

The dynamic model for the i^{th} machine in the power system including its exciter and the STATCOM is expressed in terms of the differential equations given in (1). The circuit configuration of a STATCOM including its location in terms of generator and network buses is shown in Fig.2. A list of the symbols is given in the Nomenclature section.

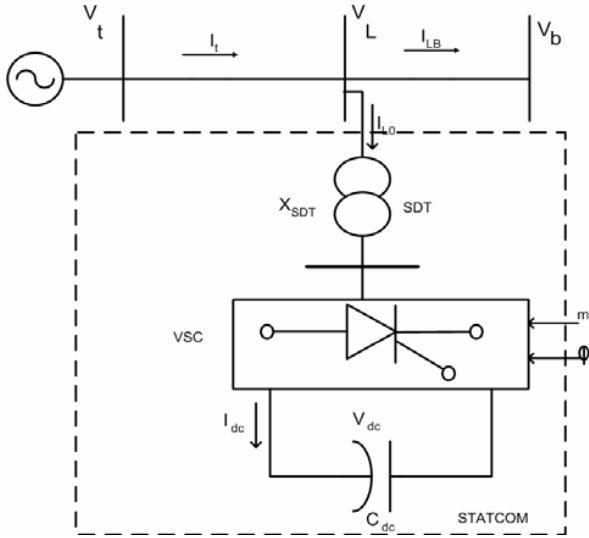


Fig. 2 The STATCOM system representation

$$\begin{aligned} \dot{e}'_{di} &= \left[-e'_{di} + (x_{qi} - x'_{di}) I_{qi} \right] \frac{1}{T'_{qoi}} \\ \dot{e}'_{qi} &= \left[E_{fdi} - e'_{qi} - (x_{di} - x'_{di}) I_{di} \right] \frac{1}{T'_{doi}} \\ \dot{\omega}_i &= -\frac{1}{2H_i} [P_{mi} - P_{ei} - D_i \omega_i] \\ \dot{\delta}_i &= \omega_o \omega_i \\ \dot{E}_{fdi} &= -\frac{1}{T_{Ai}} E_{fdi} - \frac{K_{Ai}}{T_{Ai}} (V_{toi} - V_{ti}) \\ \dot{V}_{DCi} &= \frac{m_i}{C_{DCi}} [I_{sdi} \cos \psi_i + I_{sqi} \sin \psi_i] \end{aligned} \quad (1)$$

The loads are represented by constant impedances and the load buses are eliminated. The network voltage-current variables are converted to machine d-q frames through the transformation matrix $T_r = \text{diag}[e^{j(\delta-\pi/2)}]$ and the non-state variables in (1) are eliminated. The block diagram in Fig. 3 shows the conversion of the variable from the synchronously rotating network reference frame [D-Q] to individual machine frames [d-q]. The dynamic equations for the multi-machine system are then written as,

$$\dot{x} = f[x, u] \quad (2)$$

where, the state vector x is composed of variables $[e'_d, e'_q, \omega, \delta, E_{fd}, V_{DC}]^T$ of each machine, and u is the vector of controls $[m \psi]$ of each STATCOM.

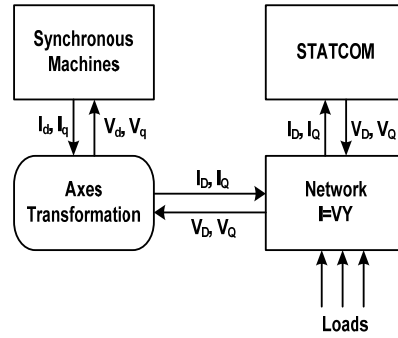


Fig. 3 Diagram showing transformation between the network (D-Q) and machine frames (d-q)

III. ROBUST DESIGN USING LOOP SHAPING TECHNIQUE

The robust control design for the synchronous generator-STATCOM system starts by linearizing the set of equations (2) around a nominal operating point as,

$$\begin{aligned} \dot{x} &= Ax + Bu \\ y &= Hx \end{aligned} \quad (3)$$

The nominal plant transfer function between the input u and selected output variable y is written as,

$$P = H [sI - A]^{-1} B \quad (4)$$

Variations in the plant operating condition is included by a structured uncertainty model as,

$$\tilde{P} = (1 + DW_2)P \quad (5)$$

W_2 is a fixed stable transfer function, the weight, and D is a variable transfer function satisfying $\|D\|_\infty < 1$. In the multiplicative uncertainty model (5), DW_2 is the normalized plant perturbation away from 1. If $\|D\|_\infty < 1$ then

$$\left| \frac{\tilde{P}(j\omega)}{P(j\omega)} - 1 \right| \leq |W_2(j\omega)|, \forall \omega \quad (6)$$

So, $|W_2(j\omega)|$ provides the uncertainty profile and in the frequency plane is the upper boundary of all the normalized plant transfer functions away from 1. For a control function C in cascade with the plant P , the robustness performance and stability measures are satisfied if,

$$\| |W_1 S| + |W_2 T| \|_\infty < 1 \quad (7)$$

In the above, W_1 is a real, rational, stable and minimum phase function. T is the input-output transfer function, the complement of the sensitivity function S .

The basic idea of the graphical loop-shaping method is to construct the loop transfer function $L = PC$ to satisfy the robust performance criterion approximately, and then to obtain the controller from the relationship $C = L/P$. For a monotonically decreasing function W_1 , it can be shown that at low frequency the open-loop transfer function L should satisfy,

$$|L| > \frac{|W_1|}{1 - |W_2|} \quad (8)$$

while, for high frequency,

$$|L| < \frac{1 - |W_1|}{|W_2|} \approx \frac{1}{|W_2|} \quad (9)$$

At high frequency $|L|$ should roll off at least as quickly as $|P|$ does. This ensures properness of C . The general features of open loop transfer function are that the gain at low frequency should be large enough, and $|L|$ should not drop-off too quickly near the crossover frequency to avoid internal instability. Steps in the controller design include: determination of dB-magnitude plots for P and \tilde{P} , finding W_2 from (6), choosing L subject to (7-9), checking for the robustness criteria, constructing C from L/P and checking internal stability. The process is repeated until satisfactory L and C are obtained. The iterative determination of controller C from the choice of open-loop function L , subject to the constraints, are accelerated by incorporating a particle swarm optimization (PSO) technique in the algorithm.

IV. PARTICLE SWARM OPTIMIZATION

The particle swarm optimization is a population-based optimization tool developed by Eberhart and Kennedy [10]. PSO technique conducts search using a population of particles where each particle is a candidate solution. Particles change their positions by flying around in a multidimensional search space until either computational limits are exceeded or relatively unchanging positions have been encountered. During the flight each particle adjusts its position according to the experience of its own as well as that of the neighboring particle [10-12]. In the PSO algorithm, each particle updates its velocity and position by the relationship,

$$V_i(k+1) = Q(k)V_i(k) + K_1 \text{rand}_1[xx] \{X_{pbest}(k) - X_i(k)\} + K_2 \text{rand}_2[xx] \{X_{gbest} - X_i(k)\} \quad (10)$$

$$X_i(k+1) = X_i(k) + V_i(k) \quad (11)$$

where, K_1 and K_2 are two positive constants, $\text{rand}_1(xx)$ and $\text{rand}_2(xx)$ are random numbers in the range $[0, 1]$, and Q is the inertia weight. X_i represents position of the i -th particle and V_i is its velocity. The first term in (10) depends on the former velocity of the particle(s), the second is the cognition modal, which includes particles' own thinking and memory, and the third part represents the socio-psychological adaptation knowledge of the particles. The three parts together determine the space searching ability. The first part has the ability to search for local minimum. The second part causes the swarm to have a strong ability to search for global minimum and avoid local minimum. The third part reflects the information sharing among the particles. Under the influence of the three parts, the particle can reach the best position.

The PSO algorithm starts by initializing the velocity and position of the population of particles randomly. In the first iteration the 'global best' and the 'local best' are set equal. The process is repeated until some acceptable solution is reached or the maximum number of iterations exceeded.

In the proposed PSO based loop-shaping approach the robust controller structure is pre-selected as,

$$C(s) = \frac{b_m s^m + \dots + b_1 s + b_0}{a_n s^n + \dots + a_1 s + a_0} \quad (12)$$

The open loop function L is then constructed from $L(s) = P(s)C(s)$. The performance index J to be minimized is chosen to include the robustness criteria as well as the constraints on L given by (8-9) and is expressed as,

$$J = \sum_{i=1}^N r_i J_{Bi} + r_o J_s \quad (13)$$

where, J_{Bi} are the robust stability indices and J_s is the stability index of the over-all closed loop system. r_i and r_o are the penalties associated with the respective indices and N is the number of frequency points in Bode plot of $L(j\omega)$. At each frequency ω_i , the magnitude of open-loop transmission $L(j\omega_i)$ is calculated and then checked to see whether or not the robust stability bound is satisfied at that frequency. The robust stability indices are defined by,

$$J_{Bi} = \begin{cases} 0, & \text{if bound at } \omega_i \text{ is satisfied} \\ 1, & \text{otherwise} \end{cases} \quad (14)$$

$i = 1, 2, 3, \dots, N$

The stability of the closed loop nominal system is tested by solving the roots of characteristic polynomial and then checking whether all the roots lie in the left side of the complex plane. The stability index J_s is defined as,

$$J_s = \begin{cases} 0, & \text{if stable} \\ 1, & \text{otherwise} \end{cases} \quad (15)$$

The coefficients b_m, \dots, b_1 and a_n, \dots, a_1 are searched by the PSO algorithm to minimize J subject to the constraints; a_n being set to 1. The flow chart for the proposed PSO based loop-shaping algorithm is shown in Fig. 4.

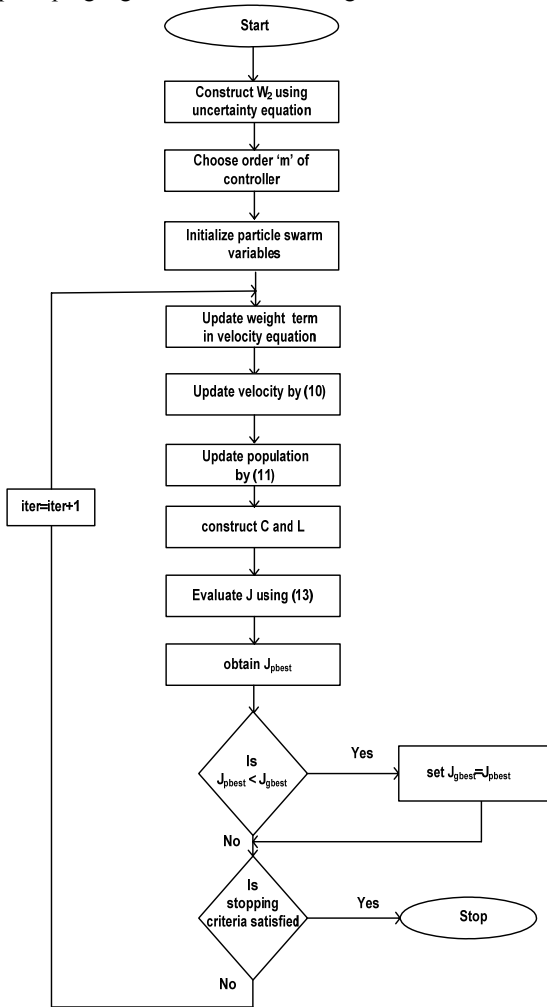


Fig. 4 Flow chart for the proposed PSO based loop-shaping.

V. ROBUST DESIGN USING LOOP SHAPING TECHNIQUE

The robust control design was implemented on the multi-machine power system shown in Fig.1. Considering a STATCOM between generator 2 and bus 9, the detailed dynamic model is expressed in terms of 20 first order equations. A reduced order model was obtained considering the angular speed deviation ($\Delta\omega_2$) of the generator #2 as the plant output and voltage modulation index m of the STATCOM as the input. A balanced realization technique was employed for the reduction procedure [13]. The plant transfer function of the minimum order model which fits that of the detailed model was obtained from several simulation studies. The minimal plant function of the reduced system for the nominal operating point was found to be,

$$P = \frac{-100s(s-40.93)(s+15.27)(s^2+0.66s+17.22)}{s(s+30)(s+4.44)(s+0.33)(s^2+0.62s+31.19)} \quad (16)$$

Off-nominal outputs between 0.4 and 1.4 pu and power factor from 0.8 lagging to 0.8 leading were considered for the different generators. The quantity, $|\tilde{P}(j\omega)/P(j\omega)-1|$ for each perturbed plant was constructed and the uncertainty profile was fitted to the following function,

$$W_2(s) = \frac{0.191(s+20.6)(s+0.86)}{(s^2+10.01s+25.57)} \quad (17)$$

A Butterworth filter satisfying all the properties for $W_1(s)$ is selected as,

$$W_1(s) = \frac{K_d f_c^2}{s^3 + 2s^2 f_c + 2s f_c^2 + f_c^3} \quad (18)$$

For $K_d = 0.0001$ and $f_c = 1$, and for a choice of open-loop transfer function L which satisfies the loop-shaping properties outlined in section 3, the relationship $L=PC$ yield the following controller function,

$$C(s) = \frac{16.88(s+2.63)(s+0.71)(s^2+0.63s+0.39)(s^2+0.46s+0.37)}{(s^2+11.41s+79.21)(s^2+1.68s+1.64)(s^2+0.66s+0.67)} \quad (19)$$

VI. THE ROBUST DESIGN WITH PSO

For the reduced order nominal plant transfer function (16), the PSO starts with W_1 and W_2 arrived at through the loop-shaping procedure of section 5. A second order controller function is selected for the robust design. Following the procedure given in section 4, the PSO algorithm converged to yield the control function,

$$C(s) = \frac{12.82(s+7.33)(s+0.23)}{s^2+3.6768s+77.455} \quad (20)$$

The open-loop function $L(s)$ is then obtained as,

$$L(s) = \frac{-1.281 \times 10^3 s(s-40.93)(s+15.27)(s+7.33)(s+0.22)(s^2+0.66s+17.22)}{s(s+30)(s+4.44)(s+0.33)(s^2+3.68s+77.46)(s^2+0.62s+31.19)} \quad (21)$$

The parameters used in the PSO algorithm are: $K_1=K_2=2$; maximum and minimum weights for Q are 1.2 and 0.1, respectively. The population size was taken to be 20 and the maximum number of iterations set to 1500.

By considering the 20th order detailed model of the 4-machine power system, the controller function arrived at by the PSO algorithm is,

$$C(s) = \frac{25 \times 10^3 (s+3.9998)(s+0.0002)}{s^2+0.07454s+2.797} \quad (22)$$

Loop shaping plots relating W_1 , W_2 , and L for reduced order and detailed model with and without PSO are shown in Fig. 5 while, the corresponding performance measures are in Fig. 6. In Fig. 5, the open-loop functions (L) were selected to fit the upper and lower bounds set by (8-9) in all the three cases. With the graphical construction procedure the control structure is more complicated and gave the open-loop function (L) slightly different from those obtained by PSO (b and c). Plot b in Fig. 5 is with the reduced order plant model, while c is with the full-order multi-machine power system model. The plots for the nominal and robust performance measures are shown in Fig. 6. It can be observed that performance measures are almost identical for all the three cases, and that they are well satisfied.

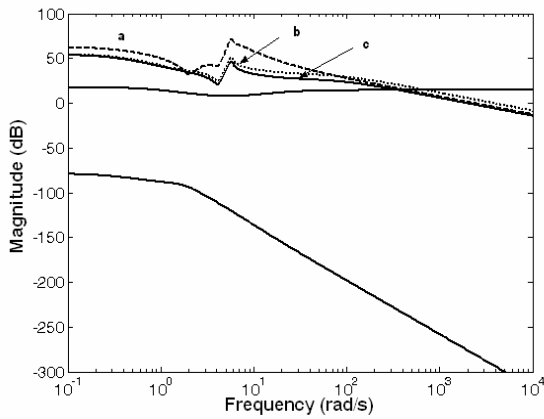


Fig.5 Loop-shaping plots: the open-loop function L for, a) reduced order model through graphical loop-shaping, b) reduced order model through PSO, and c) detailed order model through PSO.

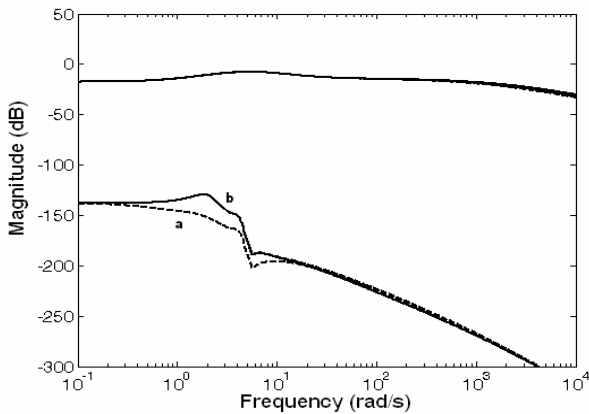


Fig. 6 The nominal and robust performance measures: a) reduced order model through graphical loop-shaping, b) reduced and detailed order models through PSO.

VII. EVALUATION OF THE ROBUST CONTROL

The performance of the designed control was evaluated through simulations of the 4-machine power system given in Fig.1. Comparison of the responses with the original graphical loop-shaping control and PSO based loop-shaping methods are given in Figs. 7 and 8. Fig.7 shows the relative rotor angles of the generators for a 50% torque pulse on generator

#2 for 0.1 sec at nominal loading with a) no STATCOM control, b) PSO based loop-shaping and, c) original loop-shaping, respectively. The nominal plant function was that of the reduced order model obtained through balance realization. Fig. 8 shows the angle variations when a three phase fault for 0.1 sec is applied at bus 2. The relative rotor angle of the generators are shown for, a) no STATCOM control, b) PSO based loop-shaping and, c) original loop-shaping, respectively. This is a severe disturbance, and in the absence of control action the system is transiently unstable. It can be observed that both the graphical and PSO based loop-shaping techniques produce controller functions that give almost identically good transient control. The reduced order model as obtained through through balance realization is employed.

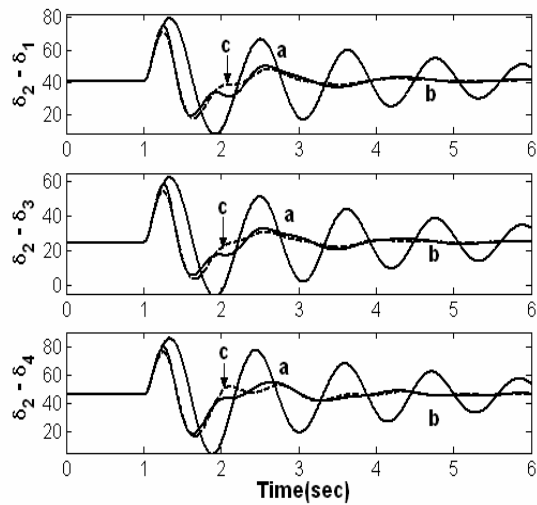


Fig. 7 Comparison of relative angles for a 50% input torque pulse on generator 2 for 0.1s with (a) no control, (b) PSO based loop-shaping, and (c) graphical loop-shaping

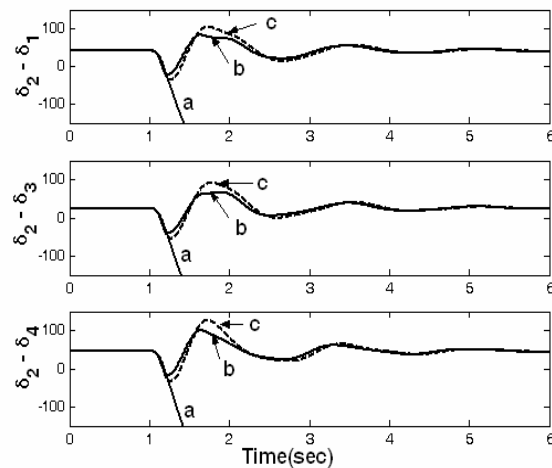


Fig. 8 Relative rotor angles following a 3 phase fault at bus 2 for 0.1 sec with (a) no control, (b) PSO based loop-shaping control, and (c) graphical loop shaping control.

The controller was then tested for a number of other operating conditions. Figs. 9 and 10 show the variation of relative rotor angles for a disturbance of 50% input torque pulse for 0.1 seconds on generator #2 and a three phase fault at bus #2 for 0.1 sec, respectively. The different loading conditions are given in Tables I and II in the Appendix. It can be observed from the figure that the robust controller damps the oscillations very quickly for all these widely different loadings conditions.

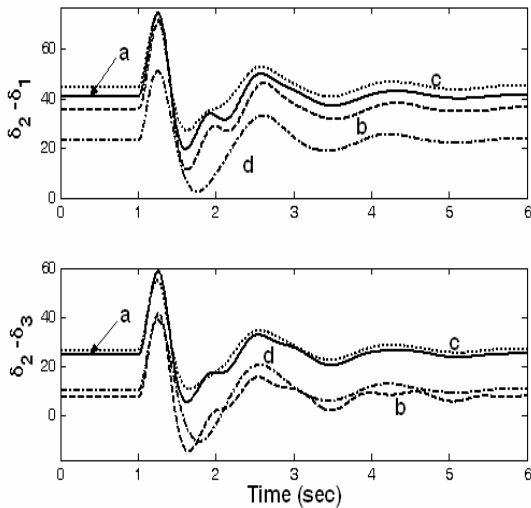


Fig. 9 Relative rotor angle deviations for four different loadings following a 50% torque pulse on shaft of generator #2 for 0.1 sec.

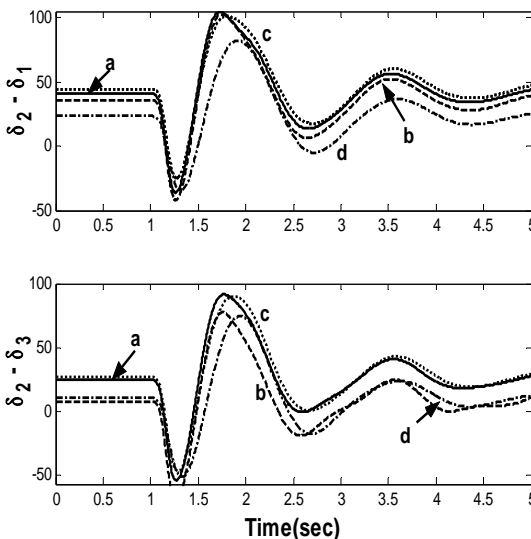


Fig. 10 Relative rotor angle deviations for the loadings of Fig. 9 for a 3 phase fault at bus #2 for 0.1 sec.

VIII. CONCLUSIONS

Robust STATCOM controller for a multi-machine power system has been designed through a graphical loop-shaping procedure. Though it's a powerful method, the graphical loop-shaping technique is handicapped by the dimensionality curse. This has been circumvented by embedding a particle swarm optimization procedure in the loop-shaping design. The advantage of using the PSO is that the order of the controller can be chosen a-priori. The validity of the robust design was verified through a reduced order model obtained through a balanced realization technique. The PSO embedded loop-shaping robust STATCOM controller design is computationally efficient and has been observed to provide very good damping profile over a wide range of operation of the multi-machine power system.

NOMENCLATURE

- δ Generator rotor angle
- ω Rotor speed
- ω_o Base (synchronous) speed
- P_m Mechanical power input
- P_e Electrical power output
- H, D Inertia constant, damping coefficient of generator
- e_q Quadrature (q) axis internal voltage
- E_{fd} Field voltage
- x_d, x_d' Synchronous, transient direct (d) axis reactance
- I_d d-component of armature current
- K_A, T_A Exciter gain, time constant
- V_t Generator terminal voltage
- E_{fdo}, V_{to} Nominal field, terminal voltage
- V_{dc} dc capacitor voltage of STATCOM
- C_{dc} Capacitance of dc capacitor
- m, ψ Modulation index, phase of STATCOM voltage

APPENDIX

TABLE I
GENERATION: P (MW) AND Q (MVAR) FOR VARIOUS TEST CASES

Gen	Case a		Case b		Case c		Case d	
G ₁	23	11	30	22	68	19	12	31
	2	9	7	6			3	
G ₂	70	24	72	36	53	78	33	49
	0	4	5	6	5		0	
G ₃	30	19	57	33	16	74	16	10
	0	3	5	6	5		5	5
G ₄	45	26	67	46	24	11	15	
	0	6	5	1	5	1	7	94

TABLE II
LOAD: P (MW) AND Q (MVAR) FOR VARIOUS TEST CASES

Loads	Case a		Case b		Case c		Case d	
S_A	35 0	19 5	46 0	27 5	27 5	13 5	20 0	15 0
S_B	35 0	19 5	46 0	27 5	17 5	13 5	12 5	17 5
S_C	65 0	37 5	90 0	47 5	41 0	25 0	35 0	25 0
S_D	32 5	15 5	45 0	22 0	15 0	10 0	12 5	75

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