0035 | 0.0032 | 0.0025 | 0.0032 | 0.0023 | 0.0021 | 0.0034 | 0.0033 | 0.0029 |
| Neyriz | 0.0025 | 0.0034 | 0.0023 | 0.004 | 0.0037 | 0.0034 | 0.0025 | 0.0032 | 0.0023 | 0.002 | 0.0033 | 0.0032 | 0.0027 |
| Safashahr | 0.0024 | 0.0034 | 0.0022 | 0.0038 | 0.0036 | 0.0035 | 0.0023 | 0.0033 | 0.0022 | 0.0019 | 0.003 | 0.0025 | 0.0023 |
| Zarghan | 0.0022 | 0.0028 | 0.0023 | 0.0035 | 0.0029 | 0.0027 | 0.0024 | 0.0026 | 0.0028 | 0.0018 | 0.0028 | 0.0027 | 0.0027 |

The result of this investigation indicated that both monthly and yearly means by the Hargreaves method were significantly correlated with those of the Penman-Monteith method at all available recording stations in North of Fars Province Iran); hence, it is possible to predict monthly and yearly ETo values precisely in other areas where the required data for the Penman-Monteith estimations are unavailable and

only maximum and minimum air temperatures have been recorded.

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