

A Bayesian Hierarchical ^{13}C COBT to Correct Estimates Associated with a Delayed Gastric Emptying

Leslie J.C.Bluck, Sarah J.Jackson, Georgios Vlasakakis, and Adrian Mander

Abstract—The use of a Bayesian Hierarchical Model (BHM) to interpret breath measurements obtained during a ^{13}C Octanoic Breath Test (^{13}C COBT) is demonstrated. The statistical analysis was implemented using WinBUGS, a commercially available computer package for Bayesian inference. A hierarchical setting was adopted where poorly defined parameters associated with a delayed Gastric Emptying (GE) were able to "borrow" strength from global distributions. This is proved to be a sufficient tool to correct model's failures and data inconsistencies apparent in conventional analyses employing a Non-linear least squares technique (NLS). Direct comparison of two parameters describing gastric emptying (t_{lag} -lag phase, $t_{1/2}$ -half emptying time) revealed a strong correlation between the two methods. Despite our large dataset ($n=164$), Bayesian modeling was fast and provided a successful fitting for all subjects. On the contrary, NLS failed to return acceptable estimates in cases where GE was delayed.

Keywords—Bayesian hierarchical analysis, ^{13}C COBT, Gastric emptying, WinBUGS.

I. INTRODUCTION

GAMMA Scintigraphy is widely recognised as the 'gold standard' method for measuring Gastric Emptying (GE) in humans. The clinical procedure and different variations of the protocol have been well described [1][2], but essentially the test requires the subject to ingest a radio-labelled meal and in the following few hours a number of images of the quantity of radiolabel retained in the stomach are obtained. These measurements are used to identify a mathematical model (power exponential function) [3] from which the time of the maximum emptying rate ($t_{lag(s)}$) and the time at which half of

the ingested label substrate has left the stomach ($t_{1/2(s)}$) can be derived.

However, use of the test raises several ethical issues such as exposure of the patient to a significant amount of radiation, and its application in paediatrics or pregnancy. Furthermore there is a number of inconsistencies between reported studies (meal composition, meal form, display methodology, quantitative parameters) that have led to a need for the development of an alternative test capable of overcoming these issues.

The ^{13}C -octanoate acid breath test (^{13}C COBT) was first introduced by Ghos [4] as an indirect, low cost and ethically acceptable method to measure gastric emptying in man. Due to its nature the test is suitable for repetitive studies and in all populations. The octanoate (in common with all medium chain fatty acids) passes unchanged through the stomach and enters the small intestine where it is rapidly absorbed and then transported to the liver where it is immediately oxidised into CO_2 and water. Subsequently, the only limiting factor for its metabolism is the time interval that it actually resides in the stomach.

The standard protocol for the ^{13}C COBT requires the ingestion of a labelled solid meal followed by a number of breath measurements of the instantaneous recovery of the labelled $^{13}\text{CO}_2$. By fitting a mathematical model to a set of breath measurements two key parameters can be obtained, known as the half and lag time ($t_{1/2(b)}$ and $t_{lag(b)}$ respectively).

Although the ^{13}C COBT has been exploited in many studies [5][6], the test has not yet achieved universal acceptance, due mainly to its inability to provide parameters which are directly comparable to those from gamma scintigraphy. The reason for this is that firstly approximately half of the recovery of the label is lost in the tricarboxylic acid cycle [7]-[10], and secondly its appearance in breath is delayed by its passage through the bicarbonate pools, which leads to a reduced and blunted signal in comparison with scintigraphy (Fig. 1).

Recently, a "self-correction" mathematical model has been proposed to estimate GE using breath measurement as the input data [11]. Model parameters were found to highly correlate with the ones from the gamma scintigraphy test although its identification requires that the $^{13}\text{CO}_2$ in breath is well defined and that GE is not severely delayed (Fig. 2) as frequently happens in many pathological states such as obesity and type 2 diabetes mellitus [12][13].

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The application of some prior knowledge to the statistical inference of the parameters, within the context of a Bayesian framework, is suggested as a sufficient tool to overcome the deficiency in the data when GE is delayed. Bayesian techniques allow the investigator to include some information

II. METHODS

A. Dataset

A number of studies previously conducted at our laboratories have been reanalysed for this work (Table I).

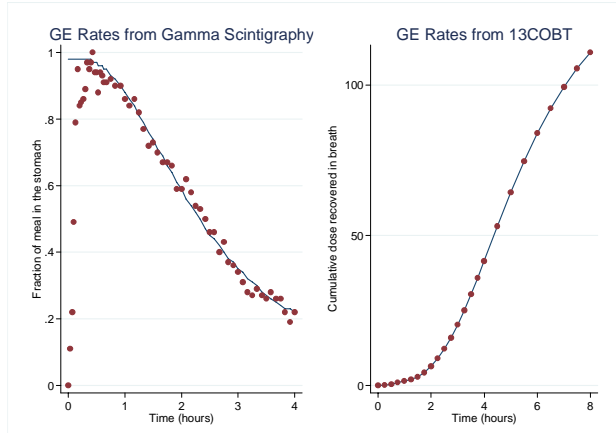


Fig. 1 Gastric emptying patterns as illustrated by a Gamma Scintigraphy Test(left panel) and a ¹³COBT (right panel).

before the analysis is commenced. In practice this is done by defining probability distributions for the model's macroparameters which are subsequently updated by the measurements (data), producing a full probability model. This can be done either by allowing these parameters to vary freely individually or by choosing to allow them to share a number of common properties and characteristics in the context of a hierarchical setting.

TABLE I
STUDIES USED IN THE STATISTICAL ANALYSIS

No	Study	Breath Datasets	Ref.
1	Frequent Feasibility Feeding study	16	[14]
2	Frequent Feeding study	32	[14]
3	Obesity Study	32	[15]
4	Meal Size study	36	[16]
5	Meal Composition study	48	[16]

In all a total of 164 sets of breath test data obtained from a large population (lean and obese subjects) were reanalyzed simultaneously using a Bayesian hierarchical model. The reader is referred to the citations in Table I for more information regarding the protocols.

B. Generic Protocol for the Breath Test

The studies were performed in the volunteer suite at MRC Human Nutrition Research (MRC-HNR), Cambridge, UK and were approved by the Local Research Ethics Committee. All the reported investigations were performed on healthy adults with no history of gastrointestinal disorder. Informed written consent to the tests was obtained from each subject following the receipt of written explanations of the protocol and purpose of the study.

C. Study-day protocol

Subjects were asked to abstain from alcohol and strenuous physical activity, and to fast from 8.00 pm on the day before being studied. To prevent dehydration a single glass of water was allowed on waking on the morning of the study. On arrival at the MRC-HNR height (without shoes) was measured to the nearest 1 cm and weight determined to the nearest 0.01 kg for the estimation of basal metabolic rate (BMR) [17]. The ¹³COBT using an egg-based meal, with a standard energy content of 2MJ. The egg was separated and a standard dose of 100µL of ¹³C-octanoic acid (621µmole) added to the yolk. The egg was then dry-fried in a non-stick pan, and served with 3 slices of toasted bread spread with a total of 10g butter, 100mL of orange juice and 100mL water. Subjects were asked to consume the meal in less than ten minutes.

Basal samples of breath were collected prior to the meal being consumed and continued for six hours. For the first four hours samples were taken every fifteen minutes, and every half hour for the final two-hour period. All breath samples were collected in duplicate. Isotope analysis was performed using isotope ratio mass spectrometry (IRMS), with a reference gas traceable to an international standard V-(PDB).

The calculations were performed as follows:

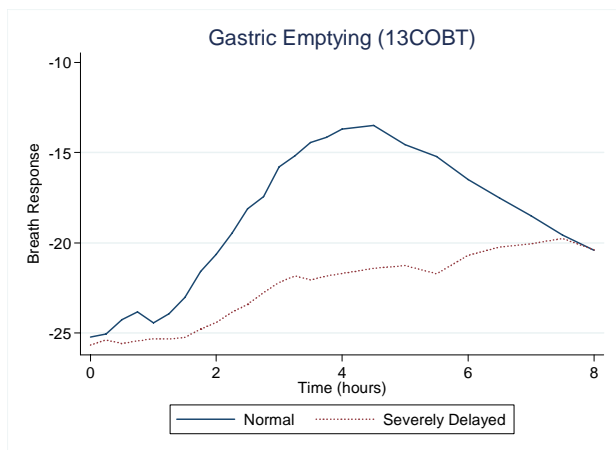


Fig. 2 Illustration of a normal and a severely delayed Gastric Emptying.

This work aims to introduce a Bayesian Hierarchical Model (BHM) into the ¹³COBT for the estimation of GE in a wide range of cases comprising well- and poorly- defined breath recovery curves. For this purpose we exploited a large dataset from several studies conducted in our laboratories and which have already been reported in the literature.

CO₂ production rate (mole/hr),

$$F_{CO_2}(n) = 0.04518 W(n)^{0.5378} H(n)^{0.3964} \quad (1)$$

from the formula given by [18], where $W(n)$ is the weight (kg) and $H(n)$ the height (m) for the n^{th} subject.

The isotope data was fitted to curves according to (2)

$$\delta(n,t) = \delta_b(n) + \frac{1000 \cdot d}{(PDB) \cdot F_{CO_2}(n)} F_{\infty}(n) k(n) \beta(n) (1 - \exp\{-k(n)t\})^{\beta(n)-1} \cdot \exp\{-k(n)t\} \quad (2)$$

where $F_{\infty}(n)$ (the fraction of the dose recoverable in breath), $k(n)$, and $\beta(n)$ are parameters of the fit for the n^{th} subject, d is the isotope dose given, PDB the isotopic composition of the international standard, and $\delta(n,t)$ and $\delta_b(n)$ (‰) the measured isotopic compositions with respect to PDB for each of the breath test at time t and in the basal state respectively.

From the coefficients of the fit two parameters descriptive of the gastric emptying process were calculated [19]

$$t_{1/2}(n) = \frac{-\text{Ln}(1 - 2^{-1/\beta(n)})}{k(n)} \quad (3)$$

$$t_{lag}(n) = \frac{\text{Ln}\{\beta(n)\}}{k(n)} \quad (4)$$

D. Bayesian Hierarchical Analysis

Bayesian modelling was performed using a conditional BHM consisting of the available breath data ($k = 1,2,\dots,164$) and a degree of prior information embedded to the unknown parameter vector $\theta(n) = \{F_{\infty}(n), k(n)\}$ from which the two parameters of interest $\{t_{1/2}^{BAY}(n), t_{lag}^{BAY}(n)\}$ were then estimated. According to Bayesian inference, prior information was updated from the available dataset to formulate conditional probability distributions known as *posteriors*. Posterior distributions are weighted products between the likelihood of the data and the prior information according to Bayes Theorem [20]

$$p(\theta(n) | y(n)) = \frac{p(y(n) | \theta(n))p(\theta(n))}{p(y(n))} \quad (5)$$

where $y(n)$ is the available data (breath test measurement $\delta(n,t)$ for the n^{th} subject obtained at time $t = 1,2,\dots,25$), θ is the unknown parameter vector, $p(\theta(n))$ is the probability vector consisting of the prior beliefs, $p(y(n) | \theta(n))$ is the likelihood, $p(y(n))$ is a scaling factor, and $p(\theta(n) | y(n))$ is the posterior probability distribution vector. By omitting the scaling factor $p(y(n))$ which is independent on θ one can obtain a reduced form of Bayes theorem,

$$p(\theta(n) | y(n)) \propto p(y(n) | \theta(n))p(\theta(n)) \quad (6)$$

We let individual parameters of fit $F_{\infty}^{BAY}(n), k^{BAY}(n)$ depending on other hyperparameters $F_{\infty}^{BAY}(p), k^{BAY}(p)$ which were assigned vague non-informative priors (p for population). The richness of our data and the fact that all subjects underwent the same protocol, allowed us to build a hierarchical setting with parameters borrowing strength from each other, as illustrated from the graphical model in Figure 3.

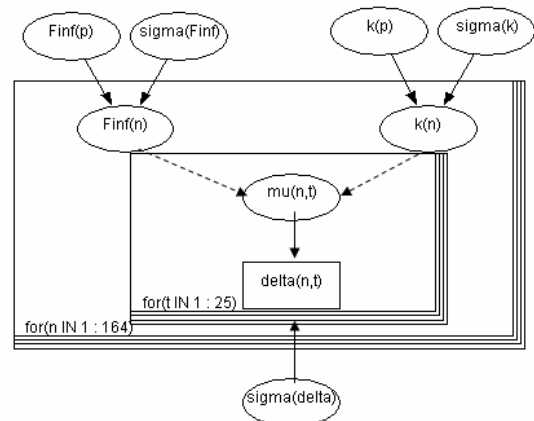


Fig. 3 Graphical (Doodle) representation of the Bayesian Hierarchical Model used in this study

The commercially available computer package WINBUGS [21] was used to implement the model. WinBUGS was used to generate two Markov Chains [22] comprising 6000 samples for each of the unknown parameters. The first 1000 samples were used as the "burn-in" and the rest (5000) for the posterior sampling. The entire process took approximately 34 minutes in a standard desktop workstation.

E. BHM versus NLS

Comparison of results from individual studies with their Non-linear least squares (NLS) counterparts previously obtained using MS Excel was used to assess the performance

of the Bayesian method. Parameter estimates are reported as posterior means \pm standard deviation (SD) for the BHM ($F_{\infty}^{BAY}(p), k^{BAY}(p), t_{1/2}^{BAY}(n), t_{lag}^{BAY}(n)$) and point estimates \pm standard deviations for the NLS ($t_{1/2}^{NLS}(n), t_{lag}^{NLS}(n)$). Pearson correlation was used to assess the agreement of the results obtained by the two methods and statistical significance using a 5% significance level was determined using a paired t-test.

III. RESULTS

The global distribution defining the parameters $F_{\infty}^{BAY}(p)$, and $k^{BAY}(p)$ were all found to be near-normally distributed (mean and median coincident), with symmetrical confidence limits. $F_{\infty}^{BAY}(p)$ was found to be $42.9 \pm 0.8\%$ (mean \pm SD) and $k^{BAY}(p) = 0.511 \pm 0.012 \text{hr}^{-1}$. The ranges of the individual gastric emptying time parameters were $1.66 \text{hr} < t_{lag}^{BAY} < 7.25 \text{hr}$, and $2.23 \text{hr} < t_{1/2}^{BAY} < 8.07 \text{hr}$. In general the standard deviation of the individual value of the parameter was found to increase with its absolute value, with the average coefficient of variation (c.v.) being 2.2%, and 2.7% for t_{lag}^{BAY} and $t_{1/2}^{BAY}$ respectively. The β parameter which is also obtained from the fitted curve and is closely associated to the derivation of the key parameters ($t_{lag}, t_{1/2}$) was successfully obtained by both the BHM and the NLS methods. It is worth mentioning that β derived from the Bayesian approach (β^{BAY}) was much larger for obese subjects compared to its values associated with leans.

Bayesian analysis and the BHM implemented in WinBUGS returned a successful fit and derived estimates for all subjects in contrast to the NLS which returned unsatisfactory fitting for all individuals with a delayed GE. A representative illustration of the Bayesian model fit is shown in Fig. 4.

Comparison of the two estimates (t_{lag}), and ($t_{1/2}$) from the NLS and Bayesian methods is indicative of the 'borrowing of strength' effect featured in the hierarchical analysis (Fig. 5). Both parameters obtained from the two methods were highly correlated with regression lines being identical to the unity (slopes equal to 1, $r = 0.84$ and $r = 0.82$ for t_{lag} and $t_{1/2}$ respectively). Further paired t-tests did not reveal any statistical difference for t_{lag} and $t_{1/2}$ derived from the two methods.

IV. DISCUSSION

In this paper it is clearly demonstrated that Bayesian analysis is a superior approach to estimate gastric emptying in a large dataset of subjects obtained from different studies in the literature. Furthermore, it was observed that the Bayesian hierarchical model is capable to fully interpret breath data obtained from an $^{13}\text{COBT}$ even in cases where GE was severely delayed. Moreover, the Bayesian method was found adequate to fully overcome problematic issues associated to

the conventional NLS such as failures in model's fitting, inconsistent data arising when GE is delayed and large uncertainty across the parameters.

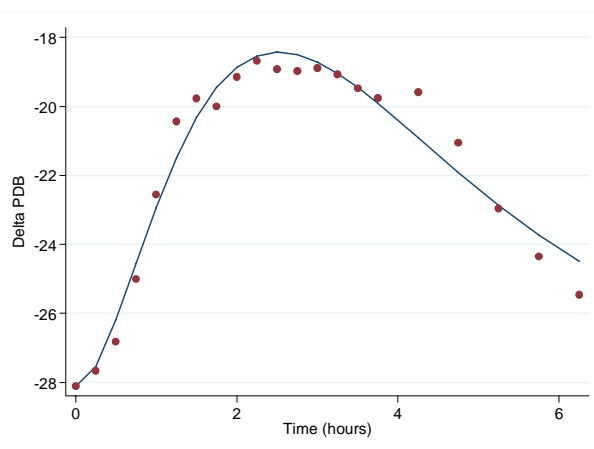


Fig. 4 Raw breath test results and the Bayesian fit.

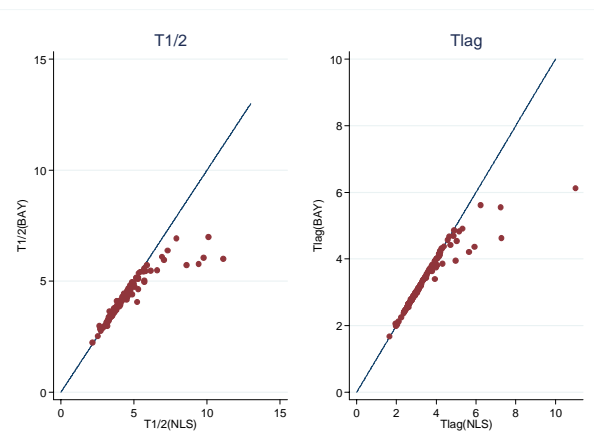


Fig. 5 Regression lines for $t_{1/2}$ (left panel) and t_{lag} (right panel). A strong agreement was observed between the two methods.

The use of the commercially available computer package WinBUGS allowed the satisfactory generation of two Markov Chains from which we derived posterior means with the associated shape of uncertainty (probability distributions) for each of the parameters. Furthermore, the program allowed the automatic generation of the limits of credibility for all parameters.

The adoption of a hierarchical setting was shown to reduce the labour of the computational analysis compared to the classical individual approach. The intensiveness and complexity of Bayesian analysis has been mentioned many times in the literature [23]. In the present analysis, the time required for the model's fit was slightly more than 30 minutes which compares favourably to other methods particularly when bearing in mind all the extra features associated to the WinBUGS package.

In addition, there was strong correlation between the two methods especially in cases where the gastric emptying was not ill-posed. Similar regression figures have been also reported by others [4]. However, the significant advancement of the Bayesian method was clearer when dealing with subjects with a severely delayed GE. In contrast to the NLS, Bayesian method returned estimates and a successful modelling for all subjects. Bayesian analysis was able to discriminate between lean and obese subjects based on their β parameter. It was found that β^{BAY} parameter was greater in obese people who feature a delayed GE, something that is in concordance with other studies in the literature [3].

The main advantage of the Bayesian approach is the ability to provide theoretically self-consistent and plausible estimates of individual and population parameters, albeit with extra care being required during data preparation.

In summary Bayesian hierarchical methods provide a robust and reliable way to analyses the gastric emptying breath test. The methods avoid parameter estimation failure in cases where data quality is sub-optimal, yet reproduce the results of standard non-linear least squares methods when the data is well-behaved. We would recommend that the WinBUGS package be adopted routinely for the estimation of gastric emptying by ^{13}C -octanoate breath test.

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