Speed Sensorless Direct Torque Control of a PMSM Drive using Space Vector Modulation Based MRAS and Stator Resistance Estimator

A. Ameur, B. Mokhtari, N. Essounbouli, L. Mokrani

Abstract—This paper presents a speed sensorless direct torque control scheme using space vector modulation (*DTC-SVM*) for permanent magnet synchronous motor (*PMSM*) drive based a Model Reference Adaptive System (*MRAS*) algorithm and stator resistance estimator. The *MRAS* is utilized to estimate speed and stator resistance and compensate the effects of parameter variation on stator resistance, which makes flux and torque estimation more accurate and insensitive to parameter variation. In other hand the use of *SVM* method reduces the torque ripple while achieving a good dynamic response. Simulation results are presented and show the effectiveness of the proposed method.

Keywords—*MRAS*, *PMSM*, *SVM*, *DTC*, Speed and Resistance estimation, Sensorless drive

I. INTRODUCTION

AC motor control has attracted much attention recently in the power electronics field [1]. Permanent magnet synchronous motors *(PMSM)* have been widely used as servo-machines over the last two decades. In recent years, they are used more in the variable speed applications due to some advantages like: more simplicity, low dependency on the motor parameters, good dynamic torque response, high rate torque/inertia [2] Since the advent of the direct torque control (*DTC*) for induction machines in the 1980's as proposed by M. Depenbrock [1] and Takahashi [3], its research has been becoming ever more prevalent in the society. The main advantages of *DTC* are the simple control scheme, a very good torque dynamic response, as well as the fact that it does not need the rotor speed or position to realize the torque and flux control, moreover *DTC* is not sensitive to parameters variations (except stator resistor) [1]-[5].

However, it still has some disadvantages that can be summarized in the following points:

- Difficulty variable switching frequency,
- High current and torque ripple;
- High sampling frequency needed for digital
- Implementation of hysteresis comparators.
- High noise level at low speed [3];

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To overcome the above drawbacks, some researchers have been trying to propose solution to solve these problems by substitute hysteresis control by *fuzzy* control [4]. An effective modality for reducing the torque ripple without using a high sampling frequency is to calculate a proper reference voltage vector that can produce the desired torque and flux values, and then applied to the inverter using space vector modulation (*SVM*) [6]-[9]. This approach is known in the literature as *DTC-SVM*. Even though this control method provides fast torque response and small torque ripples.

The high performance speed or position control requires an accurate knowledge of rotor shaft position and velocity in order to synchronize the phase excitation pulses to the rotor position. This implies the need for speed or a shaft position sensor such as an optical encoder or a resolver. However, the presence of this sensor (expensive and fragile and require special treatment of captured signals), causes several disadvantages from the standpoint of drive cost, encumbrance, reliability and noise problem [6]-[10].

To achieve sensorless operation of a *PMSM* drive, several algorithms have been suggested in recent literature. These methods can broadly be classified as:

- Back-emf based estimators with explicit compensation for nonlinear properties, parameter variation and disturbances.
- Estimation based on high frequency signal injection, exploiting the saliency property of a *PMSM* [3].
- Adaptive or robust observers based on advanced models.

The Method of observers is sometimes more favourable due to its robustness to parameter variations and its excellent disturbance rejection capabilities[7]-[9].

This paper proposes the control strategy using space vector modulation (*DTC-SVM*) based on the *MRAS* (Model Reference Adaptive System) in the sensorless control of a permanent magnet synchronous motor and stator resistance estimation So that it can overcome the problem of sensitivity in the face of motor parameter variation.

II. PMSM MODEL

The stator and rotor flux equation of *PMSM* can be written in the reference frame of Park in the following form [2]:

$$\begin{bmatrix} \phi_d \\ \phi_q \end{bmatrix} = \begin{bmatrix} L_d & 0 \\ 0 & L_q \end{bmatrix} \begin{bmatrix} i_{sd} \\ i_{sq} \end{bmatrix} + \begin{bmatrix} \phi_e \\ 0 \end{bmatrix} \tag{1}$$

While the equations of the stator voltages are written in this same reference frame in the following form:

$$\begin{bmatrix} v_d \\ v_q \end{bmatrix} = r_s \begin{bmatrix} i_{ds} \\ i_{qs} \end{bmatrix} + \begin{bmatrix} L_d & 0 \\ 0 & L_q \end{bmatrix} \frac{d}{dt} \begin{bmatrix} i_{ds} \\ i_{qs} \end{bmatrix} + p\Omega_r \begin{bmatrix} 0 & -L_q \\ L_d & 0 \end{bmatrix} \begin{bmatrix} i_{ds} \\ i_{qs} \end{bmatrix} + p\Omega_r \begin{bmatrix} 0 \\ \phi_e \end{bmatrix} \qquad (2)$$

In addition the electromagnetic torque can be expressed:

$$T_e = \frac{3}{2} p \left((l_d - l_q) i_{ds} i_{qs} + q_e i_{qs} \right) \qquad (3)$$

The mechanical equation of the motor can be expressed as flows:

$$J\dot{\Omega} = T_e - T_l - f_r \Omega \qquad (4)$$

III. CONVENTIONAL DTC

The methods of direct torque control (*DTC*) as shown in figure 1 consist of directly controlling the turn off or turn on of the inverter switches on calculated values of stator flux and torque from relation (6). The reference frame related to the stator makes it possible to estimate flux and the torque, and the position of flux stator. The aim of the switches control is to give the vector representing the stator flux the direction determined by the reference value.

$$\begin{cases} \phi_{s\alpha} = \int_0^t (v_{s\alpha} - r_s i_{s\alpha}) \, dt \\ \phi_{s\beta} = \int_0^t (v_{s\beta} - r_s i_{s\beta}) \, dt \end{cases} \qquad (5)$$

The DTC is deduced based on the two approximations described by the formulas (6) and (7) [1],[5]:

$$\bar{\phi}_s(k+1) \approx \bar{\phi}_s(k) + \bar{V}_s T_s \quad \rightarrow \quad \Delta\bar{\phi}_s \approx \bar{V}_s T_s \qquad (6)$$

$$T_e = k(\bar{\varphi}_s \times \bar{\varphi}_r) = k |\bar{\varphi}_s| \, |\bar{\varphi}_r| \sin(\delta) \qquad (7)$$

More over:

$$\begin{cases} \hat{\phi}_s = \sqrt{\hat{\phi}_{s\alpha}^2 + \hat{\phi}_{s\beta}^2} \\ \angle \hat{\phi}_s = arctg \, \dfrac{\hat{\phi}_{s\beta}}{\hat{\phi}_{s\alpha}} \end{cases} \qquad (8)$$
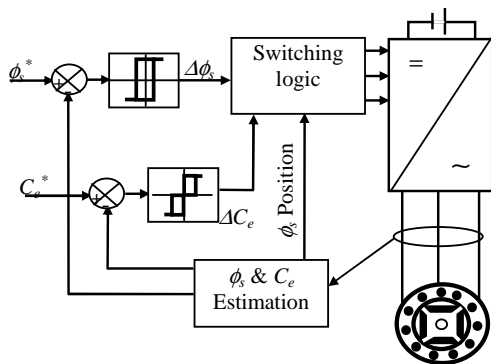

Fig. 1 Diagram of *DTC* control applied for *PMSM* supplied with a three-phase inverter with *PMW*

A two levels classical voltage inverter can achieve seven separate positions in the phase corresponding to the eight sequences of the voltage inverter.
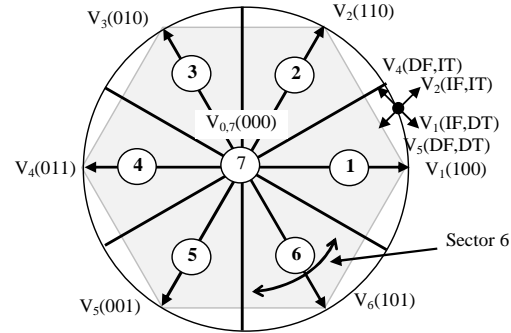

Fig. 2 Different vectors of stator voltages provided by a two levels inverter

Where: I (D)F : Increase (Decrease) of Flux amplitude.
I(D)T : Increase (Decrease) of Torque.

Table I have the sequences corresponding to the position of the stator flux vector in different sectors (see Figures 1).

TABLE I
VECTORS VOLTAGE LOCALIZATION

$\Delta\phi_s$	ΔC_e	S_1	S_2	S_3	S_4	S_5	S_6
	1	110	010	011	001	101	100
1	0	000	000	000	000	000	000
	-1	101	100	110	010	011	001
	1	010	011	001	101	100	110
0	0	000	000	000	000	000	000
	-1	001	101	100	110	010	011

The flux and torque are controlled by two comparators with hysteresis illustrated in Figure 3. The dynamics torque are generally faster than the flux then using a comparator hysteresis of several levels, is then justified to adjust the torque and minimize the switching frequency average [5].
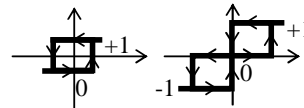

Fig. 3 Comparators with hysteresis used to regulate flux and torque

IV. SPACE VECTOR MODULATION

The Space Vector Modulation (*SVM*) is not based on separate calculations for each arm of a three-phase voltage inverter but by determination of a reference voltage vector from eight voltage vectors. This is generally calculated and approximated on a modulation period *T* from a vector average voltage developed by the application of adjacent voltage vectors and zero vectors V_0 and V_7. We note with T_i and T_{i+1} a two-time application of these vectors; their sum must be less than the period T of the inverter switching. The *SVM* consists in projecting the reference voltage vector on both V_{sref} desired voltage vectors V_1 and V_2 in the first sector and the application time of each adjacent vector is given by [9]:
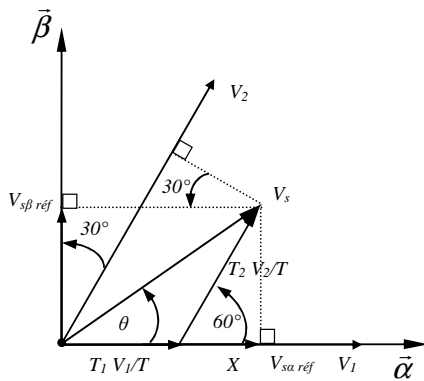
Fig. 4 Projection of the reference Voltage Vector

Where:

T_s: represents the switching period;

T_1: the time of application of the vector $\overline{V}_1$;

T_2 is the time of application of the vector $\overline{V}_2$;

T_0: the duration of the sequence of freewheel.

The determination of the amount of times T_1 and T_2 is given by simple projections:

$$\begin{cases} V_{s\alpha} = \dfrac{T_1}{T}\left|\overline{V}_1\right| + x.\cos(30°) \\ V_{s\beta} = \dfrac{T_2}{T}\left|\overline{V}_2\right| \\ x = \dfrac{V_{s\beta}}{\tan g(60°)} \end{cases} \quad (9)$$

Finally, with the $(\alpha\text{-}\beta)$ component values of the vectors given in the Table 4.2,

TABLE II
$(\alpha\text{-}\beta)$ COMPONENT VALUES OF THE VECTORS VOLTAGE

Vectors	S_a	S_b	S_c	$V_{\alpha s}$	$V_{\beta s}$
V_0	0	0	0	0	0
V_5	0	0	1	$\sqrt{2}U_C/\sqrt{3}$	0
V_3	0	1	0	$U_C/\sqrt{6}$	$U_C/\sqrt{2}$
V_4	0	1	1	$-U_C/\sqrt{6}$	$U_C/\sqrt{2}$
V_1	1	0	0	$-\sqrt{2}U_C/\sqrt{3}$	0
V_6	1	0	1	$-U_C/\sqrt{6}$	$-U_C/\sqrt{2}$
V_2	1	1	0	$U_C/\sqrt{6}$	$-U_C/\sqrt{2}$
V_7	1	1	1	0	0

The amount of times of application of each adjacent vector is:

$$\begin{cases} T_1 = \dfrac{T}{2U_c}\left(\sqrt{6}.V_{\alpha s\ réf} - \sqrt{2}.V_{\alpha\beta\ réf}\right) \\ T_2 = \sqrt{2}\,\dfrac{T}{U_c}V_{\beta s\ réf} \end{cases} \quad (10)$$

The rest of the period spent in applying the null-vector. For every sector, commutation duration is calculated. The amount of times of vector application can all be related to the following variables:

$$\begin{cases} X = \dfrac{T}{U_c}\sqrt{2}.V_{\beta s\ réf} \\ Y = \dfrac{T}{U_c}\left(\dfrac{\sqrt{2}}{2}.V_{\beta s\ réf} + \dfrac{\sqrt{6}}{2}.V_{\alpha s\ réf}\right) \\ Z = \dfrac{T}{U_c}\left(\dfrac{\sqrt{2}}{2}.V_{\beta s\ réf} - \dfrac{\sqrt{6}}{2}.V_{\alpha s\ réf}\right) \end{cases} \quad (11)$$

In the previous example for sector 1, $T_1 = -Z$ and $T_2 = X$. Extending this logic, one can easily calculate the sector number belonging to the related reference voltage vector.

Application durations of the sector boundary vectors are tabulated as;

TABLE III
DURATIONS OF THE SECTOR BOUNDARY VECTORS

Sectors (S_i)	1	2	3	4	5	6
T_1	-Z	Y	X	Z	-Y	-X
T_2	X	Z	-Y	-X	-Z	Y

The third step is to compute the three necessary duty cycles as;

$$\begin{cases} T_{aon} = \dfrac{T_e - T_i - T_{i+1}}{2} \\ T_{bon} = T_{aon} + T \\ T_{con} = T_{bon} + T_{i+1} \end{cases} \quad (12)$$

V. DIRECT TORQUE CONTROL SCHEME USING SPACE VECTOR MODULATION (DTC-SVM)

The strategy of the *DTC-SVM* uses a switching *SVM* vector and imposed constant frequency. This DTC- fixed frequency does not use the controller hysteresis; it significantly relaxes the constraints of computing time. Furthermore, this methodology is based on an explicit calculation of the control to achieve the objective of torque, and the oscillations of the latter are considerably reduced [11].

This is a strategy for generating a stator reference voltage which should be applied to PMSM and it can be inserted into a block PWM inverter (see Fig. 6).

In *DTC-SVM*, the generation of command pulses (S_a, S_b, S_c) applied to control the inverter switches is usually based on the use of a predictive controller. The error of torque $\Delta C_e = \left(C_{eref}^* - \hat{C}_e\right)$, the reference amplitude stator flux ϕ_s^* delivered by predictive controller, It can receives information about the module and the position of estimated stator flux $\hat{\phi}_s$ and measured stator current vector, then the predictive controller determinate the stator voltage reference vector in polar coordinates $\overline{V}_{sref} = \left[V_{sref} \quad \angle V_{sref}\right]$ for space vector modulator (SVM), which finally generates the pulses (S_a, S_b, S_c) to control the inverter [9].

From the vector diagram of Figure (5) and equation (1) one can obtain the following expression for the torque [11]:

$$T_e = \frac{3}{2} p \frac{\varphi_s^*}{l_d l_q} \left[q_e l_q \ sin(\delta) + \frac{1}{2} \varphi_s^* \left(l_d - l_q \right) sin(2\delta) \right] \qquad (13)$$

Where δ is the angle between the stator and rotor flux linkage when the stator resistance is neglected.

From equation (13), we note that for constant amplitude of the stator flux and flux produced by permanent magnet, the electromagnetic torque can be changed by control on the torque angle δ which can be varied by changing position of the stator flux vector in respect to *PM* vector using voltage vector delivered by the inverter. In steady state, the stator flux and rotor flux rotate at synchronous speed, δ is constant and corresponds to the torque angle. In transient state, δ varies and the stator flux and rotor flux rotate at different speeds.
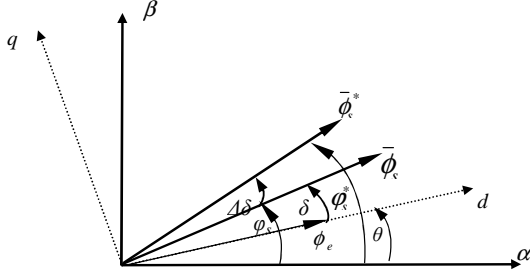

Fig. 5 Vector diagram illustrating the conditions of torque control

The error torque and the amplitude of the reference stator flux are delivered to the predictive controller. The relation between the torque error and the increment of the load angle $\Delta\delta$ is nonlinear. So a *PI* controller that produces the increment of the load angle can minimize the error instantaneous torque. The reference $\Delta\delta$ value of the stator voltage vector, is calculated based on the stator resistance, the signal $\Delta\delta$, the measured stator current, the flux stator magnitude and its estimated position as follows: [11]

$$V_{as \ ref} = \frac{\phi_s^* cos \ (\varphi_s + \Delta\delta) - \phi_s cos \ (\varphi_s)}{T_s} + r_s i_{as}$$

$$V_{\beta s \ ref} = \frac{\phi_s^* sin \ (\varphi_s + \Delta\delta) - \phi_s sin \ (\varphi_s)}{T_s} + r_s i_{\beta s} \qquad (14)$$

where

$$V_{s \ ref} = \sqrt{V_{as \ ref}^{\ \ 2} + V_{\beta s \ ref}^{\ \ 2}}$$

$$\varphi_{s \ ref} = arctan \left(\frac{V_{\beta s \ ref}}{V_{as \ ref}} \right) \qquad (15)$$

For constant flux operating region, the value of reference stator flux amplitude is equal to the flux amplitude produced by permanent magnet q_e [11].
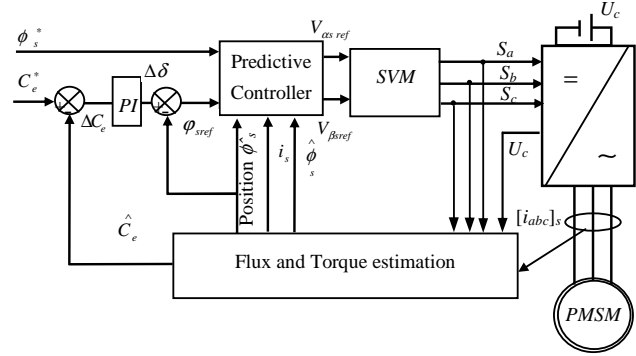

Fig. 6 Diagram of *DTC-SVM* control applied for *PMSM* supplied with a three-phase inverter

VI. MODEL REFERENCE ADAPTIVE SYSTEM

The presence of sensors measuring these quantities implies several disadvantages in addition to the extra cost; a greater number of connections between the motor and the control board and reduced robustness. For these reasons several strategies to detect the speed and position without sensors have been developed over the last twenty years. Multitude observers have been proposed, but only a few [7]-[12] are able to sustain persistent and accurate wide speed range sensorless operation.

The model reference adaptive system (*MRAS*) is an important adaptive controller [10]. The *MRAS* for estimating rotor position angle and speed is based on a stator current estimator using discontinuous control. Due to the fact that only stator currents are directly measurable in a *PMSM* drive. In this way, when the estimated currents, i.e., state, reach the manifold. Comparing to other adaptation techniques, this method is simple and needs a low computation power and has a high speed adaptation even at zero speeds. This method because eliminates the produced error in the speed adaptation, is more stable and robust.

The rotor speed and the stator resistance are reconstructed using the model reference adaptive system (*MRAS*). The MRAS principle is based on the comparison of the outputs of two estimators. The first is independent of the observed variable named as model reference. The second is the adjustable one. The error between the two models feed an adaptive mechanism to turn out the observed variable.

In this work, the actual system is considered as the model reference and the observer is used as the adjustable one. The rotor speed is included in the (16) that present current model are relevant to rotor speed. So the stator current model is chosen as the state variable:

$$\begin{cases} \dfrac{d}{dt} \hat{i}_{ds} = \dfrac{v_{ds}}{l_d} - \dfrac{\hat{r}\hat{i}_{ds}}{l_d} + p\hat{\Omega}_r \hat{i}_{qs} \\[3mm] \dfrac{d}{dt} \hat{i}_{qs} = \dfrac{v_{qs}}{l_d} - \dfrac{\hat{r}\hat{i}_{qs}}{l_d} - p\hat{\Omega}_r \hat{i}_{ds} - p\dfrac{q_e}{l_d}\hat{\Omega}_r + \dfrac{k\hat{r}i_{qs}}{l_d} \end{cases} \qquad (16)$$

The stator resistance and the rotor speed are built around the following adaptive mechanisms:

$$\begin{cases} \hat{r}_s = -\dfrac{1}{l_d} \displaystyle\int_0^t (e_{ds}\,\hat{i}_{ds} + e_{qs}\,\hat{i}_{qs})\,dt \\[4mm] \hat{\Omega}_r = \dfrac{1}{p}\left(k_p\,e + k_i \displaystyle\int_0^t e\,dt\right) \end{cases} \quad (17)$$

$$e = i_{ds}\hat{i}_{ds} - i_{qs}\hat{i}_{qs} - \dfrac{q_e}{l_d}e_{qs} \qquad (18)$$

$$e_{ds} = i_{ds} - \hat{i}_{ds}\,;\, e_{qs} = i_{qs} - \hat{i}_{qs} \qquad (19)$$

Where k_p and k_I are the proportional and integral constants respectively. The tracking performance of the speed estimation and the sensivity to noise are depending on proportional and integral coefficient gains. The integral gain k_I is chosen to be high for fast tracking of speed. While, a low proportional k_p gain is needed to attenuate high frequency signals denoted as noises [12].
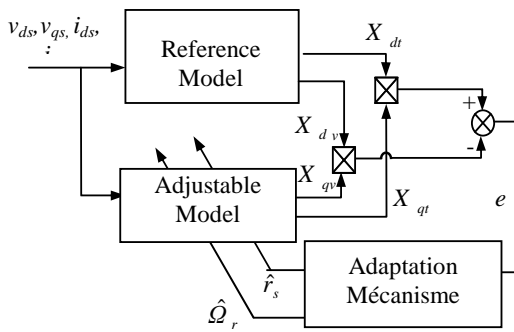

Fig. 7 Basic MRAS structure

V. Results of Simulation

Table (IV), summarizes the *PMSM* parameters used in this simulation [7].

TABLE IV
PMSM PARAMETERS

Pole pairs	3
Rated power *KW* (at 50 *Hz*)	1.5
Rated voltage (*V*)	220/380
Rated Flux (*Wb*)	0.30
Rated torque (*Nm*)	5
R_s (Ω)	1.4
L_d ; L_q (*H*)	0.0066; 0.0058
Flux magnet (Wb)	0.15
J(Kg.m²)	0.00176
f_r *(N.m/(rad/s))*	0.0038

We simulated the system drive for a reference speed of 100 (rd / s) load at startup, then from t = 0.08 (s), we assumed a variation of the stator resistance (see Fig. 5). At t = 0.15(s), the *PMSM* is tracking load equal to 5 (Nm). The results are obtained using a *PI* speed controller.

Figure 8 illustrates the evolution of stator resistance, actual and estimated (delivered by the propose *MRAS* proposed for *DTC/ DTC-SVM*). The two quantities (estimated and actual resistances) are combined in practice, in steady state. As in Figure 9, it illustrates estimated speed (rad / s) issued by

MRAS, the speed response is achieved without dip and with a shorter recovery time which is almost similar with the actual speed motor.

Figure 10, shows the stator flux estimation using the *MRAS*. We notice that it is not affected by these changes. Electromagnetic torque follows his rate as shown in Figure 12.

Also, the flux and torque ripples are significantly suppressed due to the *SVM* modulation scheme as shown in Figure 11 and Figure 13
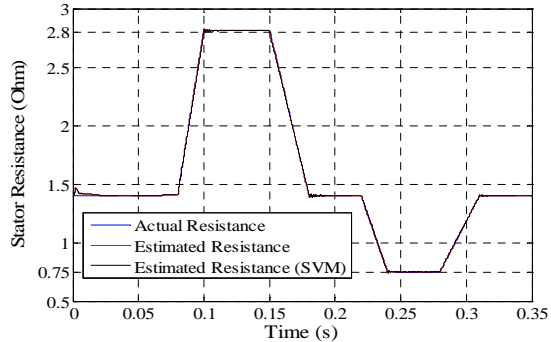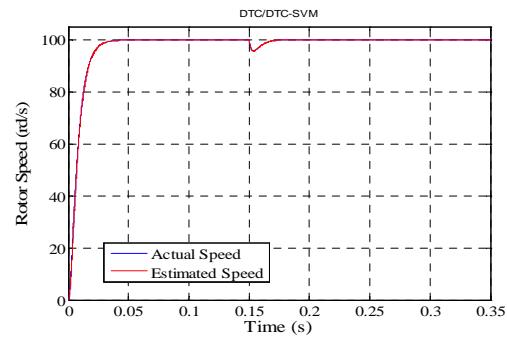

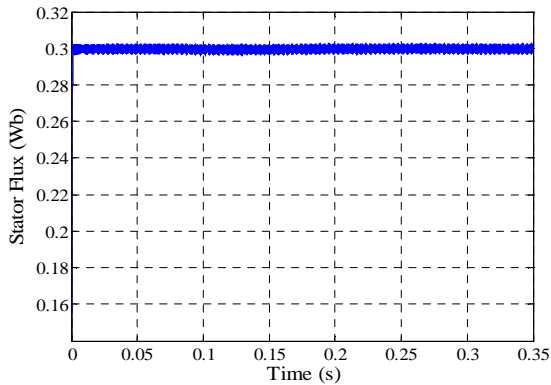Fig. 8 Stator Resistance

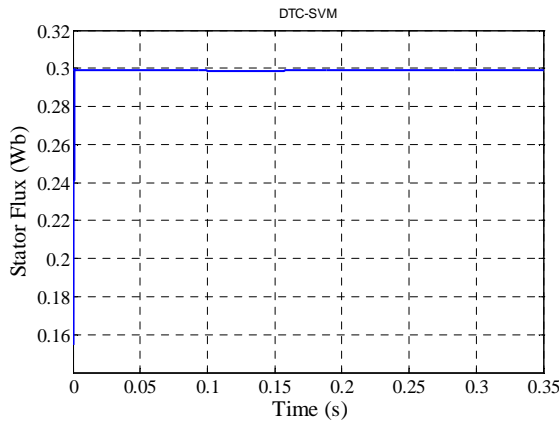Fig. 9 Rotor speed

Fig. 10 Stator Flux
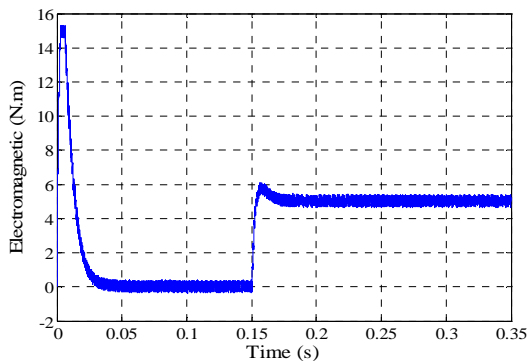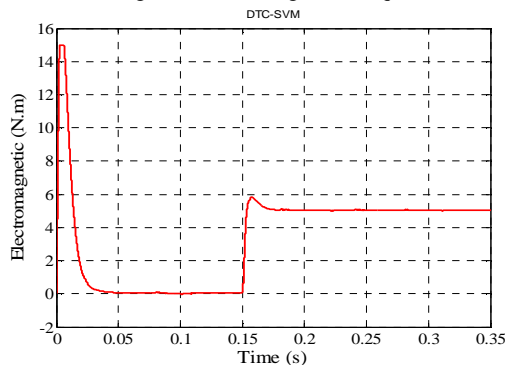
Fig. 11 Stator Flux

Fig. 12 Electromagnetic Torque

Fig. 13 Electromagnetic Torque

VI. CONCLUSIONS

In this paper, a robust *MRAS* for speed sensorless *DTC-SVM* scheme based on stator resistance estimator has been introduced. According to this control approach, the *PWM* inverter reference voltage vector is generated by a conventional *PI* predictor. The reference voltage vector is synthesized with the *SVM* technique as opposed to the switching table in the conventional *DTC*. The *DTC-SVM* scheme has lower harmonic current and consequently lower torque ripple than conventional hysteresis based *DTC*. Using of a model reference adaptive system for estimating the speed and stator resistance of a *PMSM*, compensate the effect of the variations of motor parameters and replace the position encoder. The obtained simulation results were satisfactory in terms of estimation errors, robustness and global stability of the drive electrical system for different operating conditions.

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