# A Comparative Analysis of Modulation Control Strategies for Cascade H-Bridge 11-Level Inverter

Joshi Manohar, V., Sujatha, P., and Anjaneyulu K. S. R.

Abstract—The range of the output power is a very important and evident limitation of two-level inverters. In order to overcome this disadvantage, multilevel inverters are introduced. Recently, Cascade H-Bridge inverters have emerged as one of the popular converter topologies used in numerous industrial applications. The modulation switching strategies such as phase shifted carrier based Pulse Width Modulation (PWM) technique and Stair case modulation with Selective Harmonic Elimination (SHE) PWM technique are generally used. NR method is used to solve highly non linear transcendental equations which are formed by SHEPWM method. Generally NR method has a drawback of requiring good initial guess but in this paper a new approach is implemented for NR method with any random initial guess. A three phase CHB 11-level inverter is chosen for analysis. MATLAB/SIMULINK programming environment and harmonic profiles are compared. Finally this paper presents a method at fundamental switching frequency with least % THD<sub>V</sub>.

**Keywords**—Cascade H-bridge 11- level Inverter, NR method, Phase shifted carrier based pulse width modulation(PSCPWM), Selective Harmonic Elimination Pulse Width Modulation (SHEPWM), Total Harmonic Distortion (%THD<sub>v</sub>).

## I. INTRODUCTION

NOW-A-DAYS industrial applications needs higher power rating which reached to mega watt range. For a medium voltage grid, it is troublesome to connect only one power semiconductor switch directly [1]. As a result, multilevel power converter structure has been introduced as an alternative in high power and medium voltage applications.

A multilevel converter not only achieves high power ratings, but also enables the use of renewable energy sources such as photovoltaic, wind, and fuel cells can be easily interfaced to a multilevel converter system for medium voltage high power drives, distributed energy sources and hybrid electric vehicles [2], [3]. The range of output power is limited in two level inverters, this disadvantage is overcome by multilevel inverter and they have features such as high reliability due to its modular topology, less distorted input current and less switching losses [4].

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Three multilevel converter topologies have commercially come into existence: Neutral Point Clamped (NPC), cascade H-bridge (CHB) and Flying Capacitors (FCs) [5]. Depending upon switching frequency the modulation strategies are classified into low switching frequency (fundamental switching frequency and high switching frequency. High switching frequency methods employ switching frequency in order of several kHz.

The major advantage of traditional PWM methods employing much higher frequencies concerns harmonics but some times higher frequency causes undesirable harmonics where filtering is much easier and less expensive. Also, there is no power dissipation because generated harmonics might be above the band width of actual systems. But high switching frequency leads to high switching losses there by less converter efficiency, especially when used in high power applications [6]. Fundamental switching frequency results in less switching losses and less thermal losses, which results high converter efficiency. This method is best suited for MV drives. However, this method produces lower order of harmonics.

This paper is organized as follows: Section II presents brief review on Cascade H-bridge 11-level inverter. Section III presents phase shifted carrier based PWM technique. Section IV presents Selective Harmonic Elimination PWM technique and solving non linear transcendental trigonometric equations by using Newton-Raphson method with any random initial guess. Both the methods are simulated in MATLAB/SIMULINK and comparative harmonic analysis is carried out in Section V.

## II. CASCADE MULTILEVEL INVERTER

Among the topologies of multilevel inverter mentioned in Section I, Cascade Multilevel Inverter (CMLI) is one of the most important topology because of following features such as: no specially designed transformer is needed as compared to multi pulse inverter, modular structure with simple switching strategy, occupies less space and ability to synthesize better harmonic spectrum [7].

The CMLI usually consists of a number of H-bridge inverter units with separate dc source for each unit and is connected in cascade or series as shown in Fig. 1. Each H-bridge can produce three different voltage levels:  $+V_{dc}$ , 0, and  $-V_{dc}$ . The AC output voltage of each H-bridge is connected in series such that the synthesized output voltage waveform is the sum

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of all of the individual H-bridge output voltages. By connecting the sufficient number of H-bridges in cascade and using proper modulation scheme, a nearly sinusoidal output voltage waveform can be synthesized.

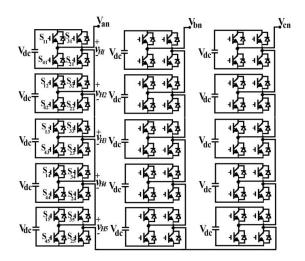


Fig. 1 Three phase cascade H- bridge 11- level inverter

The general rule for the number of levels in the output phase - to - neutral voltage in cascaded single - phase H - bridge multilevel inverter is 2s+1, where 's' is the number of H-bridges used per phase. Fig. 3 shows an 11-level output phase voltage waveform using five H-bridges per phase. The magnitude of the ac output phase voltage is sum of output voltages of all H bridges in phase. For

$$V_{an} = V_{H1} + V_{H2} + V_{H3} + V_{H4} + V_{H5}$$
 (1)

#### III. MODULATION CONTROL TECHNIQUES

The modulation control techniques for multi level inverters can be classified according to switching frequency [1]. Modulation techniques which have many commutations for the power semiconductors in one period of the fundamental output voltage have high switching frequency. Very popular methods in industrial application are carrier based PWM with triangular carriers, they are: phase shifted carrier based and level shifted carrier based PWM schemes.

Modulation control techniques that work with low switching frequency generally perform one or two commutation of the power semi conductors during one cycle of the output voltage, generating stair case waveform. For this low switching frequency, popular control technique is selective harmonic elimination PWM method.

### A. Phase-Shifted Carrier Based Pwm Technique

Generally, multilevel inverter with m voltage levels requires (m-1) triangular carriers. All the carriers have same frequency and same peak-to- peak amplitude with phase shift. The phase shift ( $\phi_{cr}$ ) between adjacent carrier waves is given by

$$\phi_{\rm cr} = 360^0 / (m-1) \tag{2}$$

The modulating signal is usually a three-phase sinusoidal wave with adjustable amplitude and frequency. By comparing the modulated wave with the carrier waves gate signals are generated. For the case of simplicity seven level CHB inverter is considered as shown in Fig. 2 (a). In this case six triangular signals are required with  $60^{0}$  phase displacement between them. In Fig. 2 (b), phase A modulating wave  $(V_{ma})$  is considered and carriers  $V_{cr1},\,V_{cr2},\,V_{cr3}$  are used to generate gatings for switches  $S_{11}\,S_{12},\,S_{13}.$  Other three carriers  $V_{cr1},\,V_{cr2},\,V_{cr3}.$  These carriers produce gatings for switches  $S_{31}\,S_{32},\,S_{33}$  of the H – bridge cells. The gate signals for other switches are not represented here because these switches operate in complementary manner with corresponding to their upper switches. Detailed explanation is presented in [8], [9].

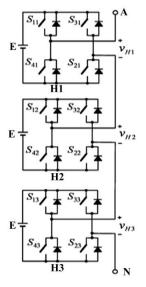


Fig. 2 (a) Per Phase diagram of CHB 7-level inverter

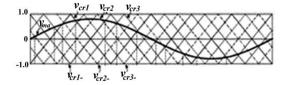


Fig. 2 (b) Carrier waves and modulating wave for Phase A in CHB 7 Level inverter

For cascade H-bridge 11-level inverter, it needs ten triangular carrier signals with phase displacement of  $36^{0}$ . The carrier waves  $V_{cr1}, V_{cr2}, V_{cr3}, V_{cr4}$  and  $V_{cr5}$  are used to generate gating signals for the upper switches  $S_{11}$   $S_{12}$ ,  $S_{13}$ ,  $S_{14}$  and  $S_{15}$  in the left leg of power cells as shown in Fig. 1.

The carrier waves  $V_{cr1}$ ,  $V_{cr2}$ ,  $V_{cr3}$ ,  $V_{cr4}$  and  $V_{cr5}$  are  $180^{\circ}$  out of phase with  $V_{cr1}$ ,  $V_{cr2}$ ,  $V_{cr3}$ ,  $V_{cr4}$  and  $V_{cr5}$  and produce gating signals  $S_{31}$ ,  $S_{32}$ ,  $S_{33}$ ,  $S_{34}$  and  $S_{35}$ . Developed simulink model is simulated at different modulation indices and %THDv is observed at each modulation index. The phase

voltage waveform of cascade H- bridge inverter has 11 voltage steps: +5E, +4E, +3E, +2E, +E, 0, -E,-2E,-3E,-4E and -5E.

#### B. Selective Harmonic Elimination Pwm Technique

Selective harmonic elimination (SHE) is a well known technique at fundamental frequency to control multilevel inverter with low switching losses and better harmonic spectrum [10]. The non linear transcendental equations which are formed by this method are solved by using NR method.

In general, the Fourier series expansion of the staircase output voltage waveform as shown in Fig. 3 is given by

$$v_{an}(\omega t) = \sum_{k=1,3,5,\dots}^{\infty} \frac{4V_{dc}}{k\pi} (\cos(k\alpha_1) + \cos(k\alpha_2) + \dots + \cos(k\alpha_s)) \sin(k\omega t)$$
(3)

where 's' is the number of H-bridges connected in cascade per phase. In this, five number of H-bridges are connected per phase. Where  $V_{dc}$  is the voltage of H- bridge. The angles are limited to between  $0^0$  and  $90^0\,(0 \le \alpha \le 90^0)$ . Because of an odd quarter-wave symmetry, all even order harmonics zero. It is not necessary to eliminate triplen harmonics because they will be eliminated in the line to line output voltage. Subsequently  $V_1$  becomes:

$$\frac{4V_{\rm dc}}{\pi}(\cos(\alpha_1) + \cos(\alpha_2) + \dots + \cos(\alpha_s)) = V_1 \tag{4}$$

In this paper, an 11-level inverter is chosen as a case study. Thus, with five angles as degrees of freedom, it is possible to eliminate four lower order harmonics i.e. 5<sup>th</sup>, 7<sup>th</sup>, 11<sup>th</sup> and 13<sup>th</sup>.

For an 11-level inverter, the following equation should be solved:

$$[\cos(\alpha_1) + \cos(\alpha_2) + \dots + \cos(\alpha_5)]/5 = m_I \cos(5\alpha_1) + \cos(5\alpha_2) + \dots + \cos(5\alpha_5) = 0 \cos(7\alpha_1) + \cos(7\alpha_2) + \dots + \cos(7\alpha_5) = 0 \cos(11\alpha_1) + \cos(11\alpha_2) + \dots + \cos(11\alpha_5) = 0 \cos(13\alpha_1) + \cos(13\alpha_2) + \dots + \cos(13\alpha_5) = 0$$
 (5)

where M<sub>I</sub> is modulation index and defined as

$$M_{\rm I} \triangleq {\pi V_1 / 4_{S} V_{dc}} \qquad (0 \le M_{\rm I} \le 1) \tag{6}$$

In general, the set of (5) can be written in a compact form as

$$F(\alpha) = B(M_i) \tag{7}$$

where, the vectors  $F(\alpha)$  and  $B(M_1)$  are functions of switching angles and modulation index respectively.

The set of (5) are five non linear transcendental trigonometric equations, known as selective harmonic elimination (SHE) equations, can be solved by a number of numerical methods [10], one of the fastest iterative methods is Newton Raphson method [11], [12]. This method begins with any random initial guess and generally converges at a zero of a given system of non linear equations.

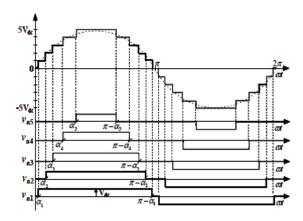


Fig. 3 Output phase voltage waveform of CHB 11-level inverter

The algorithm for The Newton-Raphson method is as follows:

- 1. Assume any random initial guess for switching angles (say  $\alpha_0$ ) such that
- 2.  $0 \le \alpha_1 < \alpha_2 \dots \dots < \alpha_5 \le \frac{\pi}{2}$
- 3 Set M. =0
- 4. Calculate  $F(\alpha_0)$ ,  $B(M_1)$  and jacobian matrix  $J(\alpha_0)$ .
- 5. Compute correction  $\delta \alpha$  during the iteration using relation.  $\Delta \alpha = J^{-1}(\alpha_0)(B(M_1)-F(\alpha_0))$ .
- 6. Update the switching angles i.e.  $\alpha(k+1) = \alpha(k) + \Delta\alpha(k)$
- 7. Perform the  $\alpha(k+1) = cos^{-1} \left( abs \left( COS(\alpha(k+1)) \right) \right)$  transformation to bring switching angles in feasible range i.e. between zero and  $\pi/2$ .
- 8. Repeat the steps (3) to (6) for sufficient number of iterations to attain error goal.
- 9. Substitute  $\alpha_0 = \alpha (k+1)$
- 10. Repeat steps (2) to (8) for whole range of M<sub>I</sub>.
- 11. Increment M<sub>1</sub> by a fixed step.
- 12. Repeat steps (2) to (10) for complete range of M<sub>I</sub>.

The above algorithm is implemented in MATLAB programming environment and the complete analysis is presented in Section IV.

#### IV. SIMULATION AND ANALYSIS

The developed code and simulink model is simulated by using MATLAB/SIMULINK and comparative analysis is presented for both modulation strategies.

# A. Phase Shift Carrier Based PWM Technique

Phase shift carrier based PWM technique is applied on three phase cascade H-bridge 11-level inverter. The developed simulink model is run at various modulation indices from 0 to 1 and at each step  $\% THD_{\rm v}$  is observed, these values are tabulated in Table I, the simulated output voltage at modulation index 1.0 and FFT analysis are presented in Figs. 4 and 5 respectively.

TABLE I %THD <sub>v</sub> vs Modulation Indices							
S.No	$\mathbf{M}_{\mathbf{I}}$	%THD <sub>v</sub>					
1	0.1	138.86					
2	0.2	68.70					
3	0.3	63.53					
4	0.4	56.61					
5	0.5	40.66					
6	0.6	30.59					
7	0.7	26.92					
8	0.8	24.20					
9	0.9	19.75					
10	1	13.85					

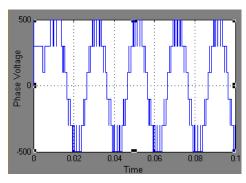


Fig. 4 Output phase voltage waveform for  $M_I = 1.0$ 

From above results in Table I, it is observed that  ${\rm \%THD_v}$  decreases as modulation index increases and minimum  ${\rm \%THD_v}$  observed at modulation index 1, which is found to be 13.83%. From FFT analysis in Fig. 5, it is observed that harmonics of 5<sup>th</sup>, 7<sup>th</sup>, 11<sup>th</sup> and 13<sup>th</sup> orders are still present in output voltage. In order to bring this value to comply IEEE 519-1992 guidelines additional filters are needed, which are quite expensive.

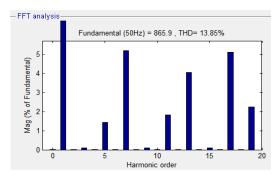


Fig. 5 FFT analysis representing harmonic order of voltage harmonics at  $M_1 = 1$ 

### B. Selective Harmonic Elimination PWM Technique

The non linear transcendental equations which are formed by SHE method are solved by Newton Raphson algorithm. The new approach in developed algorithm is, it can work with any random initial guess. By incrementing  $M_{\rm I}$  from 0 to 1 in steps of 0.001, all solution sets are computed. Graph between switching angles versus modulation indices are shown in Fig. 6.

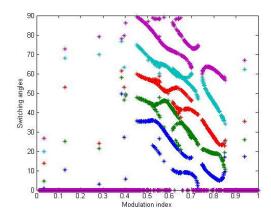


Fig. 6 Switching angles Vs modulation Indices

It can be seen from Fig. 6 that solutions do not exist at lower and upper ends of the modulation indices and also for  $M_1$  = [0.300 0.434], and [0.732 0.742] as error is not zero at these values of  $M_1$ . Multiple solution sets exist for  $M_1$  = [0.510 0.569], [0.615 0.700]. Some solutions are existing in very narrow range of  $M_1$  i.e. at [0.365], [0.387], [0.900], [0.933] and [0.982]. The developed NR algorithm is simulated at different modulation indices in feasible region and at each modulation index %THD $_{\rm v}$  and switching angles are tabulated in Table II. From Table II, it is observed that least %THD $_{\rm v}$  i.e 5.33% is produced at modulation index of  $M_1$  = 0.755.

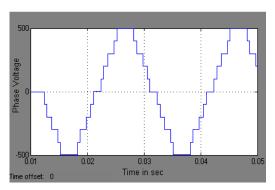


Fig. 7 Output Phase voltage waveform of SHEPWM at  $M_I = 0.755$ 

 $\label{thm:table} TABLE~II\\ \text{\%THD}~_{V}\&~SWITCHING~Angles~in~Degrees$ 

S.No	$M_{I}$	$\alpha_1$	$\alpha_2$	$\alpha_3$	$\alpha_4$	$\alpha_5$	%THD <sub>v</sub>
1.	0.460	35.46	47.39	59.32	73.95	88.73	8.81
2.	0.473	35.33	46.87	58.47	72.40	87.68	8.62
3	0.485	35.33	46.32	57.82	70.96	86.56	8.98
4	0.495	35.44	45.78	57.39	69.77	85.49	8.88
5	0.500	35.52	45.49	57.20	69.20	84.92	8.77
6	0.555	33.75	44.94	53.54	65.22	77.14	7.60
7	0.600	26.64	43.93	51.53	62.39	72.50	7.24
8	0.655	18.98	34.82	51.33	57.94	69.32	6.32
9	0.750	12.79	21.01	35.81	56.59	61.31	5.63
10	0.755	11.66	20.93	34.83	54.41	62.67	5.33
11	0.800	6.569	18.94	27.18	45.13	62.24	5.55

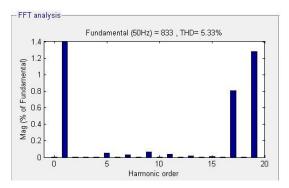


Fig. 8 FFT Analysis representing order of voltage harmonics at  $M_1 = 0.755$ 

This value of %THD also satisfies IEEE 519-1992 harmonic guidelines. The output phase voltage waveform and FFT analysis at  $M_I = 0.755$  are shown in Figs. 7 and 8 respectively. FFT analysis shows all the lower order of the voltage harmonics such as  $5^{th}$ ,  $7^{th}$ ,  $11^{th}$  and  $13^{th}$  are minimised.

#### V. CONCLUSIONS

In this paper comparative analysis is carried out for Phase shifted carrier based pulse width modulation and Selective harmonic PWM strategies, which are applied to three phase cascade H-bridge 11-level inverter. A new approach is proposed in solving non linear transcendental SHE equations by NR method with any random initial guess. By observing the results in section IV, it is observed that least %THD<sub>v</sub> is obtained in SHEPWM control strategy. Its value is found to be 5.33% at modulation index of  $M_I = 0.755$  and it also satisfies IEEE 519-1992 harmonic guidelines. It is also observed from FFT analysis in Fig. 8, all the lower order of harmonics i.e 5<sup>th</sup>, 7<sup>th</sup>, 11<sup>th</sup>, 13<sup>th</sup> are minimised and the switching angles at that instant are presented in Table II. Hence this control strategy is well suited for applications where there is need to eliminate lower order harmonics such as Medium voltage high power drives. Though, Newton-Raphson method is fast iterative method but it needs good initial guess. In order to overcome that draw back, a new approach is presented here to solve non linear transcendental equations by NR method with any random initial guess. However, this method is having a limitation of using for whole range of modulation index. It can be seen in Fig. 6, there are regions where there is no solution for SHE equations in NR method. Further, Intelligent Algorithms such as Genetic Algorithm (GA) and Particle Swarm Optimisation (PSO) may be used to minimize harmonics in that region.

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