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Similarity Based Membership of Elements to Uncertain Concept in Information System

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Abstract—The process of determining the degree of membership for an element to an uncertain concept has been found in many ways, using equivalence and symmetry relations in information systems. In the case of similarity, these methods did not take into account the degree of symmetry between elements. In this paper, we use a new definition for finding the membership based on the degree of symmetry. We provide an example to clarify the suggested methods and compare it with previous methods. This method opens the door to more accurate decisions in information systems.

Keywords—Information system, uncertain concept, membership function, similarity relation, degree of similarity.

I. Introduction

THE present era is characterized by the ability of computers I to collect and store data on any issue that we are considering for decision. The most difficult issues in research and analysis are issues of uncertainty and incomplete information, scientists have presented theories to deal with these subjects, the most important of which are the fuzzy set theory that has been proposed in [5], intuitionistic fuzzy set by [4] and rough set theory was introduced by [9]. The first theories require membership in [10] and non-membership functions based on experience. In rough set theory, information systems are used to find a membership function that has been based on equivalence relation [1]. This limits the scope of their application. Therefore, general models of the theory were introduced using similarity and dissimilarity relationships and thus created a membership function. Information systems are a general mathematical concept for analyzing uncertain data.

Studying and analyzing uncertain data in information systems plays an important role in real life areas and this approach needs to determine the degree of membership for an element to an uncertain concept. Pawlak used the equivalence relation [10], symmetry relations, topological relations were used in [3], [6], [8], we have observed that all these methods do not take into account the degree of symmetry. The aim of this paper is to present the methods of finding the membership function and to introduce a definition and construct examples and compare it with the pervious similar work. The rest of the paper is organized as follows: the second part presents the basic definitions of information system, the third part contains our definition, characteristics, the part four provides an application example, and the last part contains comparison

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with previous methods.

II. PRELIMINARIES

Rough set theory which was proposed by Pawlak [9], is a mathematical tool to deal with uncertainty and incomplete information. One of the considerable applications of rough set theory is the approximation and membership. In fact, the classical rough sets are difficult to handle well with a lot of data. For this, the relation of similarity rough sets [6], [7] has been applied.

Definition 1 [5]: The information system (Information table) is a pair IS = (U, A), where $U = \{x_1, x_2, ..., x_n\}$ is a non empty finite set of objects called the universe and $A = \{a_1, a_2, ..., a_n\}$ is a non-empty finite set of attributes such as a $U \rightarrow v_a$, $a \in A$. The set v_a is called the value set of a. The set of attributes can be divided in two subsets $C \subset A$ and D = A - C, respectively the conditional set of attributes and the decision (or class) attribute(s). The following definition is a measure for dissimilarity objects based on the information table.

Definition 2 [12]: *Dissimilarity measures:* Let the two objects be denoted as n attributes described by A, B. The measure of the dissimilarity between these two objects is defined as mismatches for them

$$d(A, B) = \sum_{i=1}^{m} \delta(a_i, b_i), \text{ where } \delta(a_i, b_i) = \begin{vmatrix} 0(a_i = b_i) \\ 1(a_i \neq b_i) \end{vmatrix}$$

One of the modern ways in artificial intelligence is to use the separation of elements near a certain element in the inferences about this element and all elements close to it. This method is applied for finding approximations of concepts, computing the accuracy of decisions and constructing membership functions to an uncertain concept. So, the case of equivalence relation can be obtained.

Definition 3 [11]: Let A = (U, A) be an information system and let $\phi \neq X \subseteq U$. The rough A-membership function of the set X (or rm-function, for short), denoted by μ_X^A , is defined as:

$$\mu_X^A(x) = \frac{|(x)_A \cap X|}{|(x)_A|} \text{ for } x \in U.$$

The above definition illustrated in Fig. 1.

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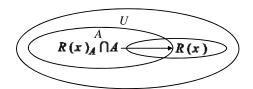


Fig. 1 Information system

III. SIMILARITY BASED MEMBERSHIP.

The purpose of this article is to construct a matrix which represents similarity or dissimilarity relation and use the similarity degrees to construct a membership function. If (u, R) is an I s R is a similarity relation u the similarity matrix is constant as follows:

$$M = a_{i,j}$$
, $i, j = \{1, 2, ..., n\}$,

where the value of $a_{i,j}$ is denoted by $\mu(x_i, x_j)$.

If (u, R) is an I s, A C u, $X \in$ the degree of member-ship of x to A denoted by $\mu_A(x)$ is given by

$$\mu_{A}\left(x\right) = \frac{\sum_{x_{i} \in A \bigcap R\left(x\right)} \{\mu(x, x_{i}), x \neq x_{i}\}}{\sum_{x_{i} \in R\left(x\right)} \mu(x, x_{i}), x \neq x_{i}}.$$

Remark 1: If $R(x) = \{y\}$ and $A \cap R(x) = \{y\}$, then

$$\mu_A(x) = \begin{cases} 1 & \text{if } R \text{ is similarity} \\ 0 & \text{if } R \text{ is dissimilarity.} \end{cases}$$

Example 1: The process begins with the definition of attribute for each class. During the test phase in the power plant for the prototype, the pre-set was adjusted. Eight examples [2] are shown in Table I with the attributes: frequency, amplitude, (harmonic distortion level) THD, and distortion. Normal, warning, and danger are the outputs.

TABLE I Fest Phase in the Power Pi ant

TEST PHASE IN THE POWER PLANT						
Ex.	Freq.	Amp.	TDH	Dis.	Out.	
x_1	Low	Nor.	Nor.	Nor.	Nor.	
x_2	Low	Med.	Med.	Nor.	Nor.	
x_3	Low	Med.	Nor.	High	Nor.	
x_4	Med.	Med.	Nor.	Med.	War.	
x_5	Med.	Med.	Nor.	High	War.	
x_6	Med.	High	Nor.	High	Dan.	
x_7	High	High	Med.	Med.	Dan.	
x_8	Med.	High	Nor.	Med.	Dan.	

Using Definition 2 we get the following dissimilarity matrix in Table II.

TABLE II THE DISSIMILARITY MATRIX x_1 Ex. x_2 χ_3 x_7 x_1 0 2 0 2 4 5 4 x_2 x_3 x_4 x_5 x_6 x_7 3 2 x_8 0

Using the dissimilarity matrix, we get $R(x) = \{y : v(x, y) \le \lambda\}$. We choose classes in more than one way according to the value of λ as follows.

From Table II, in case where the output is Normal $A = \{x_1, x_2, x_3\}$

$$\mu(x) = \frac{A \cap R(x)}{R(x)}.$$

Case I. for
$$\lambda \le 4$$

$$R(x_1) = \{x_1, x_2, x_3, x_4, x_5, x_6, x_8\},$$

$$A \cap R(x_1) = \{x_1, x_2, x_3\}$$

$$\mu_A(x_1) = \frac{0+2+2}{0+2+2+4+4+4+4} = 0.25$$

$$R(x_2) = \{x_1, x_2, x_3, x_4, x_5, x_7, x_8\},$$

$$A \cap R(x_2) = \{x_1, x_2, x_3\}$$

$$\mu_A(x_2) = \frac{2+0+2}{2+0+2+4+4+4+4} = 0.25$$

$$R(x_3) = \{x_1, x_2, x_3, x_4, x_5, x_6, x_8\},$$

$$A \cap R(x_3) = \{x_1, x_2, x_3, x_4, x_5, x_6, x_8\},$$

$$A \cap R(x_3) = \frac{2+2+0}{2+2+0+3+2+3+4} = 0.25$$

$$R(x_4) = \{x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8\},$$

$$A \cap R(x_4) = \{x_1, x_2, x_3\}$$

$$\mu_A(x_4) = \frac{4+4+3}{4+4+3+0+1+3+4+2} = 0.52$$

$$R(x_5) = \{x_1, x_2, x_3, x_4, x_5, x_6, x_8\},$$

$$A \cap R(x_5) = \{x_1, x_2, x_3, x_4, x_5, x_6, x_8\},$$

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$$A \cap R(x_6) = \{x_1, x_3, x_4, x_5, x_6, x_7, x_8\},$$

$$A \cap R(x_6) = \{x_1, x_3, x_4, x_5, x_6, x_7, x_8\},$$

$$A \cap R(x_7) = \{x_2, x_4, x_6, x_7, x_8\},$$

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$$\mu_A(x_7) = \frac{4}{4+4+3+0+2} = 0.307$$

$$R(x_8) = \{x_1, x_2, x_3, x_4, x_5, x_6, x_7, x_8\}$$

$$A \cap R(x_8) = \{x_1, x_2, x_3\}$$

$$\mu_A(x_8) = \frac{4+4+4}{4+4+4+2+3+1+2+0} = 0.6$$

 $R(x_1) = \{x_1, x_2, x_3\},$

Case II. for $\lambda \leq 3$

$$A \cap R (x_1) = \{x_1, x_2, x_3\}$$

$$\mu_A (x_1) = \frac{0+2+2}{0+2+2} = 1.0$$

$$R (x_2) = \{x_1, x_2, x_3\},$$

$$A \cap R (x_2) = \{x_1, x_2, x_3\},$$

$$\mu_A (x_2) = \frac{2+0+2}{2+0+2} = 1.0$$

$$R (x_3) = \{x_1, x_2, x_3, x_4, x_5, x_6\},$$

$$A \cap R (x_3) = \{x_1, x_2, x_3, x_4, x_5, x_6\},$$

$$A \cap R (x_3) = \{x_1, x_2, x_3\},$$

$$\mu_A (x_3) = \frac{2+2+0}{2+2+0+3+2+3} = 0.33$$

$$R (x_4) = \{x_3, x_4, x_5, x_6, x_8\},$$

$$A \cap R (x_4) = \{x_3\},$$

$$\mu_A (x_4) = \frac{3}{3+0+1+3+2} = 0.33$$

$$R (x_5) = \{x_3, x_4, x_5, x_6, x_8\},$$

$$A \cap R (x_5) = \{x_3\},$$

$$\mu_A (x_5) = \frac{2}{2+1+0+2+3} = 0.25$$

$$R (x_6) = \{x_3, x_4, x_5, x_6, x_7, x_8\},$$

$$A \cap R (x_6) = \{x_3\},$$

$$\mu_A (x_6) = \frac{3}{3+3+2+0+3+1} = 0.25$$

$$R (x_7) = \{x_6, x_7, x_8\},$$

$$A \cap R (x_7) = \phi$$

$$\mu_A (x_7) = \frac{|\phi|}{3+0+2} = 0$$

$$R (x_8) = \{x_4, x_5, x_6, x_7, x_8\},$$

$$A \cap R (x_8) = \phi$$

$$\mu_A (x_8) = \frac{|\phi|}{2+3+1+2+0} = 0$$

Case III. for $\lambda \le 2$

$$R(x_1) = \{x_1, x_2, x_3\},$$

$$A \cap R(x_1) = \{x_1, x_2, x_3\}$$

$$\mu_A(x_1) = \frac{0+2+2}{0+2+2} = 1$$

$$R(x_2) = \{x_1, x_2, x_3\},$$

$$A \cap R(x_2) = \{x_1, x_2, x_3\},$$

$$\mu_{A}(x_{2}) = \frac{2+0+2}{2+0+2} = 1$$

$$R(x_{3}) = \{x_{1}, x_{2}, x_{3}, x_{5}\},$$

$$A \cap R(x_{3}) = \{x_{1}, x_{2}, x_{3}\},$$

$$\mu_{A}(x_{3}) = \frac{2+2+0}{2+2+0+2} = 0.67$$

$$R(x_{4}) = \{x_{4}, x_{5}, x_{8}\},$$

$$A \cap R(x_{4}) = \phi$$

$$\mu_{A}(x_{4}) = \frac{|\phi|}{0+1+2} = 0$$

$$R(x_{5}) = \{x_{3}, x_{4}, x_{5}, x_{6}\},$$

$$A \cap R(x_{5}) = \{x_{3}\},$$

$$\mu_{A}(x_{5}) = \frac{2}{2+1+0+2} = 0.4$$

$$R(x_{6}) = \{x_{5}, x_{6}, x_{8}\},$$

$$A \cap R(x_{6}) = \phi$$

$$\mu_{A}(x_{6}) = \frac{|\phi|}{2+0+1} = 0$$

$$R(x_{7}) = \{x_{7}, x_{8}\},$$

$$A \cap R(x_{7}) = \phi$$

$$\mu_{A}(x_{6}) = \frac{|\phi|}{0+2} = 0$$

$$R(x_{8}) = \{x_{4}, x_{6}, x_{7}, x_{8}\},$$

$$A \cap R(x_{8}) = \phi$$

$$\mu_{A}(x_{8}) = \frac{|\phi|}{2+1+2+0} = 0$$

A comparison between the suggested method and previous method is shown in Table III.

TABLE III
COMPARISON BETWEEN SUGGESTED AND PREVIOUS METHODS

	х	The suggested method $\mu_{A}\left(x\right)$	Pawlak $\mu_A(x)$
Case I $\lambda \leq 4$	x_1	0.250	0.488
	x_2	0.250	0.428
	x_3	0.250	0.430
	x_4	0.520	0.375
	x_5	0.625	0.428
	x_6	0.307	0.330
	x_7	0.307	0.800
	x_8	0.600	0.375
	x_3	0.330	0.500
Case II	x_4	0.330	0.600
$\lambda \leq 3$	x_5	0.250	0.400
	x_6	0.250	0.500
Case III	x_3	0.670	0.750
$\lambda \leq 2$	x_5	0.400	0.500

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IV. CONCLUSION

The concept developed in this research presents a new method of finding the function of membership using the sum of degrees of symmetry and this leads to more accurate decisions in evaluating the approximations and decision making.

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