

# A Predictive control based on Neural Network for Proton Exchange Membrane Fuel Cell

M. Sedighizadeh, M. Rezaei, V. Najmi

**Abstract**—The Proton Exchange Membrane Fuel Cell (PEMFC) control system has an important effect on operation of cell. Traditional controllers couldn't lead to acceptable responses because of time- change, long- hysteresis, uncertainty, strong- coupling and nonlinear characteristics of PEMFCs, so an intelligent or adaptive controller is needed. In this paper a neural network predictive controller have been designed to control the voltage of at the presence of fluctuations of temperature. The results of implementation of this designed NN Predictive controller on a dynamic electrochemical model of a small size 5 KW, PEM fuel cell have been simulated by MATLAB/SIMULINK.

**Keywords**—PEMFC, Neural Network, Predictive Control..

## I. INTRODUCTION

As one of the most promising power supply in the future, fuel cell is drawing the attention of the governments all over the world, for it has a lot of excellent characteristics such as high efficiency, low energy consumed, friendly to environment and so on [1]. Especially for the PEMFC (Proton Exchange Membrane Fuel Cell), it has high ratio power and high ratio energy, and can start up quickly in room temperature, with no electrolyte leaking and convenient draining. The PEMFC therefore has been applied into electric vehicle, portable power supply; disperse power station and other fields. So it has shown a great future [2].

Because of amending of PEMFC's performance and increasing safety and reliability a satisfying control on PEMFC must be done. Traditional controllers couldn't lead to acceptable responses because of time- change, Long-hysteresis, uncertainty, strong-coupling and nonlinear characteristics of PEMFCs. So an intelligent or adaptive controller is needed. In this paper a neural network predictive controller have been designed to control the voltage of fuel cell with varying load, temperature at the presence of fluctuations.

The considered model in this paper predicts the FC stack performance against situations commonly encountered in

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electrical power generation systems, like insertion and rejection of loads [3]. The voltage of cell is output and pressure of oxygen, pressure of hydrogen, temperature and the load current are inputs. This paper focuses on temperature and control affect of it on output voltage of cell. The input fluctuations affect the output voltage greatly and these fluctuations must be controlled.

This paper is arranged as follows: the next section reviews the considered PEMFC's model, simulates fuel cell by MATLAB/SIMULINK and shows polarization curve of simulated cell, section III introduces NN predictive controller and it's justification with the PEMFC's considered model, section IV shows the results of implementation of this designed NN Predictive controller. Section V is conclusions.

## II. AN ELECTROCHEMICAL-BASED FUEL CELL

Operation of PEMFC is described by polarization curve that shows voltage against current. Main parameters affect polarization curve are: Pressure of hydrogen , Pressure of oxygen, Temperature, Amount of humor

The PEMFC internal electrochemical reaction is the process that combines hydrogen and oxygen over a platinum catalyst to produce water, heat and electricity. The PEMFC mechanism is shown in Figure1.

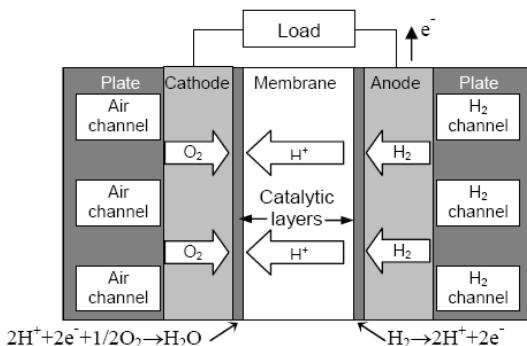
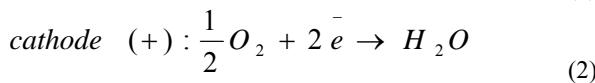
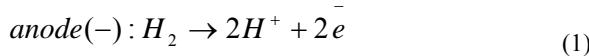


Fig. 1 Schematic diagram of PEMFC mechanism

In the presence of the activator-platinum, the molecules of  $H_2$  in anode of PEMFC discharge electrons to lines and become  $H$ -ions, meanwhile the molecules of  $O_2$  in the cathode receive the electrons from lines as well as protons from PEM, and so the molecules of water are produced. The electrode reaction equations are as follows:



Different mathematical models have been devised to simulate the behavior of PEMFC. Some are based on curve-fitting experiments [4], others are semi-empirical models that combine experimental data with parametric equations adjusted by comparison with cells physical variables like pressure and temperature [5]. In both cases, the concentration over-potential phenomenon, which is crucial in describing the dynamical behavior of such systems, is not adequately modeled. The work developed in [6] correctly considers this effect, and for this reason has been adopted as a benchmark for the simulation described in the following.

The output voltage  $V_{FC}$  of a single cell can be written as:

$$V_{FC} = E_{Nenst} - V_{act} - V_{ohmic} - V_{con} \quad (3)$$

Where  $E_{Nenst}$  is the thermodynamic potential of the cell, which represents the reversible voltage;  $V_{act}$  is the activation over-potential, (a measure of the voltage drop associated with the electrodes);  $V_{ohmic}$  is the concentration over-potential, which takes into account the resistances during conduction of the protons through the solid electrolyte and the electrons through their path;  $V_{con}$  is the concentration over-potential, which considers the voltage drop caused by the reduction of concentration of reactants gases or, alternatively, by the transport of masses of oxygen and hydrogen.

$$E_{Nenst} = 1.229 - 0.85 \times 10^{-3}(T - 298.15) + 4.31 \times 10^{-5}T[\ln(P_{H2}) + 1/2 \ln(P_{O2})] \quad (4)$$

Where T is the cell operation temperature in [K],  $P_{H2}$  and  $P_{O2}$  are respectively the hydrogen and oxygen partial pressures in [atm].

$$V_{act} = -[\zeta_1 + \zeta_2 T + \zeta_3 T \ln(C_{O2}) + \zeta_4 T \ln(i_{Fc})] \quad (5)$$

Where  $i_{Fc}$  is the cell load current in [A], and  $\zeta$ 's are the parametric coefficients defined on the basis of kinetic, thermodynamic and electrochemical phenomena [7].

$C_{O2}$  is the concentration of oxygen in the catalytic interface of the cathode (mol/cm<sup>3</sup>), determined by:

$$C_{O2} = \frac{P_{O2}}{5.08 \times 10^6 e^{-\frac{-498}{T}}} \quad (6)$$

$$V_{ohmic} = i_{Fc} (R_M + R_c) \quad (7)$$

Where  $R_c$  represent the resistance to the transfer of protons through the membrane, usually considered constant.  $R_m$  is the equivalent resistance of the membrane, calculated as:

$$RM = \frac{\rho_M l}{A} \quad (8)$$

Where  $\rho_M$  is the specific resistivity of the membrane for the electron flow ( $\Omega \cdot \text{cm}$ ), A is the cell active area ( $\text{cm}^2$ ) and l is the thickness of the membrane (cm), which serves as the electrolyte of the cell.

$$\rho_M = \frac{181.6 \left[ 1 + 0.03 \left( \frac{i_{Fc}}{A} \right) + 0.062 \left( \frac{T}{303} \right)^2 \left( \frac{i_{Fc}}{A} \right)^{2.5} \right]}{\left[ \psi - 0.634 - 3 \left( \frac{i_{Fc}}{A} \right) \right] \times \exp \left[ 4.18 \left( \frac{T - 303}{T} \right) \right]} \quad (9)$$

Where the  $\psi$  is an adjustable parameter depending on the relative humidity and stoichiometric relation of the anode gas.

$$V_{con} = -B \ln \left( 1 - \frac{J}{J_{max}} \right) \quad (10)$$

Where B is a parametric coefficient, that depends on the cell and its operation and J represents the actual current density of the cell ( $\text{A}/\text{cm}^2$ ).

Using the membrane Nafion 117 with 178 $\mu\text{m}$  width the parameters of the stack was used to simulate the control algorithm and the operation conditions are shown in nomenclature.

Fig 2. Shows polarization curve of PEMFC model described in the paper. The comparison between real data and simulation data confirms correctness of simulation [8].

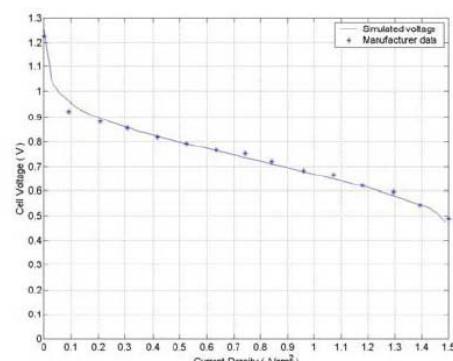


Fig. 2 Polarization curve of simulated cell (line) Actual polarization curve (nods)

The considered model in this paper predicts the FC stack performance against situations commonly encountered in electrical power generation systems, like insertion and rejection of loads. The voltage of fuel cell is output and the pressure of hydrogen, pressure of oxygen, temperature and the load current are inputs.

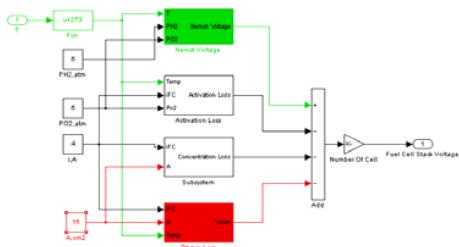


Fig 3 Model of PEMFC in Simulink

### III. NEURAL NETWORK PREDICTIVE CONTROLLER

NN Predictive Controller is one of the promising strategies for complex FC system. No matter how complicated the system is and in spite of the fluctuations, its desired output can be designated to follow the output of a reference model with specified dynamic. The neural network predictive controller strategy includes the specification of reference model with desired dynamic, on-line parameters estimation and calculation of control signals. The first step in model predictive control is to determine the neural network plant model (system identification). In this stage the prediction error between the plant output and the neural network output is used as the neural network training signal. The process is represented by figure3.

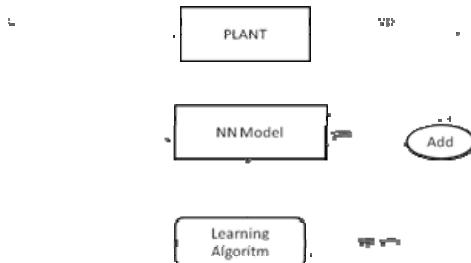


Fig4. Process of NN identification

The neural network plant model uses previous inputs and previous plant outputs to predict future values of the plant output. This feed forward network has one hidden layer and can be trained offline in batch mode, using data collected from the operation of the plant, any of training algorithms in Back Propagation can be used for network training but since our problem is a function approximation and our network has less than a few hundred weights, the Levenberg-Marquardt algorithm will have the fastest convergence. This algorithm is especially noticeable because a very accurate training is required. Levenberg-Marquardt algorithm (trainlm) [9] is able to obtain lower mean square errors and faster convergence than other algorithm tested. (See table II).

Levenberg-Marquardt uses a nonlinear least squares

algorithm to the batch training of the network like other back Propagation algorithms. The performance index for must be minimized is

$$V(\bar{x}) = \sum_{i=1}^N e_i^2(\bar{x}) \quad (11)$$

Where  $e_i(\bar{x})$  is the error between the plant output ( $y_p$ ) and the network output ( $y_m$ ) for the  $i$ th input and  $\bar{x}$  is a parameter vector includes all weights and biases that must be updated. For minimizing the performance index with respect to the parameter vector, the Newton's method would be

$$\Delta\bar{x} = -[\nabla^2 V(\bar{x})]^{-1} \nabla V(\bar{x}) \quad (12)$$

Where  $\nabla^2 V(x)$  is the Hessian matrix and  $\nabla V(\bar{x})$  is the gradient. It can be shown that

$$\nabla V(\bar{x}) = J^T(\bar{x})\bar{e}(\bar{x}) \quad (13)$$

$$\nabla^2 V(\bar{x}) = J^T(\bar{x})J(\bar{x}) + S(\bar{x}) \quad (14)$$

Where  $J(x)$  is the Jacobin matrix and

$$S(\bar{x}) = \sum_{i=1}^N e_i(\bar{x})\nabla^2 e_i(\bar{x}). \quad (15)$$

For the Gauss-Newton method it is assumed that  $S(x)=0$  and the update becomes

$$\Delta\bar{x} = [J^T(\bar{x})J(\bar{x})]^{-1} J^T(\bar{x})e(\bar{x}). \quad (16)$$

The Marquardt-Levenberg modification to the Gauss-Newton method is

$$\Delta\bar{x} = [J^T(\bar{x})J(\bar{x}) + \mu I]^{-1} J^T(\bar{x})e(\bar{x}). \quad (17)$$

The parameter  $\mu$  is multiplied by some factor ( $\beta$ ) whenever a step would result in an increased  $V(x)$ . When a step reduces  $V(x)$ ,  $\mu$  is divided by  $\beta$ .

The following table compares the performance of different algorithms for modeling the PEMFC by a feed forward Neural Network includes one hidden layer with size=7 and 4000 training data. $\mu$  for the starting of trainlm considered 0.01 and  $\beta=10$ .

The Marquardt-Levenberg algorithm can be considered a modification to Gauss-Newton [10].

TABLE I  
COMPARISON BETWEEN DIFFERENT ALGORITHMS FOR NETWORK TRAINING TO IDENTIFY PEMFC

Type	Trainbfg	trainrp	Traingdx	trainlm
Number of epochs	34	22	28	18
Performance index	$1.33 \times 10^{-9}$	0.10 43	$1.35 \times 10^{-9}$	$4.9 \times 10^{-10}$

The model predictive control method is based on the

receding horizon technique. The neural network model predicts the plant response over a specified time horizon. The predictions are used by a numerical optimization program to determine the control signal that minimizes the following performance criterion over the specified horizon

$$\sum_{j=N}^{N_2} (y_r(t+j) - y_m(t+j))^2 + p \sum_{j=1}^{N_u} (u'(t+j-1) - u'(t+j-2)) \quad (18)$$

Where  $N_1, N_2$  and  $N_u$  define the horizons. The  $u'$  variable is the tentative control signal,  $y_r$  is the desired response and  $y_m$  is the network model response.

#### IV. SIMULATION RESULTS

In this section Robustness of proposed controller is proved by simulation of controller in noisy condition. The voltage of cell is output and the pressure of hydrogen, the pressure of oxygen, the load current and temperature are inputs but controller variable is temperature. The voltage is a function of temperature of the environment. So a controller is needed to fix voltage at a constant amount.

In the first experiment the control of output voltage and its tracking is tested (figure4). Using the data generated from the electrochemical model of PEMFC, a Neural Network described in section III and the predictive controller with cost horizon  $N_2=7$ , control horizon  $N_u=2$ , control weighting factor  $\rho=0.05$  and search parameter  $\alpha=0.001$  results of figure5 are concluded.

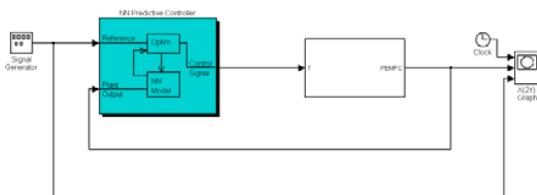


Fig. 5 Control of PEMFC voltage  
By NN Predictive Controller

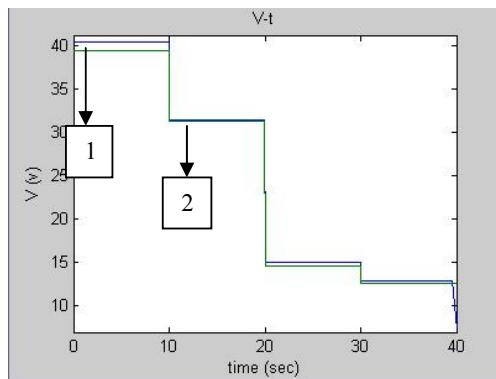


Fig. 6 Comparing of tracking operation between PID and NN Predictive Controller: 1-Setpoint Reference,  
2-NN predictive response

Results show that with NN predictive controller output voltage can lead preference value.

In the other experiment, the NN predictive controller is used as a filter to reduce the effect of noise and fluctuations in the input hydrogen valve.

In noise cancellation, the Neural Network is used to remove noise from signal in a real time. The structure of this method is shown in fig 6. Here, the desired signal  $d(n)$  the one to clean up, combines noise and desired information. To remove the noise, a signal  $n'(n)$  are fed to the NN filter that represents noise that is correlated to the noise to remove from the desired signal. So long as the input noise to the filter remains correlated to the unwanted noise accompanying the desired signal, the adaptive filter adjusts its coefficients to reduce the value of the difference between  $y(n)$  and  $d(n)$ , removing the noise and resulting in a clean signal in  $e(n)$ . Notice that in this application, the error signal actually converges to the input data signal, rather than converging to zero.

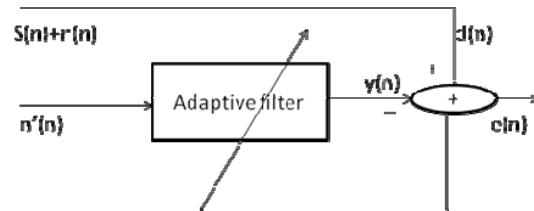


Fig. 7 NN as an adaptive filter

Fig 7 shows the output voltage of PEMFC in presence of noise in the pressure of input hydrogen with and without the NN as a filter. It can clearly be seen that the NN filter can reduce the effect of noise in output voltage.

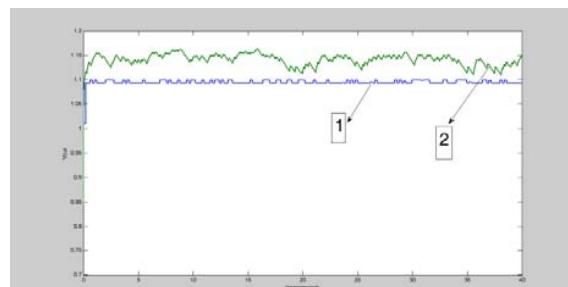


Fig. 8 The output voltage of PEMFC in presence of noise and fluctuations: 1-with NN filter, 2-without filter

#### V. CONCLUSIONS

This paper discussed the application of Neural Network Predictive controller to control the output voltage and reduction of noise and fluctuation effects. The dynamic electrochemical model of PEMFC was expressed and used to generate data with temperature as input and voltage as output. The identification approach was used, based on the single

layer feed forward neural network with Levenberg-Marquardt training algorithm. Simulation results indicate that the performance of NN predictive controller is adequate. Results also show that this controller can reduce the effect of noise as an adaptive filter.

## NOMENCLATURE

Paramete rs	Value	param eters	Value
T	343[k]	$\zeta_1$	-0.948
A	50.6[cm <sup>2</sup> ]	$\zeta_2$	$0.0028 + 0.0002 \ln(A)$ $+ 4.3 \times 10^{-5} \ln(C_{H_2})$
$P_{H_2}$	1[atm]	$\zeta_3$	$7.6 \times 10^{-5}$
$P_{O_2}$	1[atm]	$\zeta_4$	$-1.93 \times 10^{-4}$
B	0.016[v]	$\psi$	23
Rc	0.0003[Ω]	Jmax	1.5A/cm <sup>2</sup>
L	178[μm]	Jn	1.2mA/cm <sup>2</sup>



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